

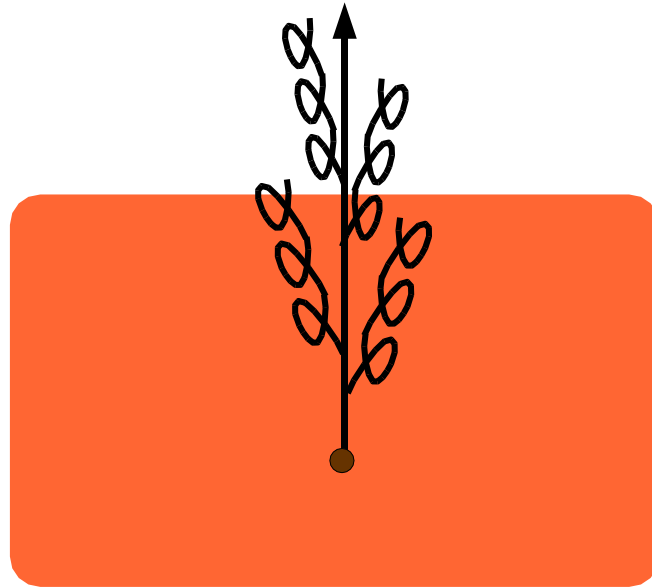
# Particules de grandes impulsions transverses au RHIC

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**Physics Department  
CERN, TH-Division**

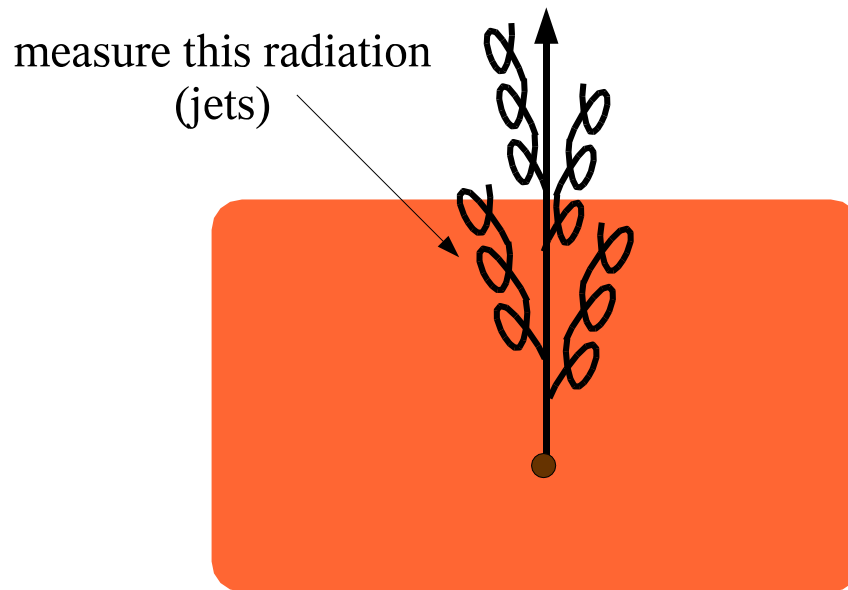
`carlos.salgado@cern.ch`, `http://home.cern.ch/csalgado`

# Jet quenching



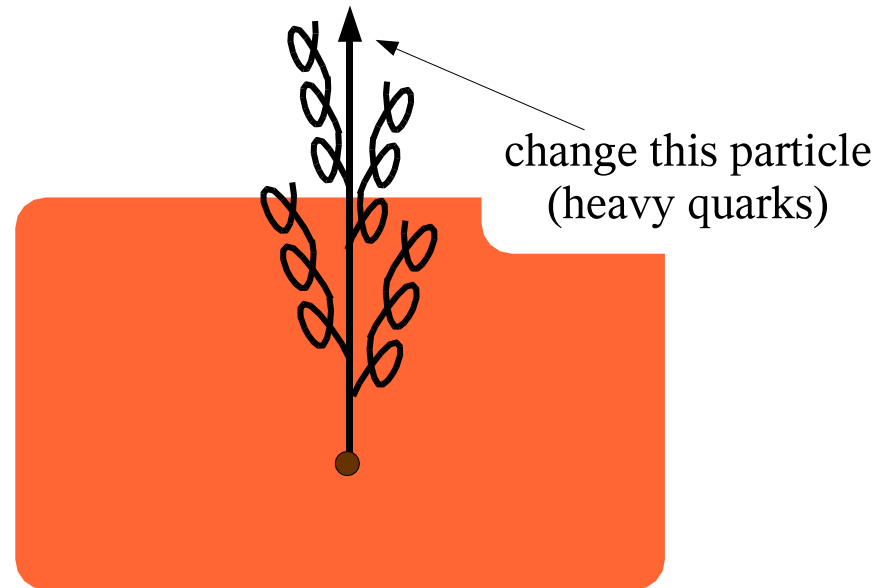
- ⇒ Suppression of light particles at high- $p_t$  observed at RHIC.
- ⇒ Well described by energy loss due to **medium-induced gluon radiation**
- ⇒ Problems: surface emission, trigger bias...

# Jet quenching



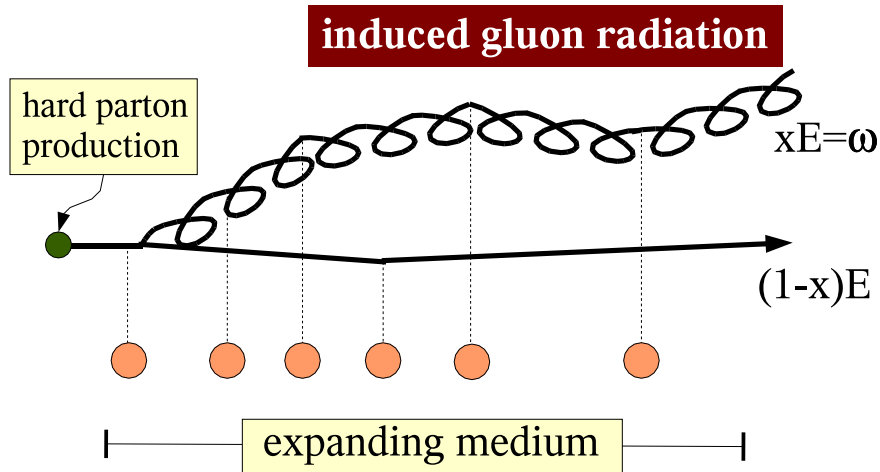
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# Jet quenching



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  - ↪ Well described by energy loss due to **medium-induced gluon radiation**
  - ↪ Problems: surface emission, trigger bias...
- ⇒ Measure the structure of radiated particles → jets
- ⇒ Change the composition of the primary → heavy quarks

# Medium-induced gluon radiation (m=0)



Medium properties: length  $L$ ,  
transport coefficient  $\hat{q} \sim \frac{\mu^2}{\lambda}$

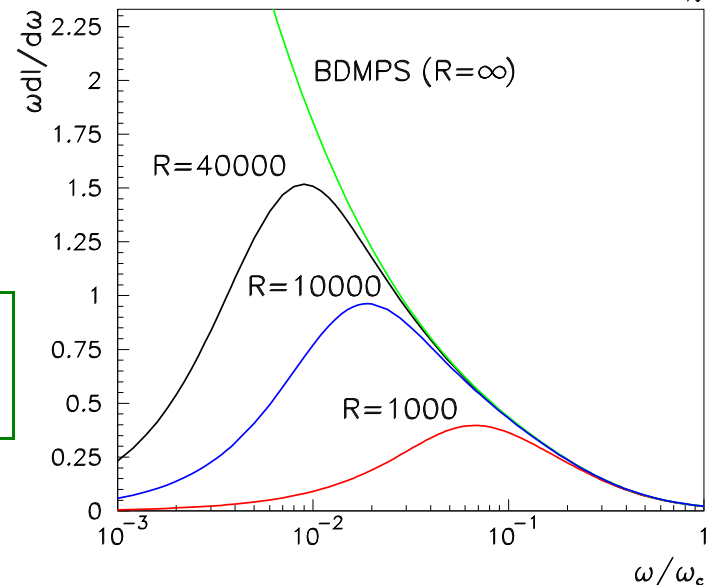
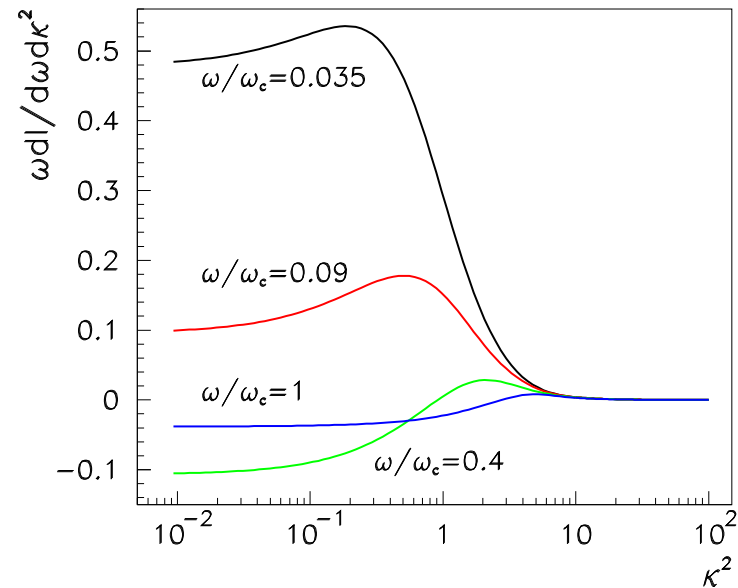
$\Rightarrow k_{\perp, \max}^2 \sim \hat{q}L$ ;  $\kappa^2 \equiv k_{\perp}^2 / \hat{q}L$

$\Rightarrow$  Accumulated phase

$$\varphi = \left\langle \frac{k_{\perp}^2}{2\omega} \Delta z \right\rangle \sim \kappa^2 \frac{\omega_c}{\omega}; \quad \omega_c \equiv \frac{1}{2} \hat{q}L^2$$

Rad. suppressed by coherence

$$\varphi \lesssim 1 \iff \kappa^2 \lesssim \omega/\omega_c$$



# Angular distribution

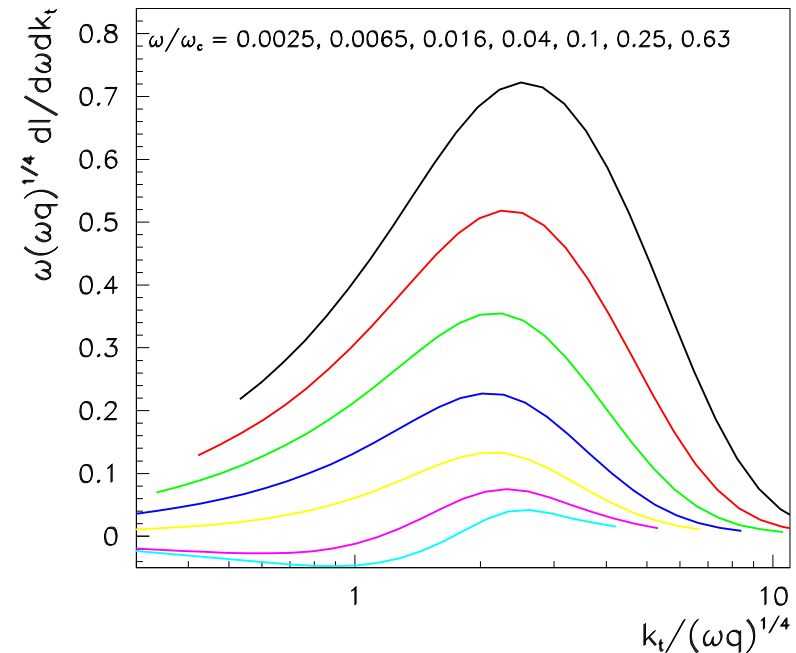
The same spectrum in different variables  $\omega/\omega_c, k_t^2/\sqrt{\omega\hat{q}}$

Heuristic argument

$$t_{\text{form}} \sim \frac{\omega}{k_t^2} \quad k_t^2 \sim \mu^2 \frac{t_{\text{form}}}{\lambda}$$

The transport coefficient is defined as  $\hat{q} = \frac{\mu^2}{\lambda}$

$$k_t^2 \sim \hat{q} t_{\text{form}} \implies k_t^2 \sim \sqrt{\omega\hat{q}}$$

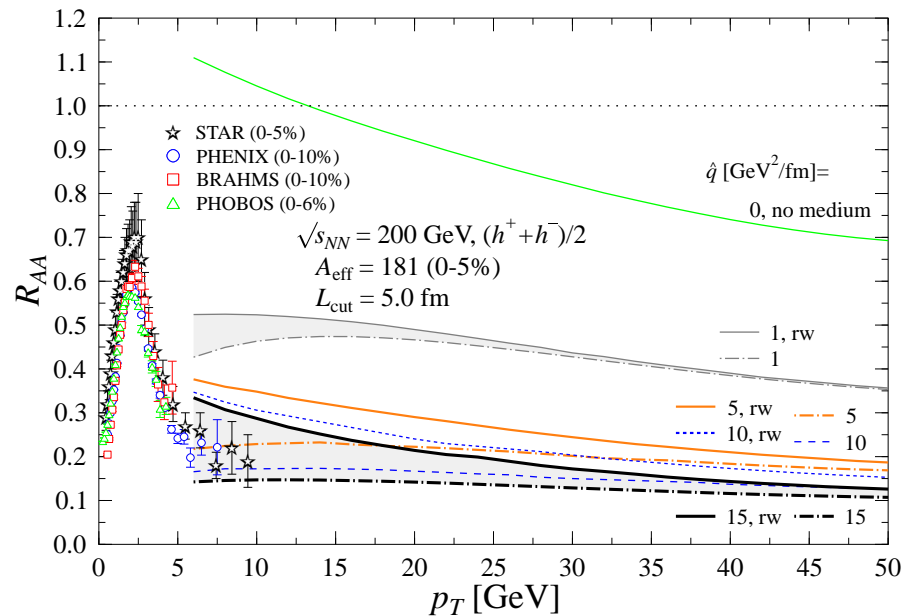


So the radiation is suppressed for

$$\sin \theta \lesssim \sqrt{\sqrt{\frac{\hat{q}}{\omega^3}}}$$

# Application of the formalism

$$d\sigma_{(\text{med})}^{AA \rightarrow h+X} = \sum_f d\sigma_{(\text{vac})}^{AA \rightarrow f+X} \otimes P_f(\Delta E, L, \hat{q}) \otimes D_{f \rightarrow h}^{(\text{vac})}(z, \mu_F^2).$$



[Eskola, Honkanen, Salgado, Wiedemann (2004)]

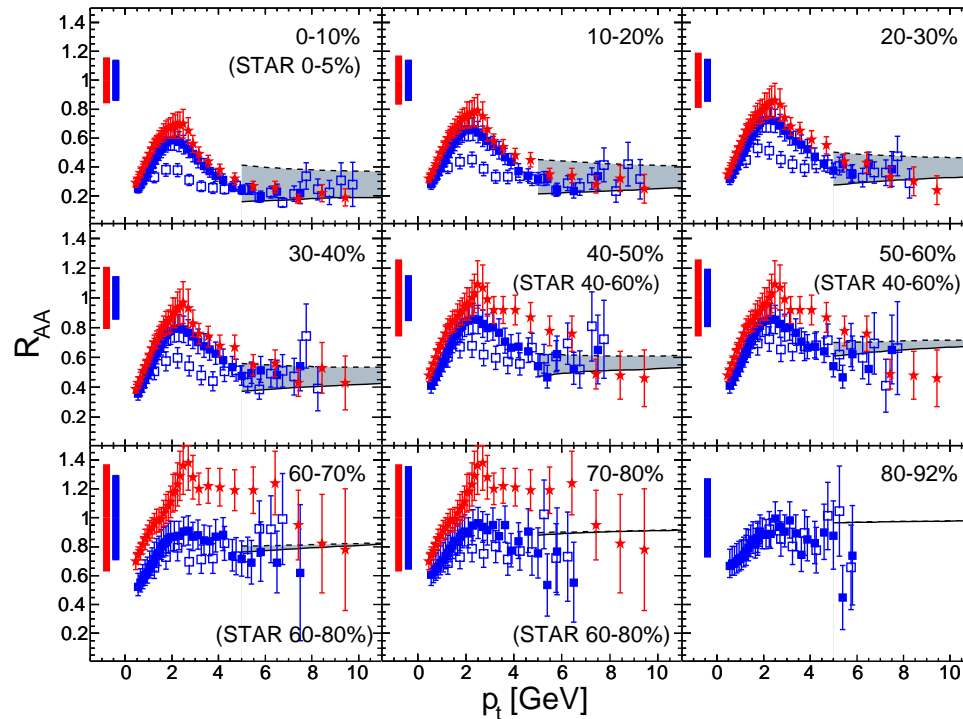
⇒ Data favors a large time-averaged transport coefficient

$$\hat{q} \sim 5 \dots 15 \frac{\text{GeV}^2}{\text{fm}}$$

[Many other groups describe these data: Gyulassy, Levai, Vitev, Wang, Drees, Feng, Jia, Arleo, Dainese, Loizides, Paic...]

# Centrality dependence

$$\hat{q} \propto \text{density}$$



[Dainese, Loizides, Paic (2005)]



# Opacity problem

⇒  $\hat{q} = c\epsilon^{3/4}$  for an ideal QGP  $c_{ideal}^{QGP} \sim 2$

⇒ We obtain [Eskola, Honkanen, Salgado, Wiedemann (2004)]

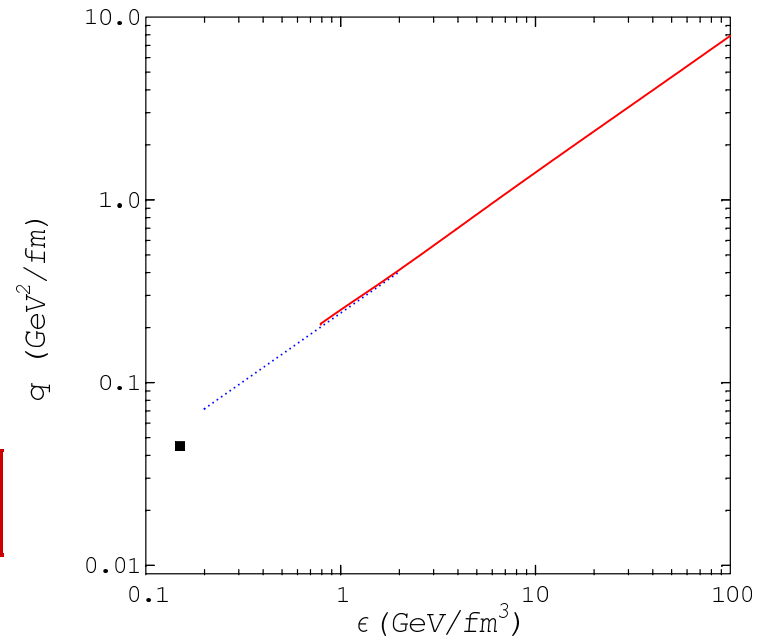
$$\bar{\hat{q}} = \frac{2}{L^2} \int_{\tau_0}^{\tau_0+L} d\tau (\tau - \tau_0) \hat{q}(\tau) \Rightarrow$$

$$c = \frac{\hat{q}}{\epsilon^{3/4}(\tau_0)} \frac{2 - \alpha}{2} \left( \frac{L}{\tau_0} \right)^\alpha \Rightarrow \boxed{c > 5c_{ideal}^{QGP}}$$

[taking  $\epsilon(\tau_0) < 100 \frac{\text{GeV}}{\text{fm}^3}$ ,  $L/\tau_0 \sim 10$ ,  $\alpha = 1$ ]

⇒ Remember  $\hat{q}$  proportional to the density  
times cross section ⇒

The interaction of the hard parton with the medium is much stronger than expected.

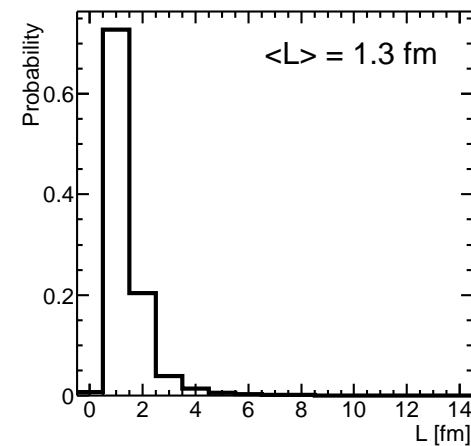
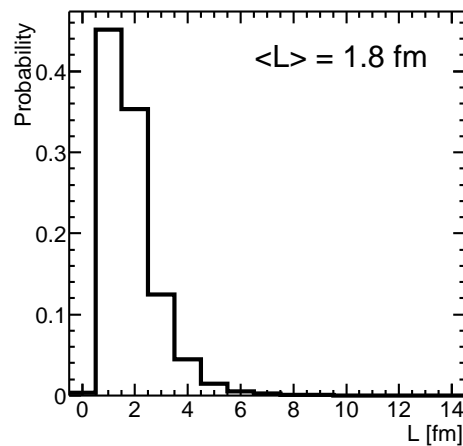
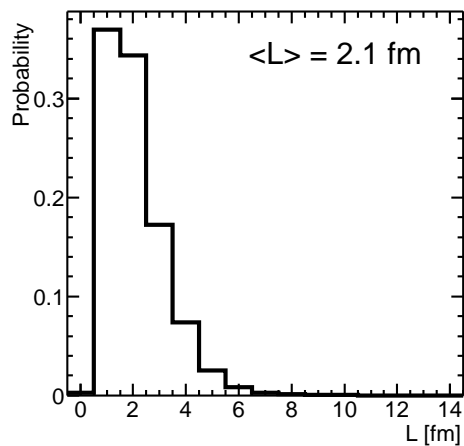
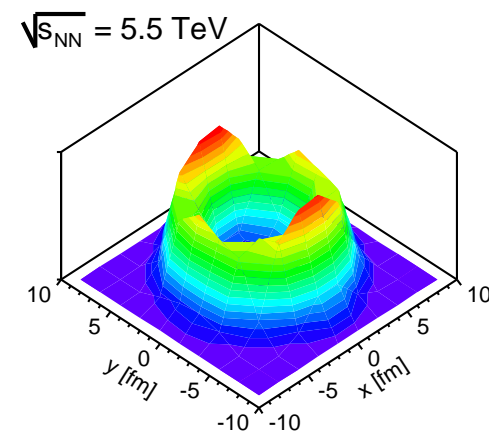
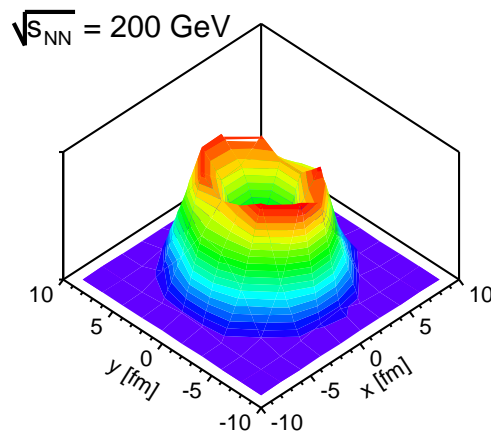
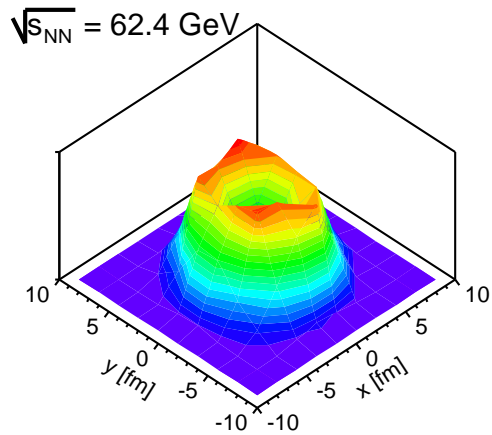


[Baier 2002]

# Corona effect

The medium produced at RHIC is so dense that only particles produced close to the surface can escape. [Muller (2003)]

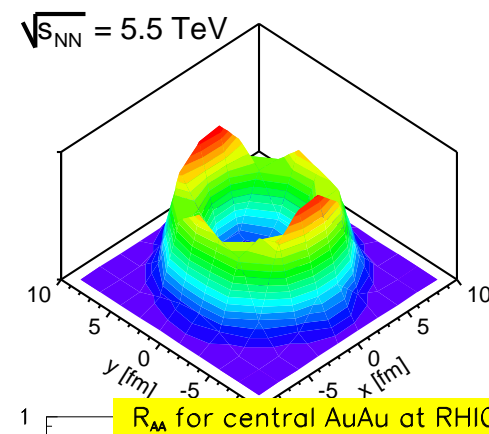
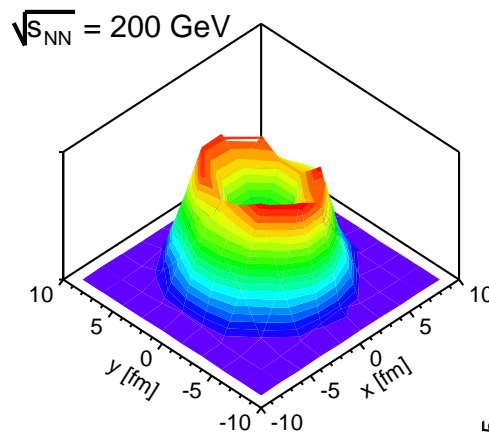
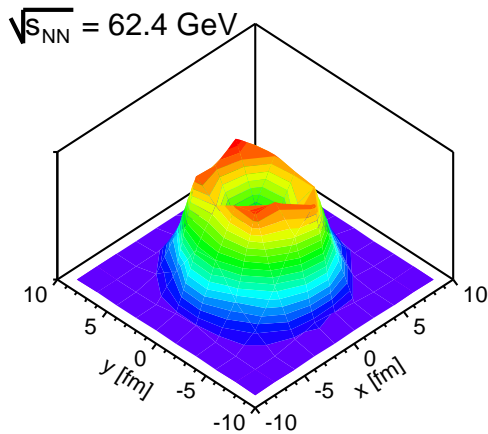
[Dainese, Loizides, Paic (2004); Eskola, Honkanen, Salgado, Wiedemann (2004)]



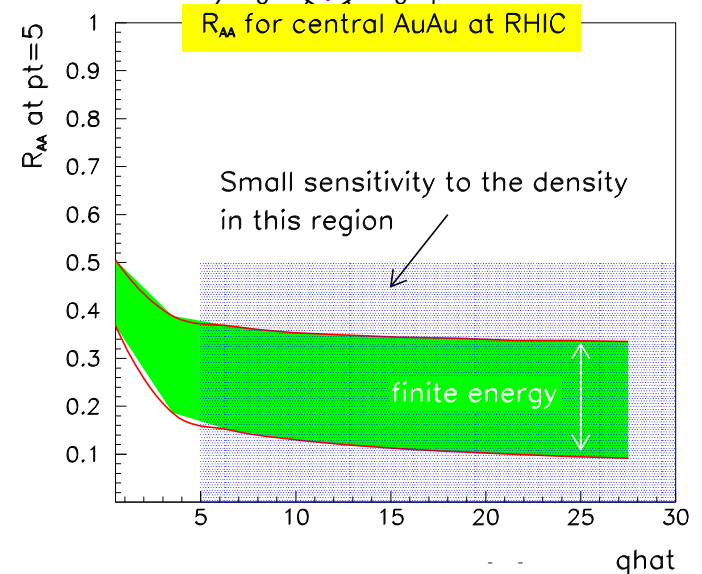
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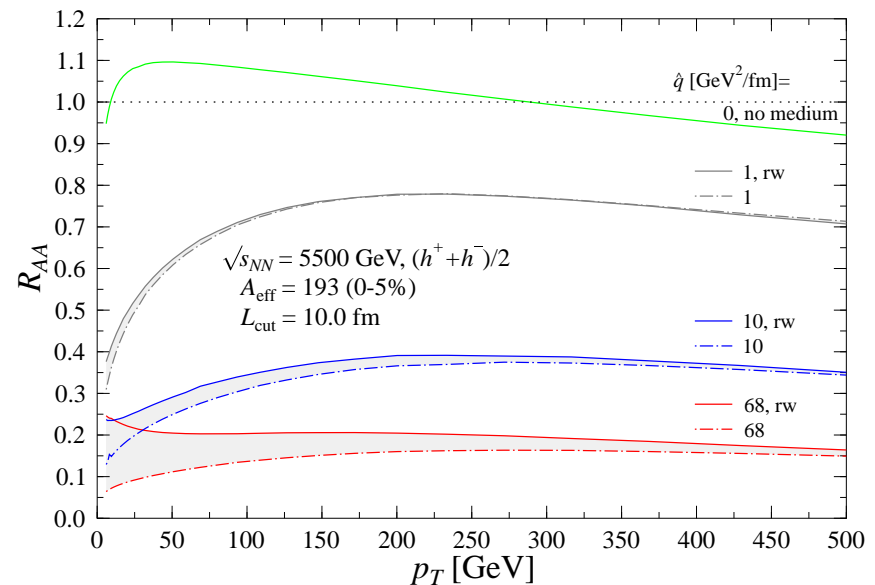
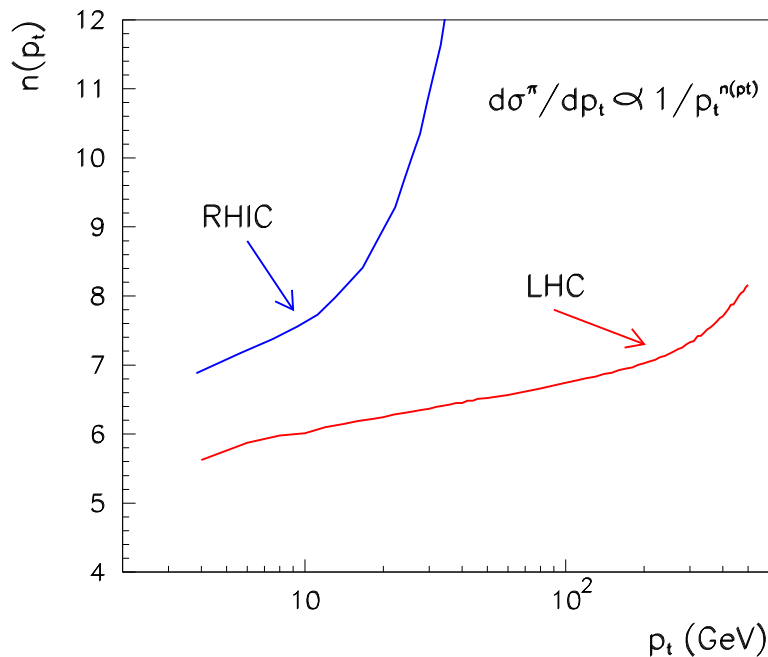
In this case, the sensitivity to  $\hat{q}$  becomes small (bad determination of the medium density)



# Flatness of the suppression

## Trigger bias

⇒ Steepness of the spectrum  $\frac{d\sigma}{dp_t} \sim \frac{1}{p_t^n} \implies$  small  $z, \epsilon$



$R_{AA}$  flat also for the LHC

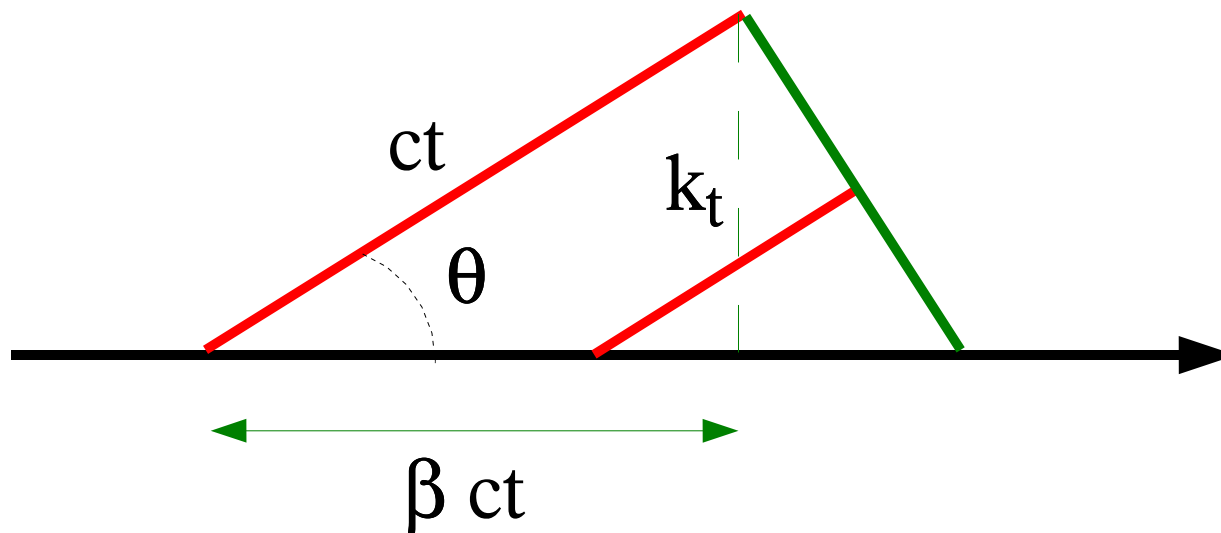
⇒ High- $p_t$  hadrons are fragile objects – more fragile the highest the  $p_t$

[Eskola, Honkanen, Salgado, Wiedemann (2004)]

# Heavy quarks

# Vacuum radiation: Dead cone effect

$$\sin^2 \theta_0 = 1 - \beta^2 = \left(\frac{m}{E}\right)^2$$

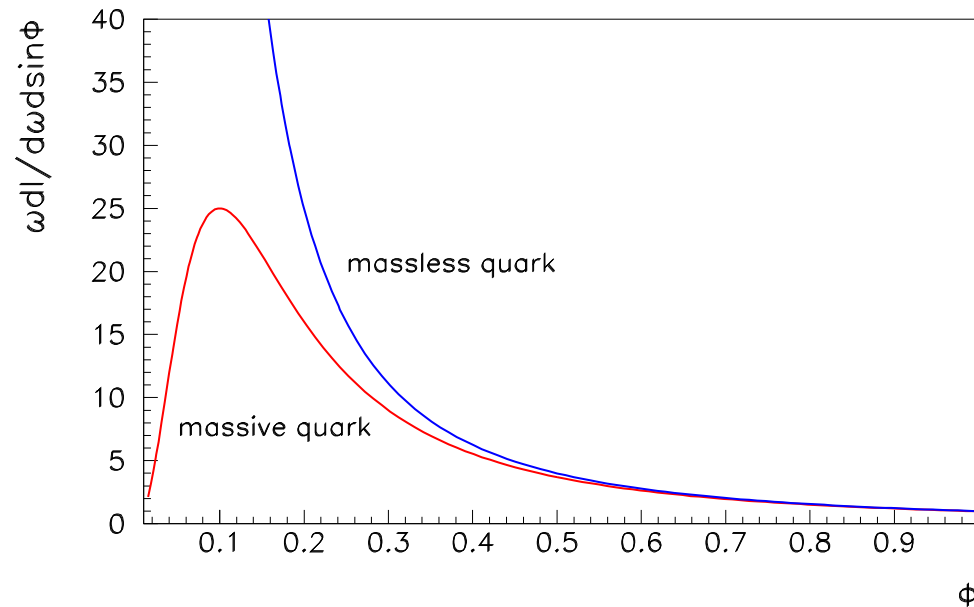


**Dead cone effect** Angles smaller than  $\theta_0 \equiv m/E$  are suppressed in vacuum radiation [Dokshitzer, Khoze, Troyan (1991)]

$$\omega \frac{dI_{\text{vac}}}{d\omega dk_t^2} \sim \frac{1}{k_t^2} \longrightarrow \omega \frac{dI_{\text{vac}}^m}{d\omega dk_t^2} \sim \frac{k_t^2}{[k_t^2 + \omega^2 \theta_0^2]^2}$$

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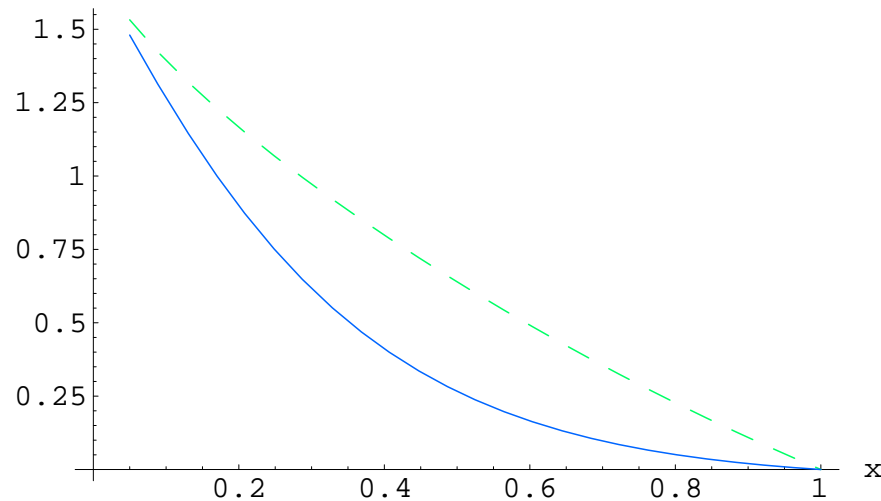
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# Heavy quark energy loss

⇒ Dokshitzer & Kharzeev 2001 took  $\theta \sim \left(\frac{\hat{q}}{\omega^3}\right)^{1/4}$

$$\omega \frac{dI_{\text{med}}^{\text{mass}}}{d\omega} = \frac{1}{\left(1 + \frac{\theta_0^2}{\theta^2}\right)^2} \omega \frac{dI_{\text{med}}^{m=0}}{d\omega}$$

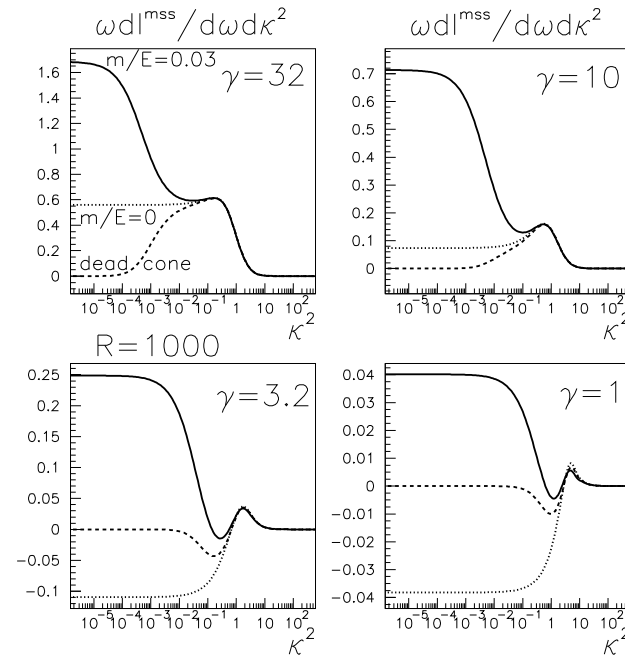


⇒ Medium-induced gluon radiation is reduced in the mass case ⇒  
less energy loss for heavy than for light quarks.



# Medium-induced gluon radiation: massive case

⇒ More refined calculations of the double differential spectrum of heavy quarks reveal a richer structure



[Armesto, Salgado, Wiedemann (2004)]

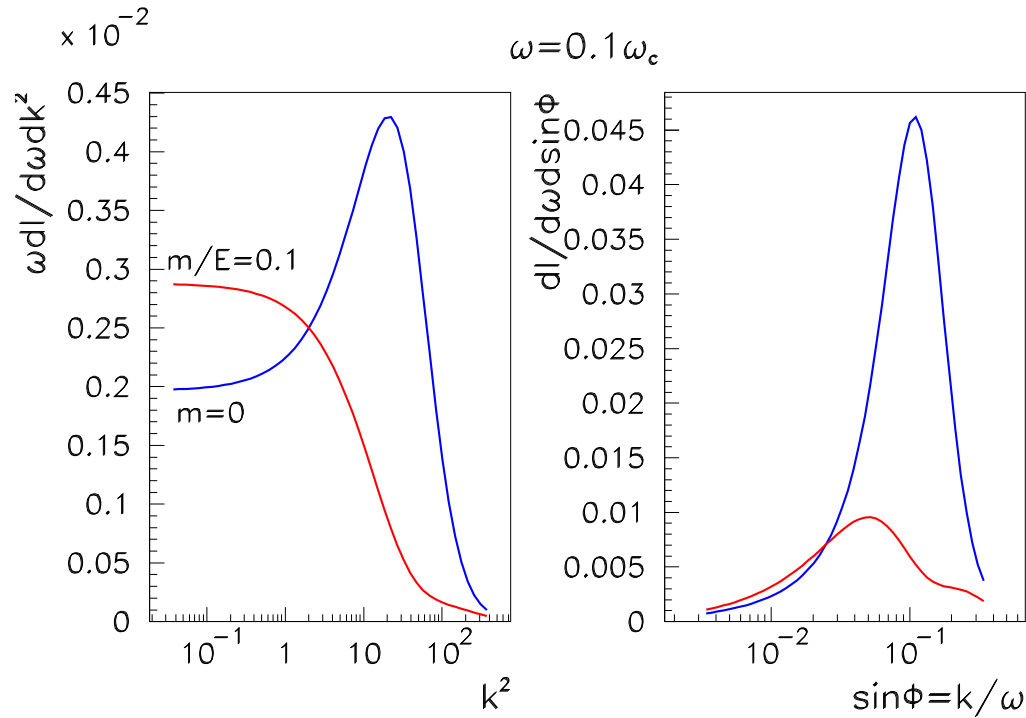
⇒ New phase term in the massive case:

$$\varphi = \left\langle \frac{k_{\perp}^2}{2\omega} \Delta z \right\rangle \longrightarrow \left\langle \frac{k_{\perp}^2}{2\omega} \Delta z + \bar{q} \Delta z \right\rangle; \quad \bar{q} \simeq \frac{x^2 M^2}{2\omega}; \quad \left[ x = \frac{\omega^2}{E^2} \right]$$

[Similar results: Djordjevic, Gyulassy (2003); Zhang, Wang, Wang (2004)]

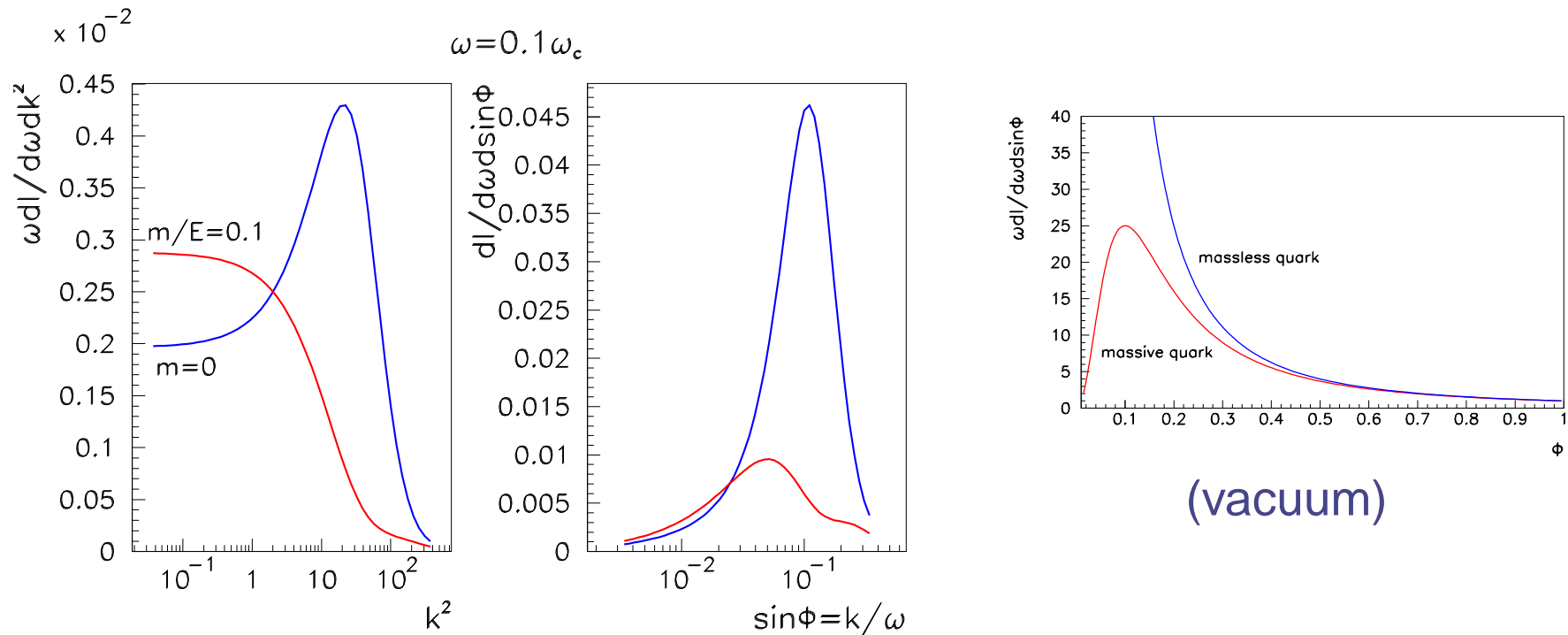
# Angular distribution

⇒ The angular distribution is modified



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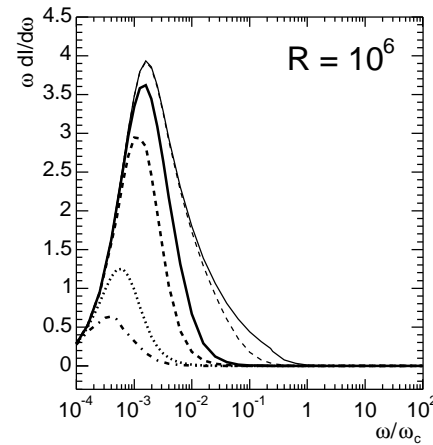
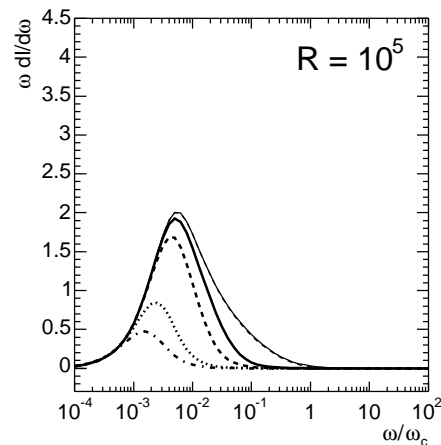
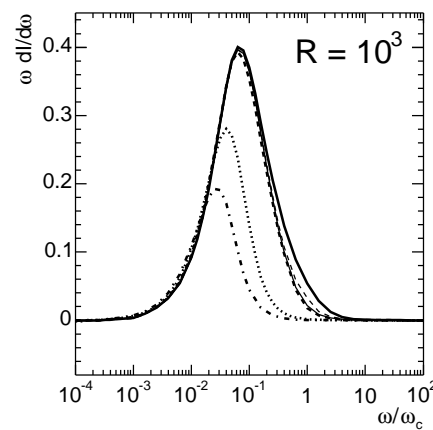
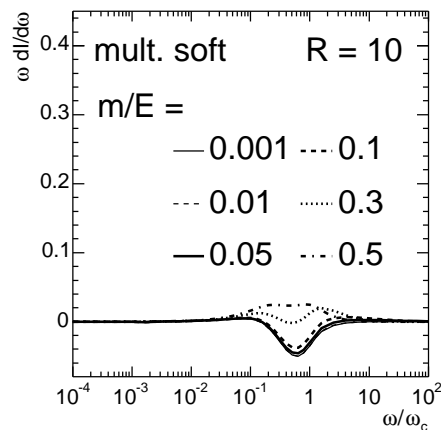


⇒ The effect of the mass in the medium case is

- Suppress radiation at large angle
- Enhance (moderately) at small angle

⇒ Net effect: **the energy loss is smaller in the massive case**

# Energy spectrum for different masses



$$R \equiv \omega_c L$$

Notice that the effect of the mass increases with the length  $L$

# Practical applications

# Formalism

$$d\sigma_{(\text{med})}^{AA \rightarrow h+X} =$$

$$d\sigma_{(\text{vac})}^{AA \rightarrow f+X} \otimes P\left(\frac{\Delta E}{\omega_c}, R, \frac{m}{E}\right) \otimes D_{f \rightarrow h}^{(\text{vac})}$$

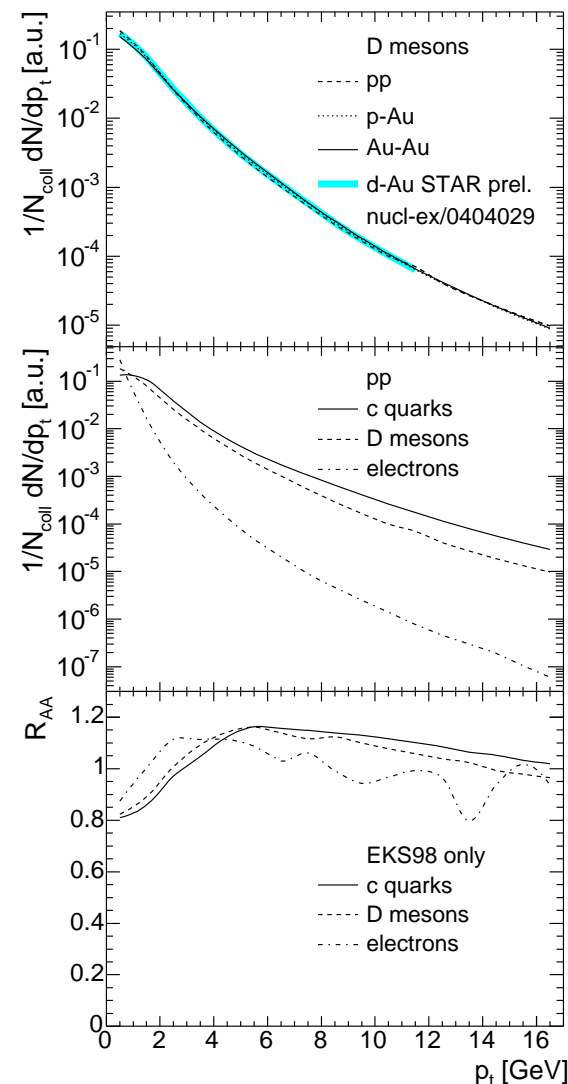
⇒  $P\left(\frac{\Delta E}{\omega_c}, R, \frac{m}{E}\right)$  probability of losing  $\Delta E$  due to medium-induced radiation ( $R = \omega_c L$ )

⇒ In the vacuum

$$P\left(\frac{\Delta E}{\omega_c}, R, \frac{m}{E}\right) = \delta(\Delta E)$$

⇒ We tuned PYTHIA to reproduce the shape of the data from STAR on the  $D$  meson  $p_t$  distribution in dAu.

[Armesto, Dainese, Salgado, Wiedemann (2005); Same method as in Dainese, Loizides, Paic (2004)]

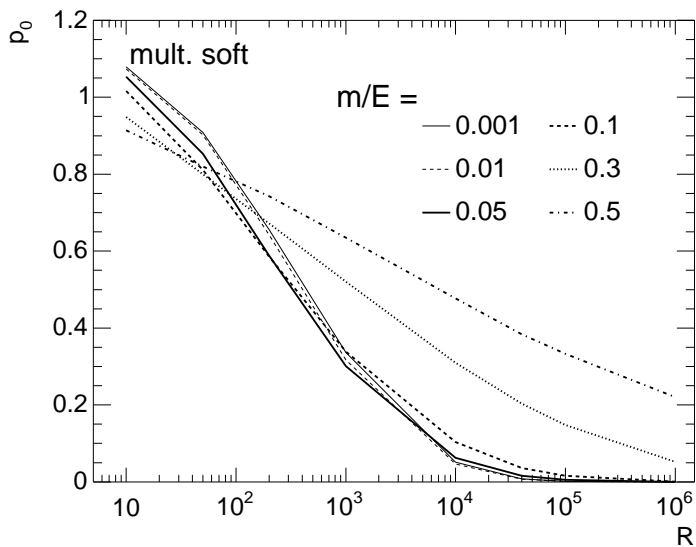


# Quenching weights

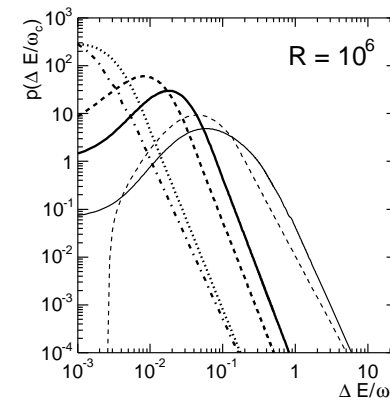
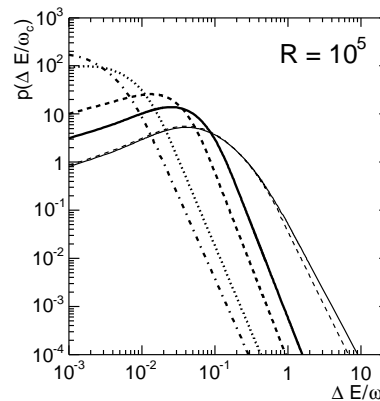
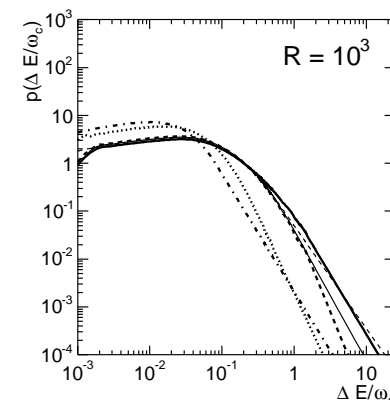
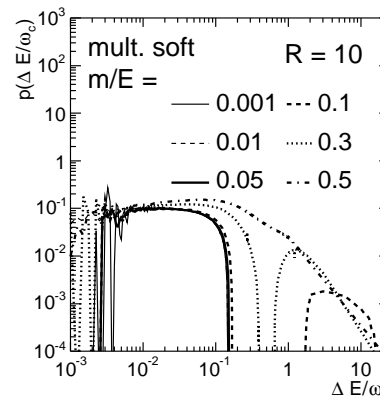
⇒ In the independent gluon emission approximation [Baier *et al* (2001)]

$$P\left(\frac{\Delta E}{\omega_c}, R, \frac{m}{E}\right) = \sum_{n=0}^{\infty} \frac{1}{n!} \left[ \prod_{i=1}^n \int d\omega_i \frac{dI^{\text{med}}(\omega_i)}{d\omega} \right] \delta\left(\Delta E - \sum_{i=1}^n \omega_i\right) \exp\left[-\int d\omega \frac{dI^{\text{med}}}{d\omega}\right]$$

probability of no-energy loss

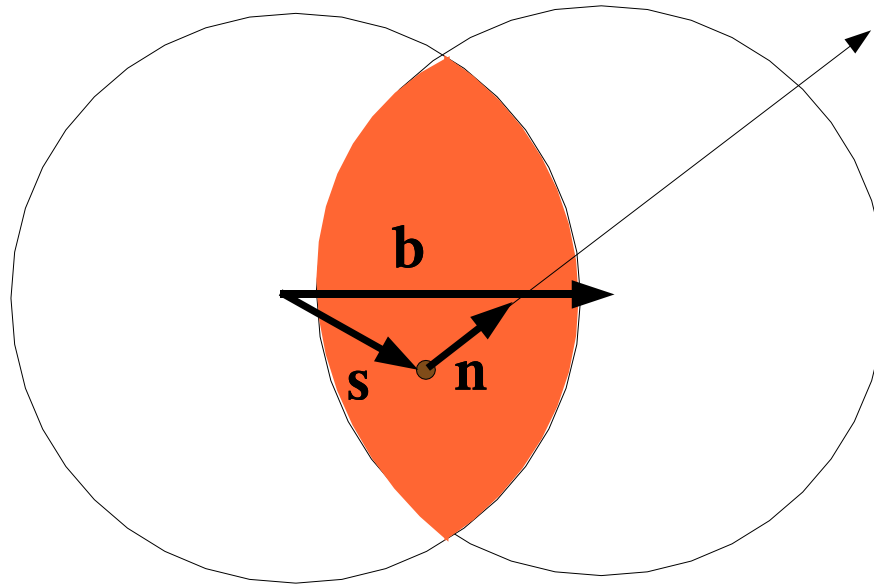


$$R \equiv \omega_c L$$



[Armesto, Dainese, Salgado, Wiedemann (2005)]

[tabulated in: <http://www.pd.infn.it/~dainesea/qwmassive.html>]



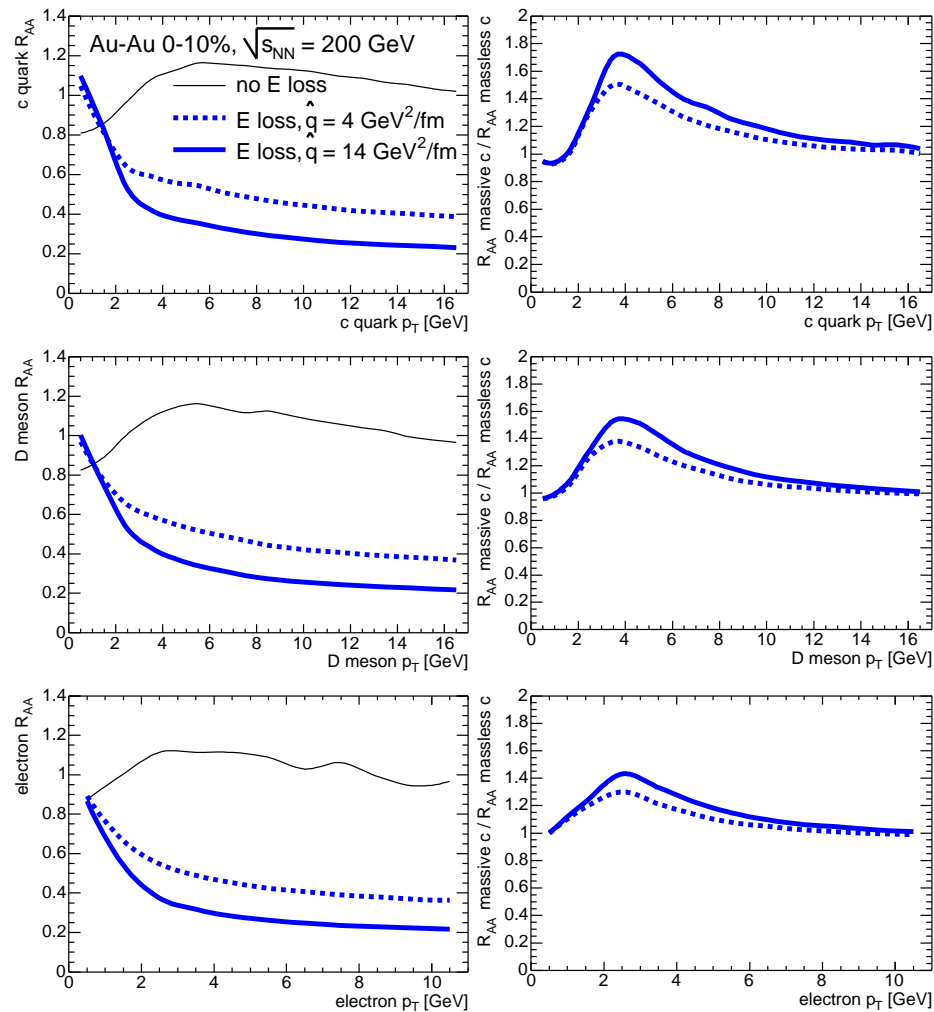
$$\hat{q}(\xi) = kT_A(\mathbf{s} + \xi\mathbf{n})T_B(\mathbf{b} - [\mathbf{s} + \xi\mathbf{n}])$$

$$\omega_c = \int_0^\infty d\xi \xi \hat{q}(\xi) ; \quad R = \frac{2\omega_c^2}{\int_0^\infty d\xi \hat{q}(\xi)}$$

[Dainese, Loizides, Paic (2004); Armesto, Dainese, Salgado, Wiedemann (2005)]



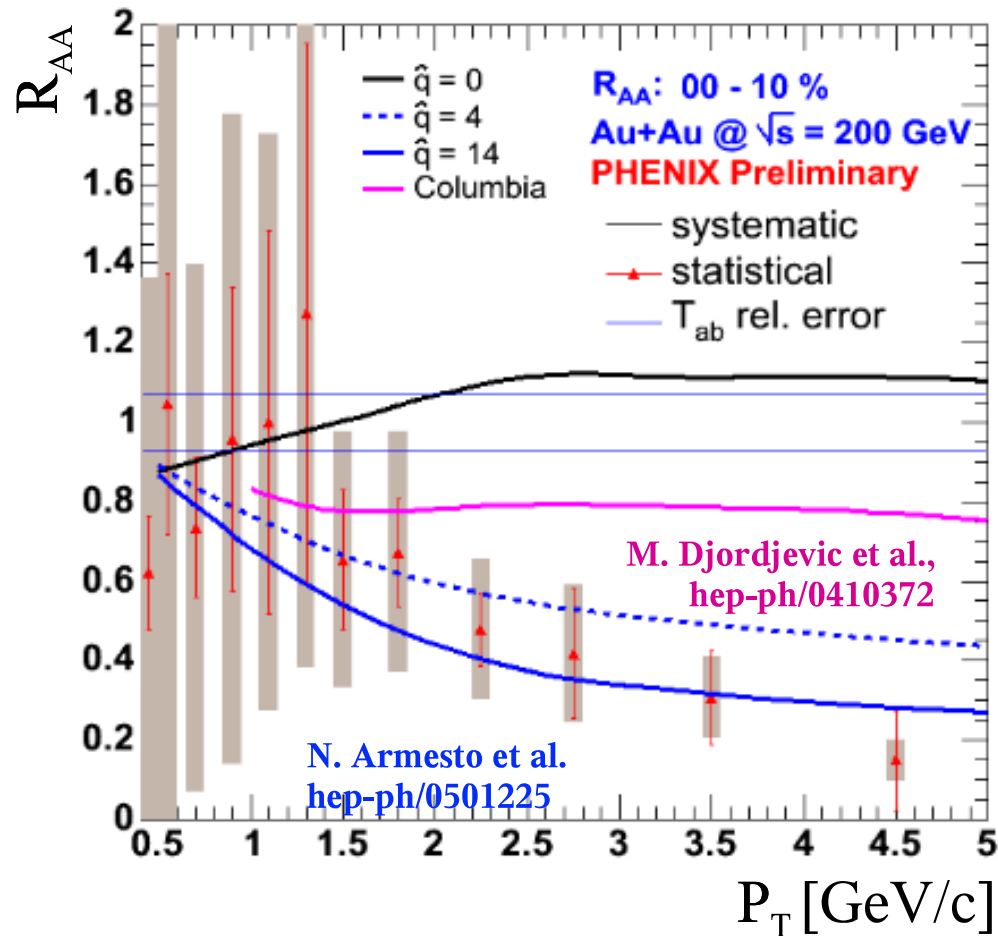
# Results for RHIC



[Armesto, Dainese, Salgado, Wiedemann (2005)]

# Comparison with preliminary data

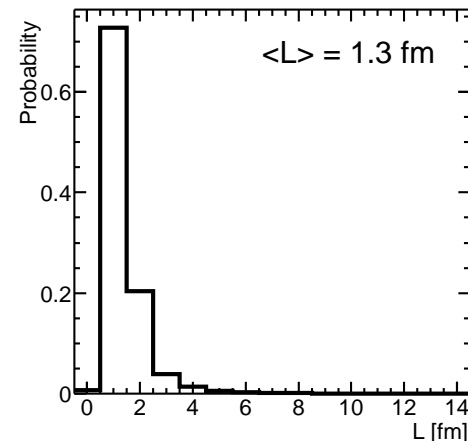
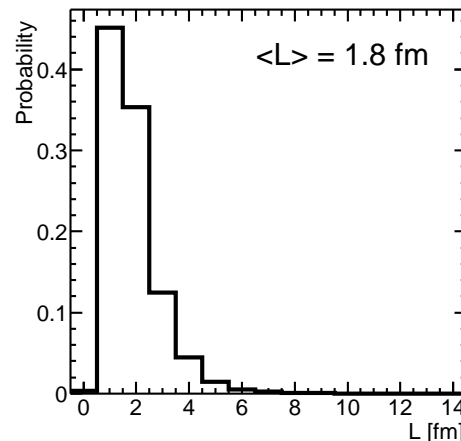
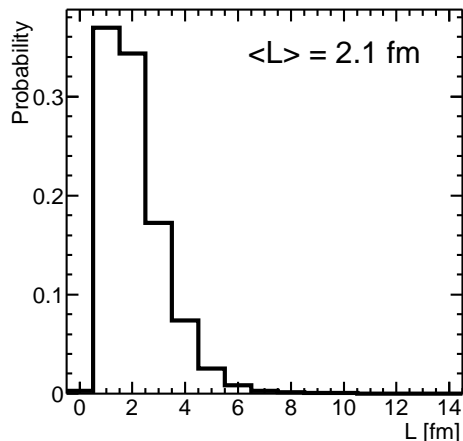
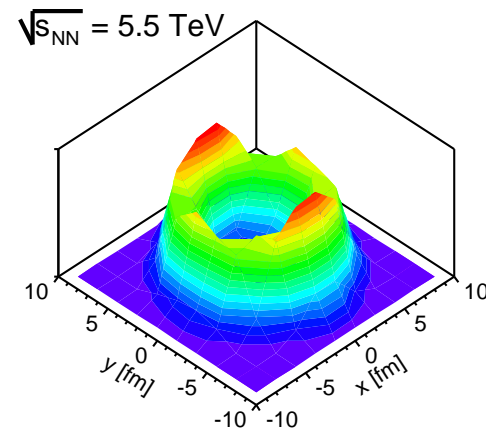
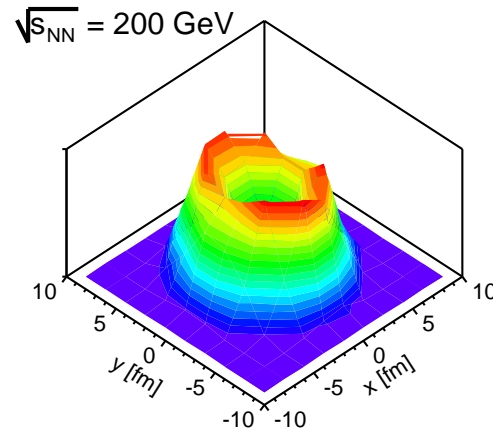
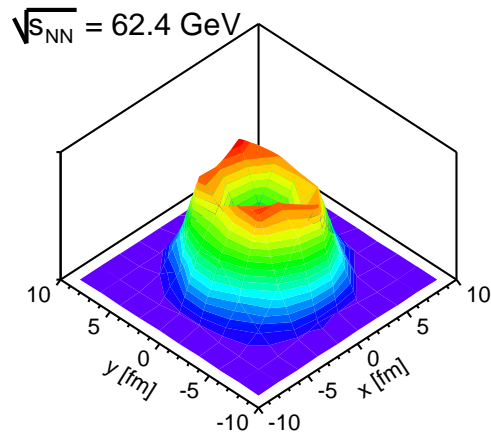
## PHENIX: Averbeck, Moriond '05



Almost the same suppression as for light quarks

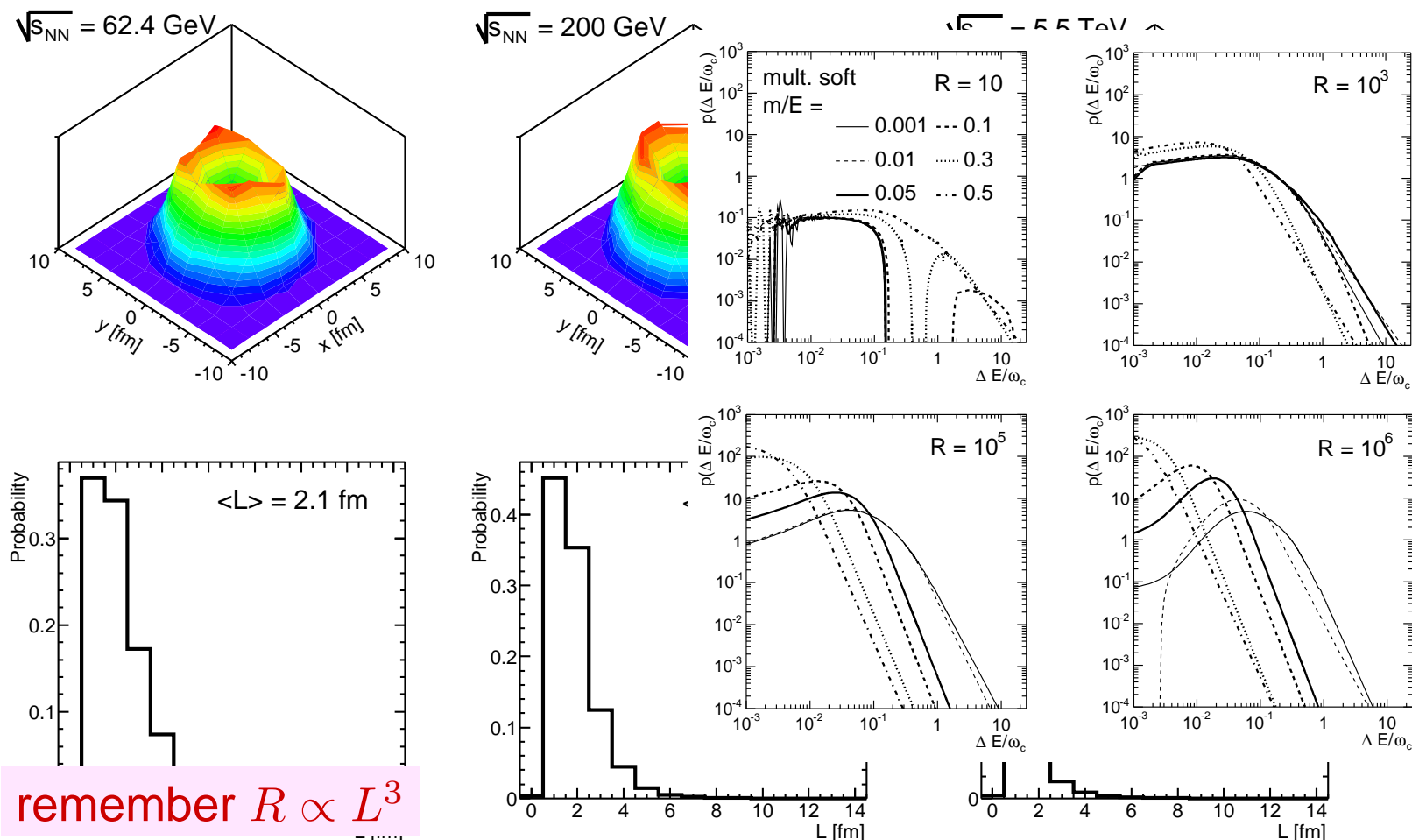
# Surface emission with mass terms

- ⇒ Suppression for charm and light quarks very similar **unexpected?**
- ⇒ Remember that mass effects small for small lengths

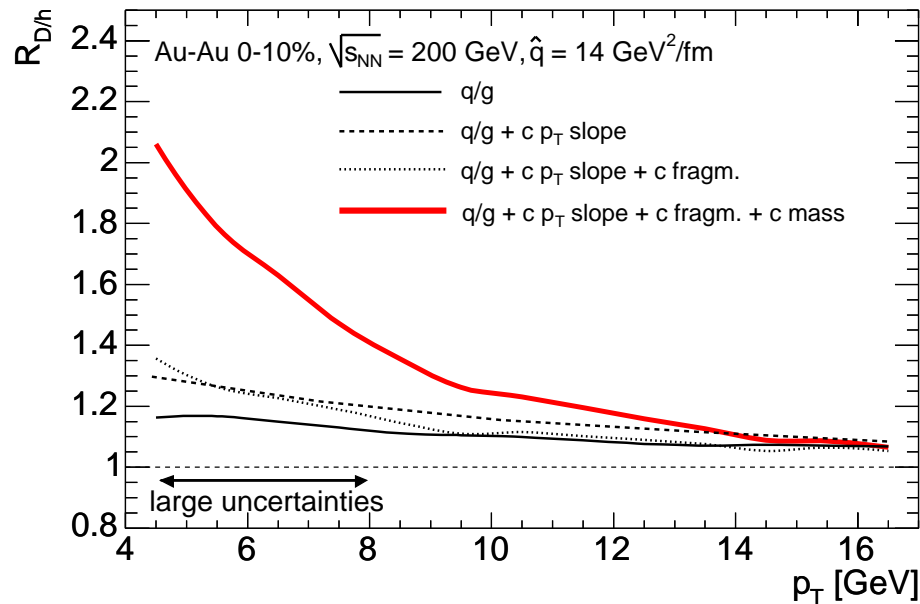


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# Massive over light particle ratio



[Armesto, Dainese, Salgado, Wiedemann 2005]

⇒ Quark vs gluon energy loss:

$$\Delta E^g = N_C / C_F \Delta E^{q, m=0}$$

↘ Increases  $R_{D/h}$

⇒ Light-particle spectrum slope larger than massive one

↘ Increases  $R_{D/h}$

⇒ charm fragmentation harder

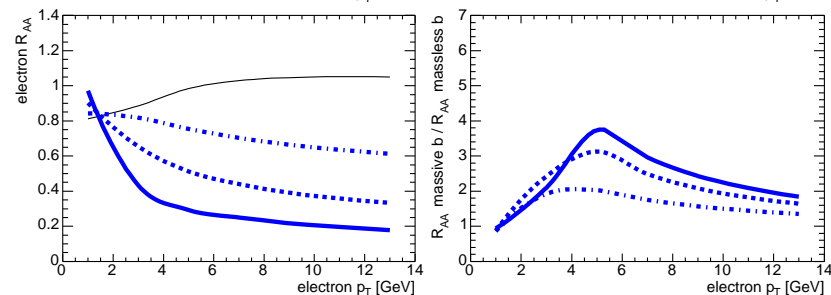
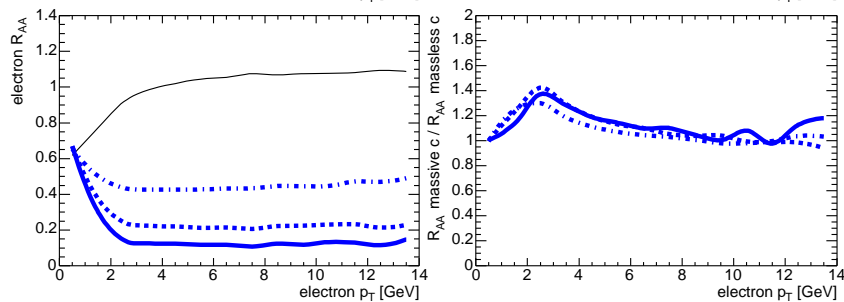
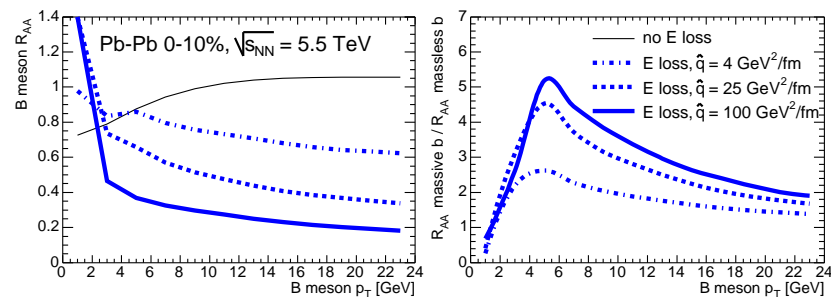
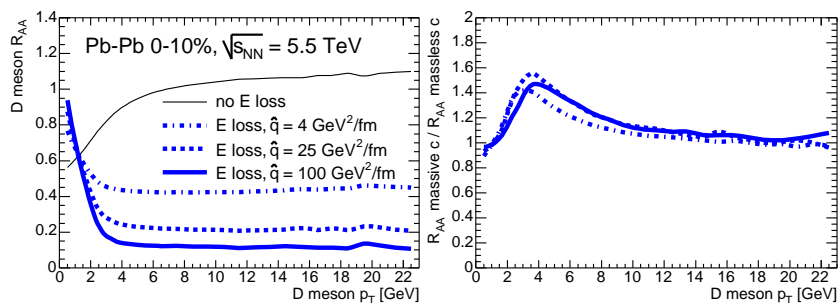
↘ Decreases  $R_{D/h}$

⇒ Heavy quark suppression of gluon radiation ('dead-cone')

↘ Increases  $R_{D/h}$

# Extrapolations to the LHC

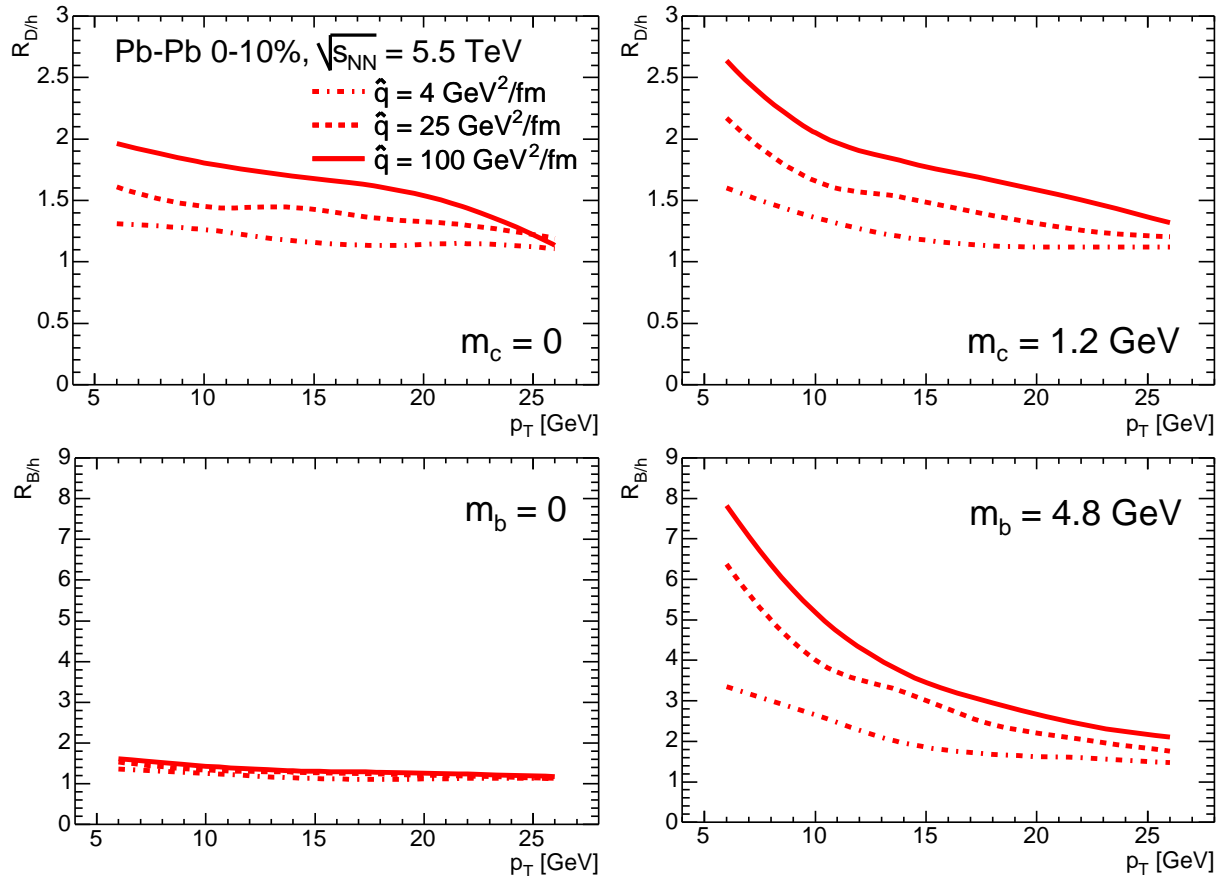
- ⇒ Extrapolation according to the expected density ( $\hat{q} \propto$  density)
- ⇒ We take a factor 7 from Eskola *et al* (2000) [probably too large]



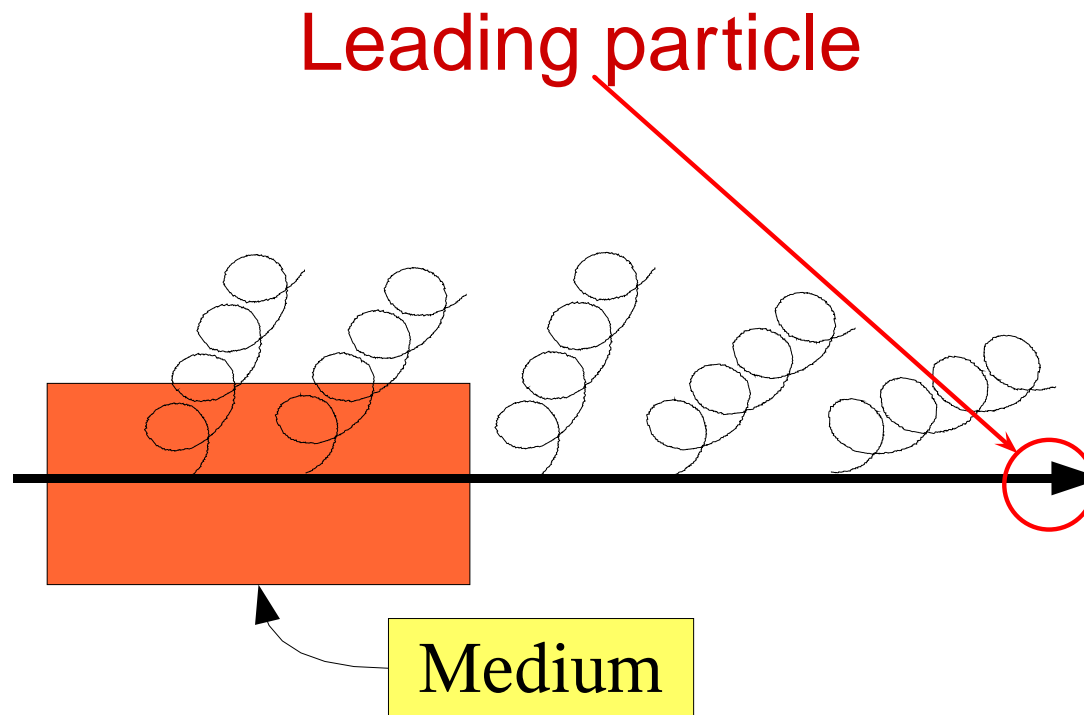
[Armesto, Dainese, Salgado, Wiedemann (2005)]

# Heavy-to-light ratios at the LHC

⇒  $D/h$  and  $B/h$  ratios for the LHC



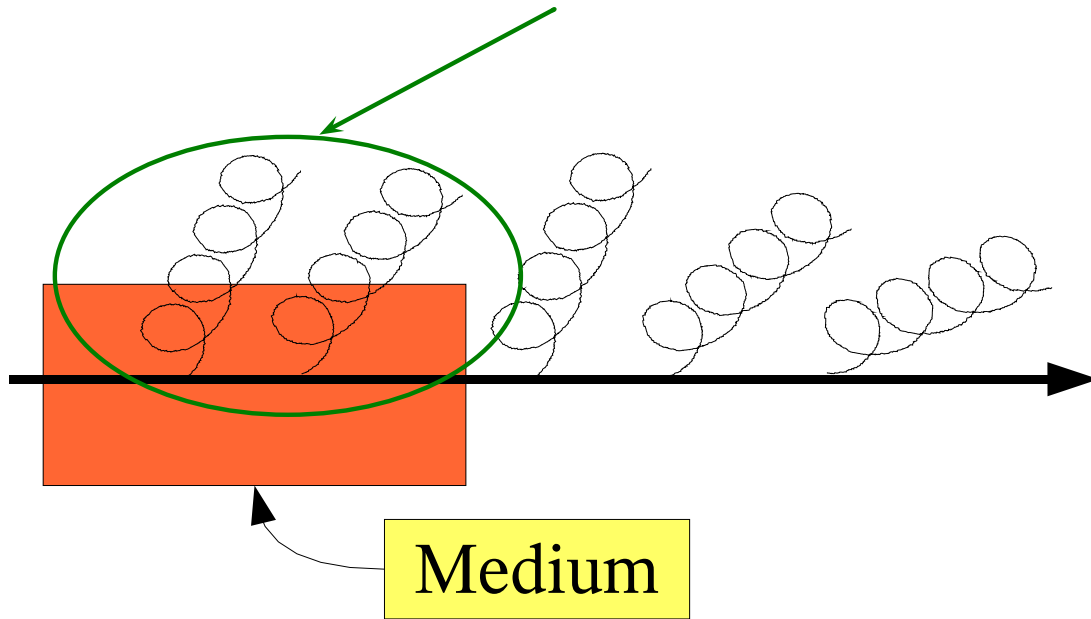
[Armesto, Dainese, Salgado, Wiedemann (2005)]



⇒ Inclusive particle measures the density of the medium:  $\Delta E \propto \alpha_S \hat{q} L^2$



Can we measure this??

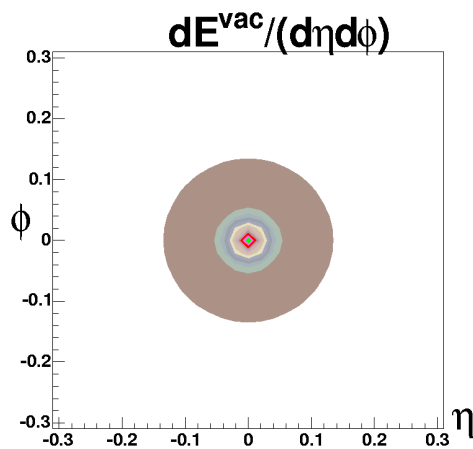


⇒ Inclusive particle measures the density of the medium:  $\Delta E \propto \alpha_S \hat{q} L^2$

⇒ The jet broadening  $\langle k_t^2 \rangle \sim \hat{q} L$

# Jet shapes in the $\eta \times \phi$ plane.

Vacuum  
(reference)

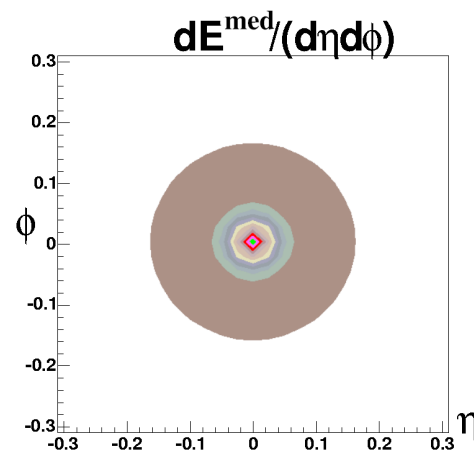
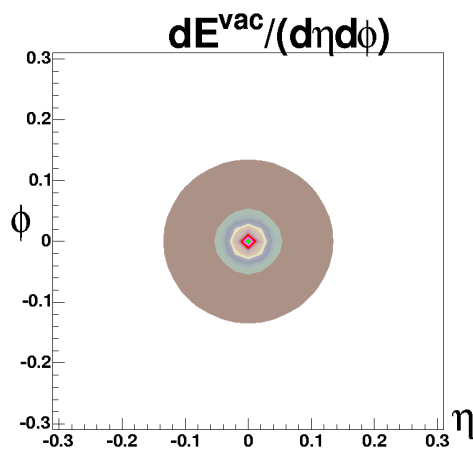
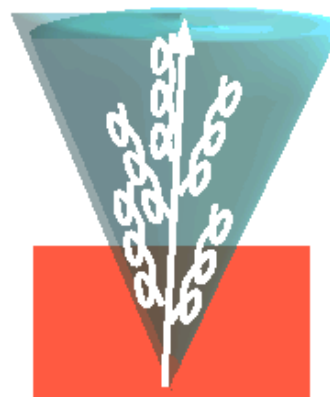


# Jet shapes in the $\eta \times \phi$ plane.

Vacuum  
(reference)



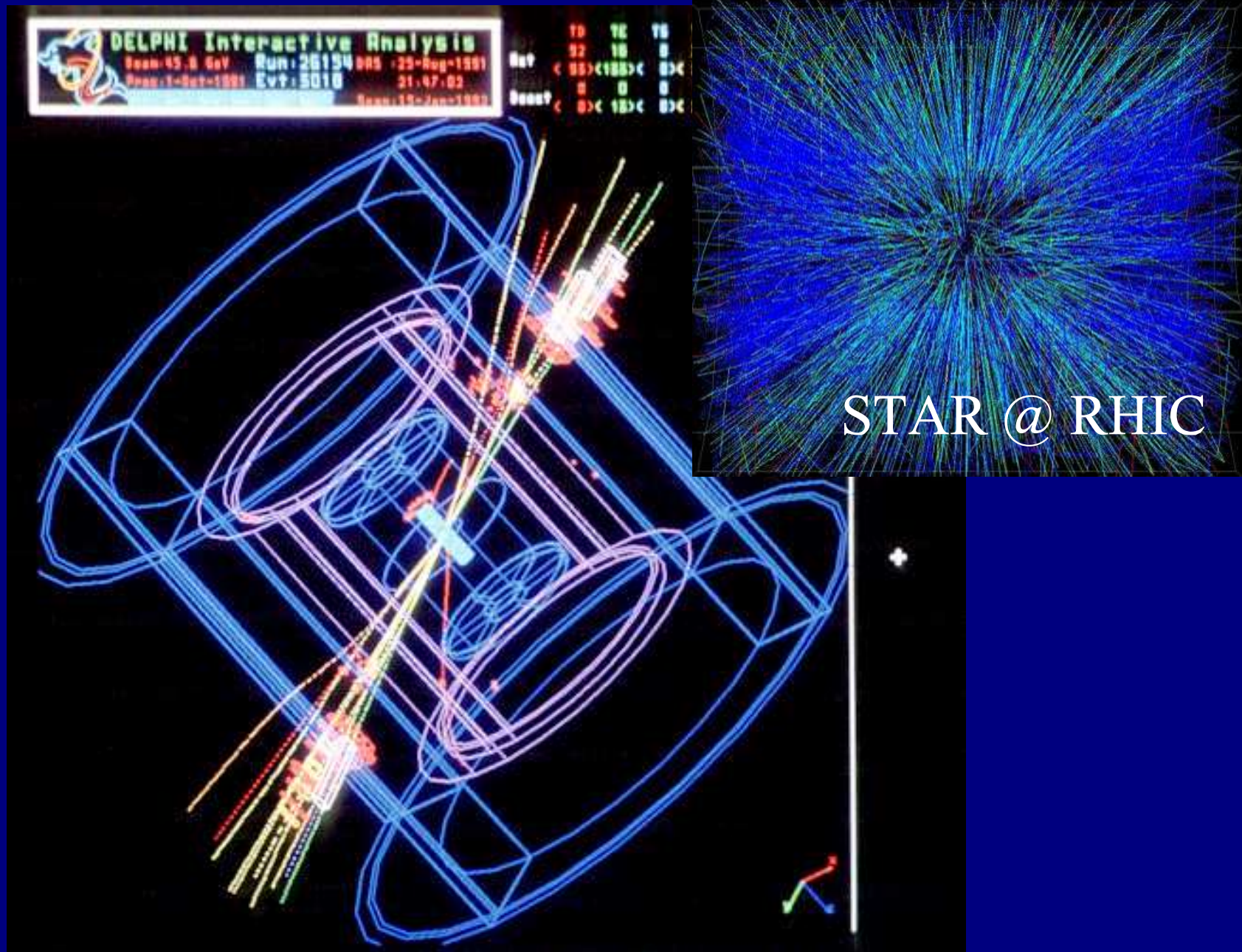
Medium:  
broadening



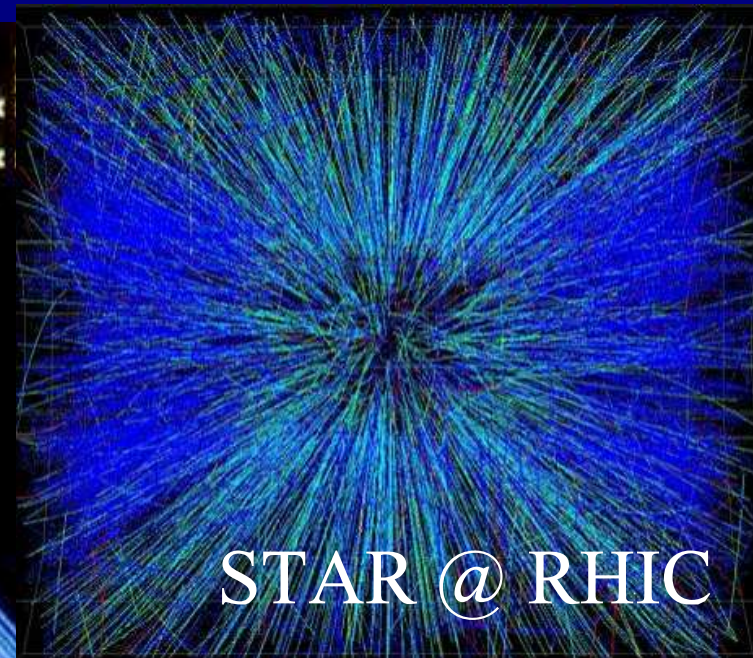
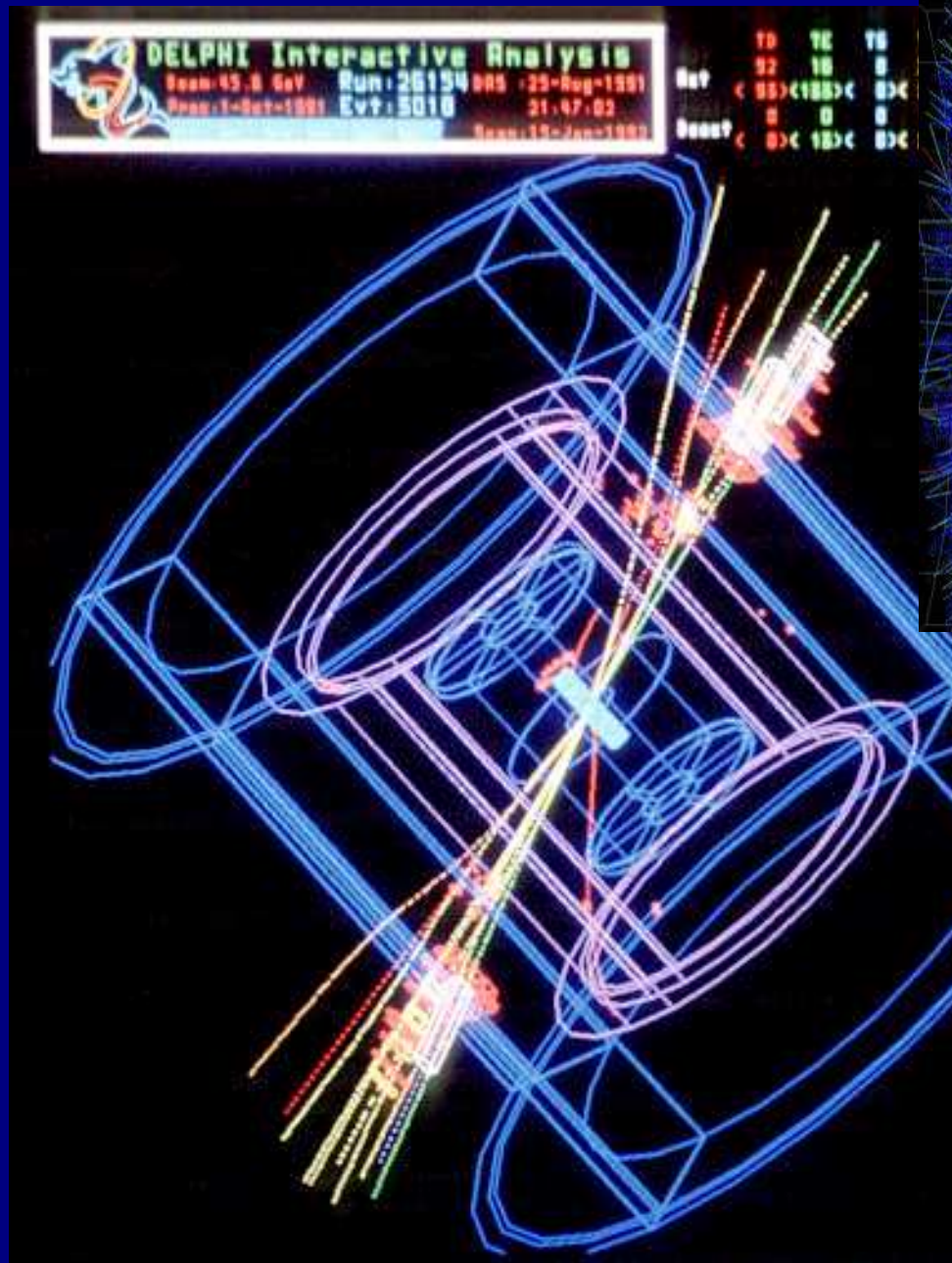
# Jets in HIC???



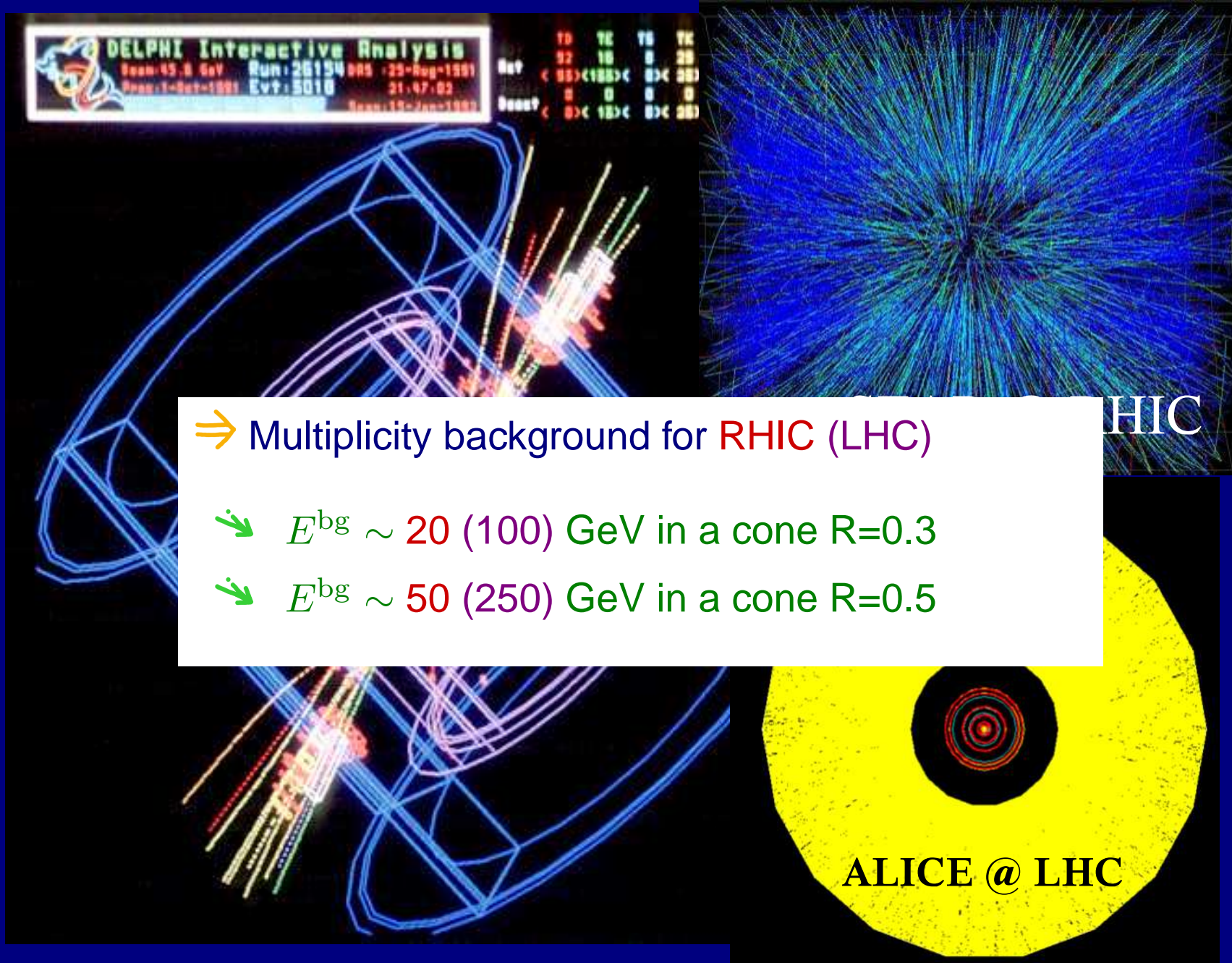
# Jets in HIC???



# Jets in HIC???



# Jets in HIC???



# Jet shapes

$\rho(R)$ , fraction of the jet energy inside a cone  $R = \sqrt{\Delta\eta^2 + \Delta\phi^2}$

$$\rho_{\text{vac}}(R) = \frac{1}{N_{\text{jets}}} \sum_{\text{jets}} \frac{E_t(R)}{E_t(R=1)}$$

$$\rho_{\text{med}} = \rho_{\text{vac}} - \frac{\Delta E_t(R)}{E_t(R=1)} + \frac{\Delta E}{E_t} (1 - \rho_{\text{vac}}(R))$$

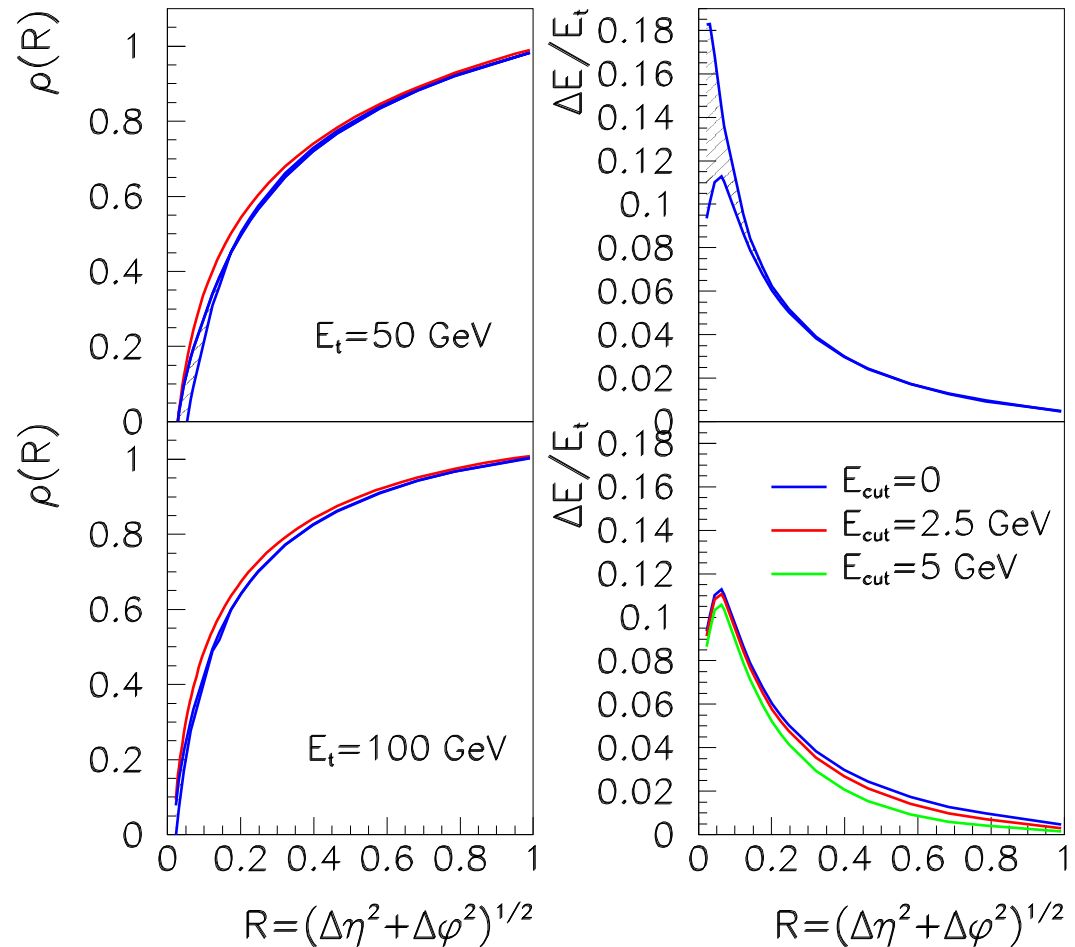
Small modification  $\rightarrow$  can jet energy be determined experimentally above background??

Scaling with number of collisions for large cone angle.

Small sensitivity to IR cuts

[Salgado, Wiedemann (2003)]

Journées RHIC–France, Etretat, Juin 2005



Vacuum D0 data: Fermilab-PUB-97/242-E



# Gluon multiplicity inside the jet.

The characteristic angular distribution of the medium-induced gluon radiation could be better observed in the quantity

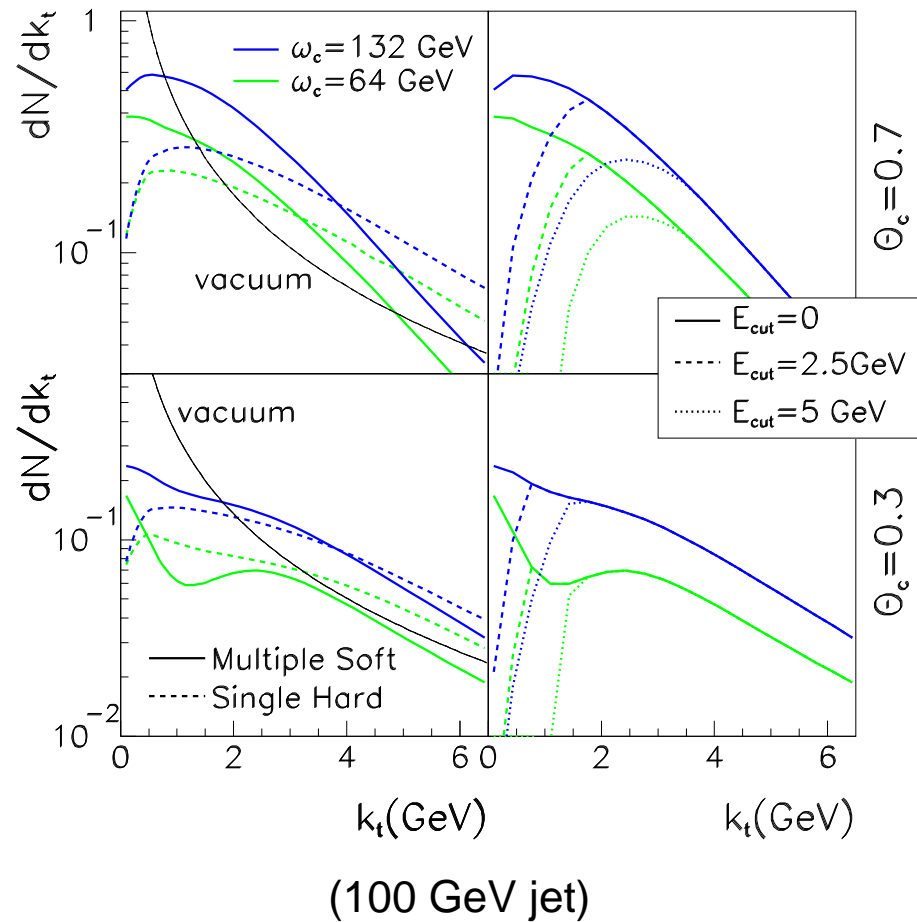
$$\frac{dN^{\text{jet}}}{dk_{\perp}} = \int_{k_{\perp}/\sin\theta_c}^E d\omega \frac{dI}{d\omega dk_{\perp}}$$

For the vacuum we simply use

$$\frac{dI_{\text{vac}}}{d\omega dk_{\perp}} \sim \frac{1}{\omega} \frac{1}{k_{\perp}}$$

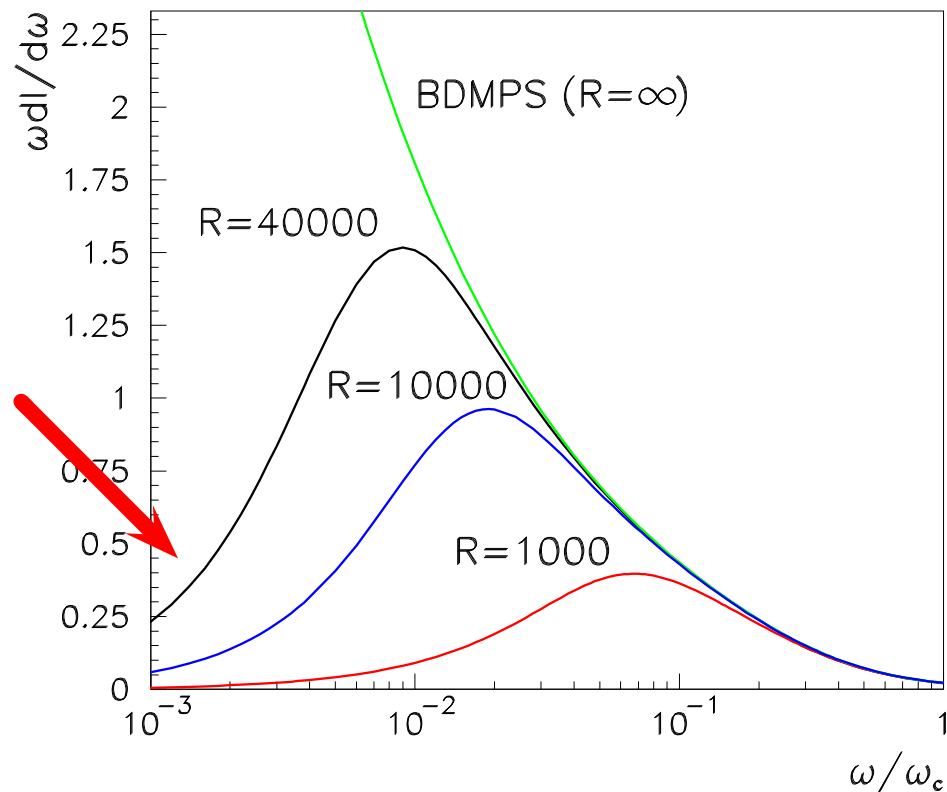
Needs a more quantitative analysis (hadronization...).

But, effect based mainly on kinematics  
remember  $k_t^2 \sim \hat{q}L (\sim Q_{\text{sat}}^2)$



# IR cuts

⇒ The fact that the results show small sensitivity to IR cuts is due to the shape of the spectrum



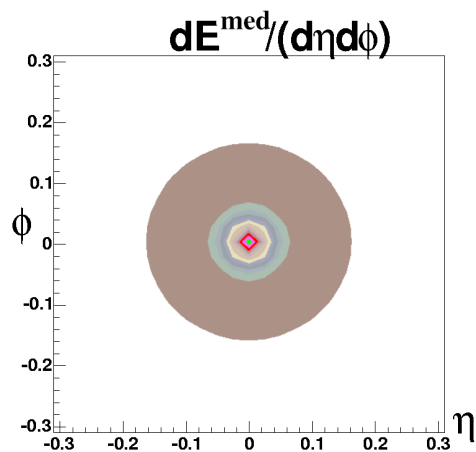
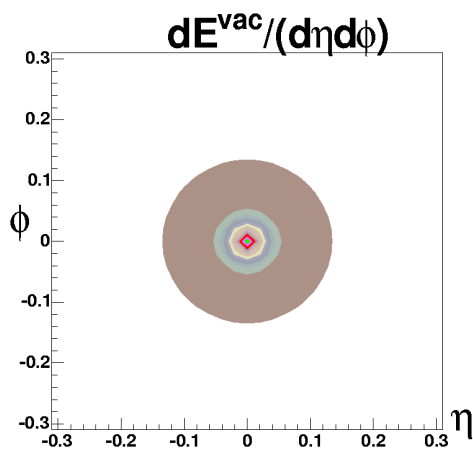
⇒ As we have seen, this is due to formation time effects.

# Jet shapes in a flowing medium

Vacuum  
(reference)



Medium:  
broadening



# Jet shapes in a flowing medium

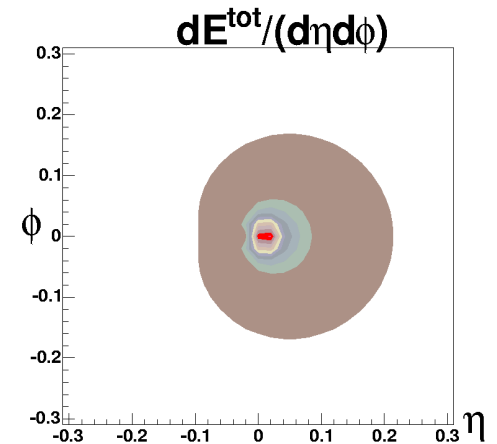
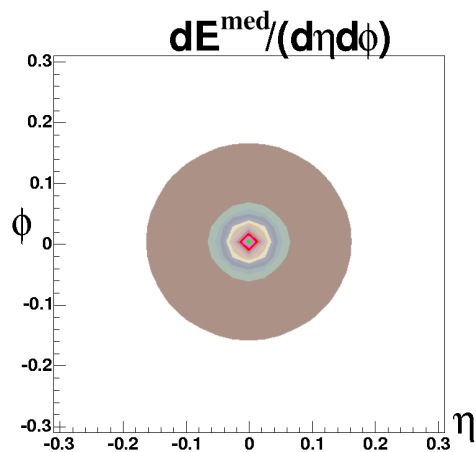
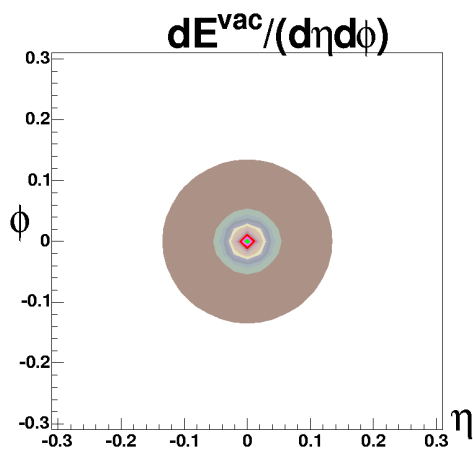
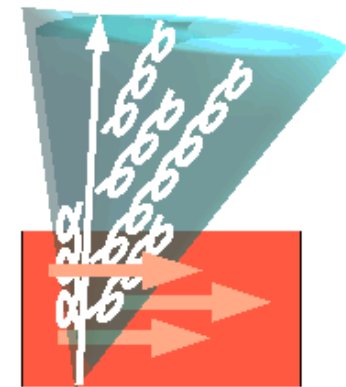
Vacuum  
(reference)



Medium:  
broadening



Flowing medium:  
anisotropic shape



# Formalism

In the single-hard scattering approximation

$$\omega \frac{dI^{\text{med}}}{d\omega d\mathbf{k}} = \frac{\alpha_s}{(2\pi)^2} \frac{4 C_R n_0}{\omega} \int d\mathbf{q} |a(\mathbf{q})|^2 \frac{\mathbf{k} \cdot \mathbf{q}}{\mathbf{k}^2} \frac{-L \frac{(\mathbf{k}+\mathbf{q})^2}{2\omega} + \sin \left( L \frac{(\mathbf{k}+\mathbf{q})^2}{2\omega} \right)}{[(\mathbf{k} + \mathbf{q})^2 / 2\omega]^2},$$

we shift the Yukawa potential by a 3-momentum  $q_0 = (\mathbf{q}_0, q_l)$  proportional to the flow field.

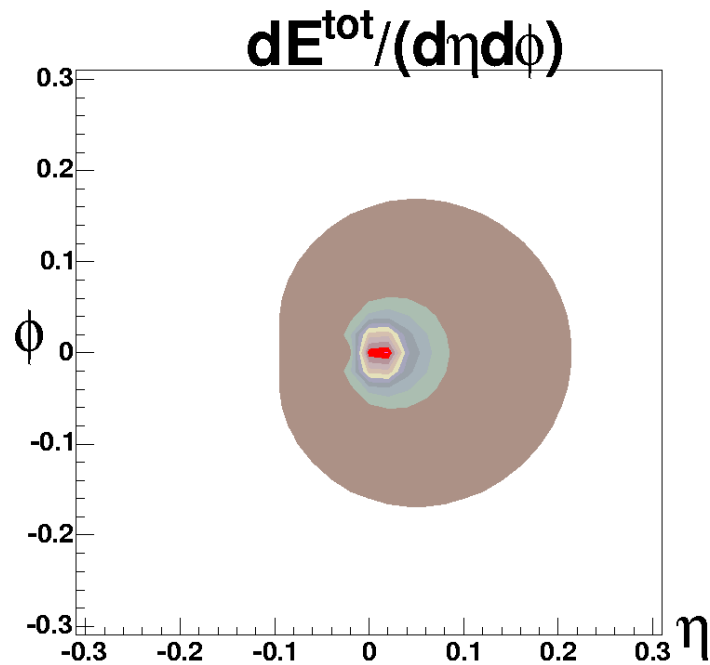
(Armesto, Salgado, Wiedemann hep-ph/0405301)

$$|a(\mathbf{q})|^2 = \frac{\mu^2}{\pi [\mathbf{q}^2 + \mu^2]^2} \longrightarrow \frac{\mu^2}{\pi [(\mathbf{q} - \mathbf{q}_0)^2 + \mu^2]^2}.$$

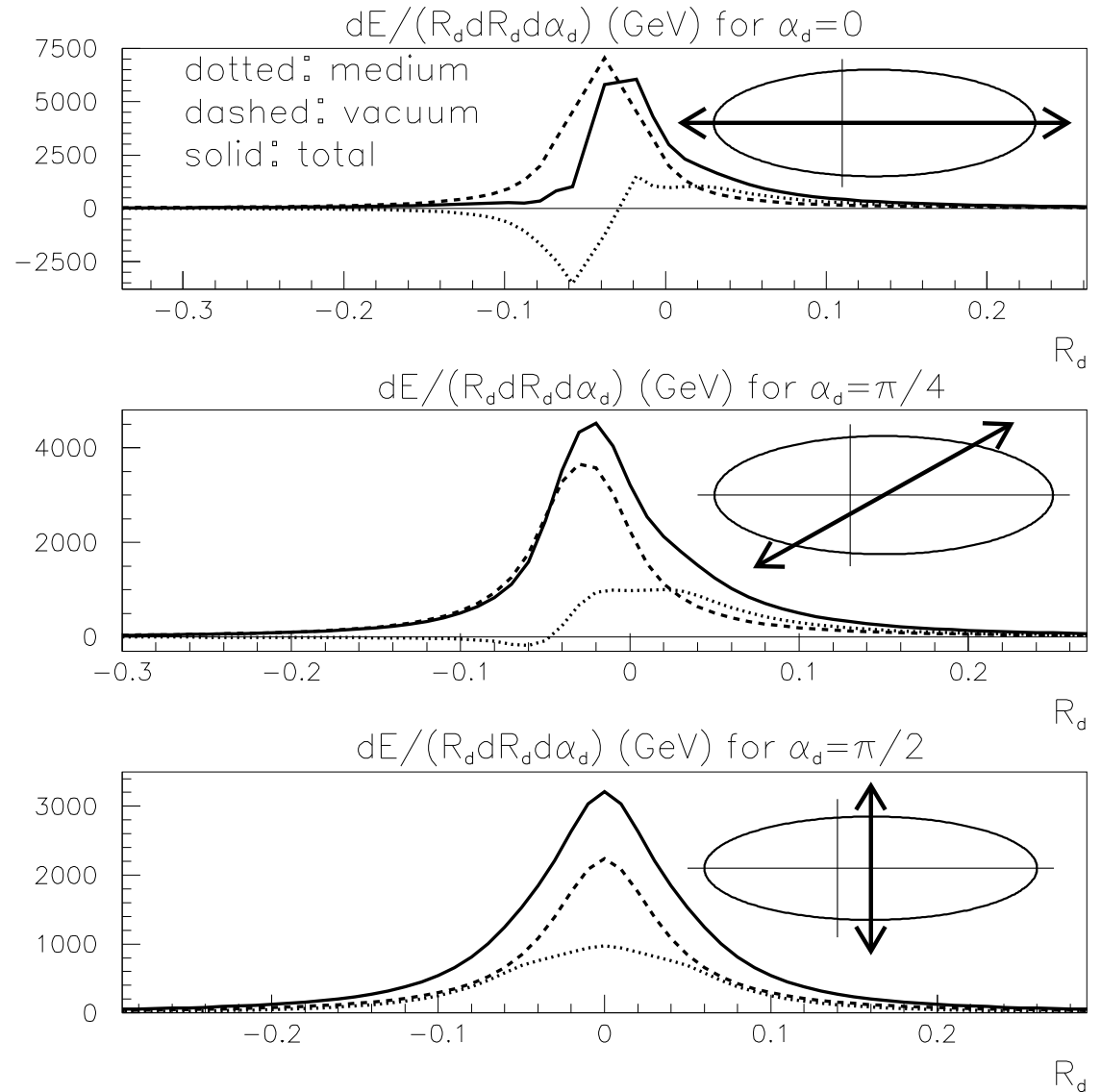
⇒ In the comoving frame  $\langle k^2 \rangle \sim \mu^2$ ,  $\Delta E \sim \alpha_s n_0 \mu^2 L^2$ .

⇒  $q_0$  characterizes the additional (asymmetric) momentum transfer.

# Jet energy distribution

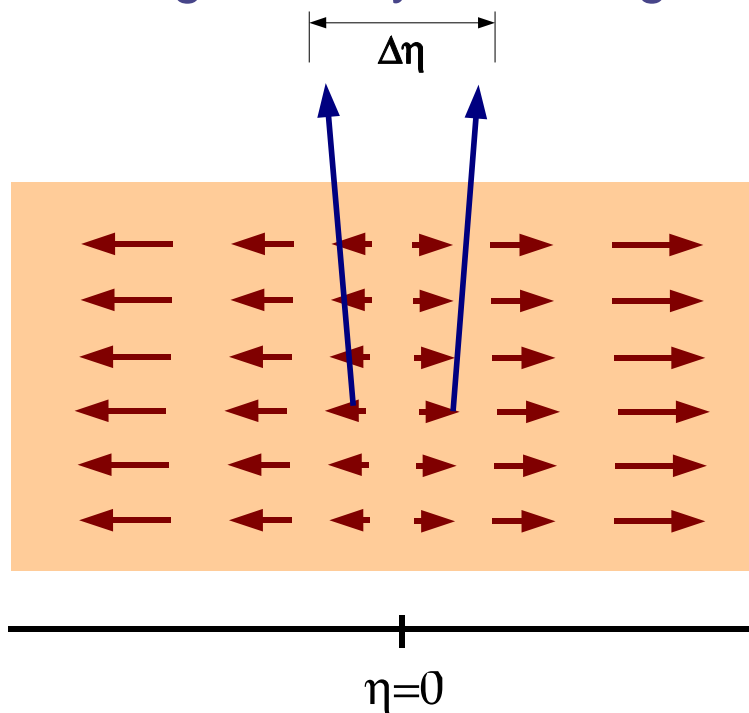


Flow in the  $+z$  direction



# Where to look for

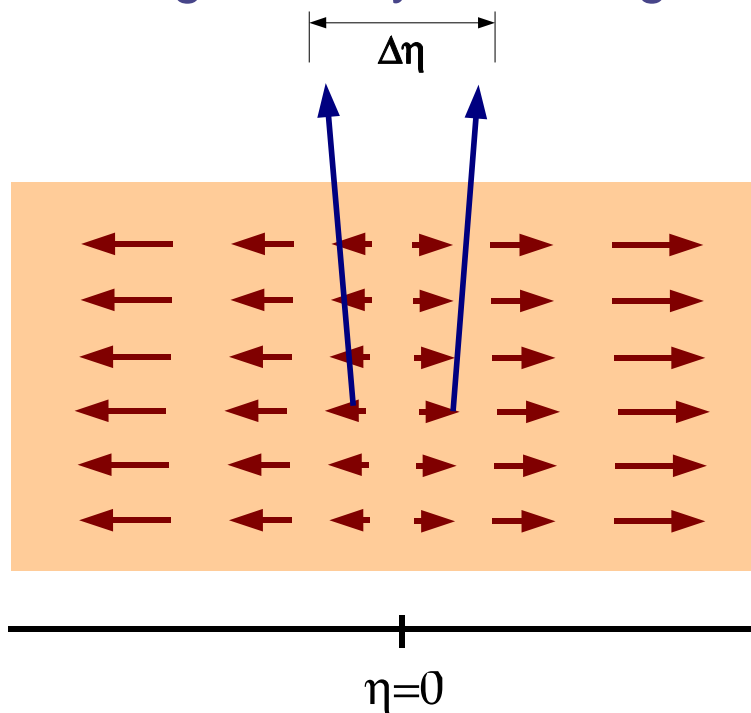
Longitudinal flow: jets are not in the longitudinally comoving frame



For symmetric  $\Delta\eta$  our previous results need to be symmetrized by adding the corresponding  $\pm q_0$ .

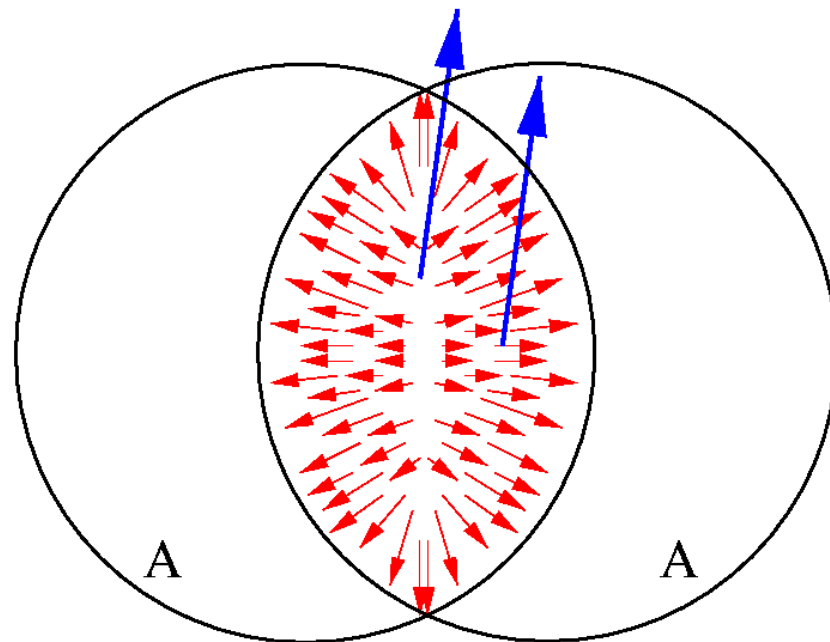
# Where to look for

Longitudinal flow: jets are not in the longitudinally comoving frame



For symmetric  $\Delta\eta$  our previous results need to be symmetrized by adding the corresponding  $\pm q_0$ .

Radial flow

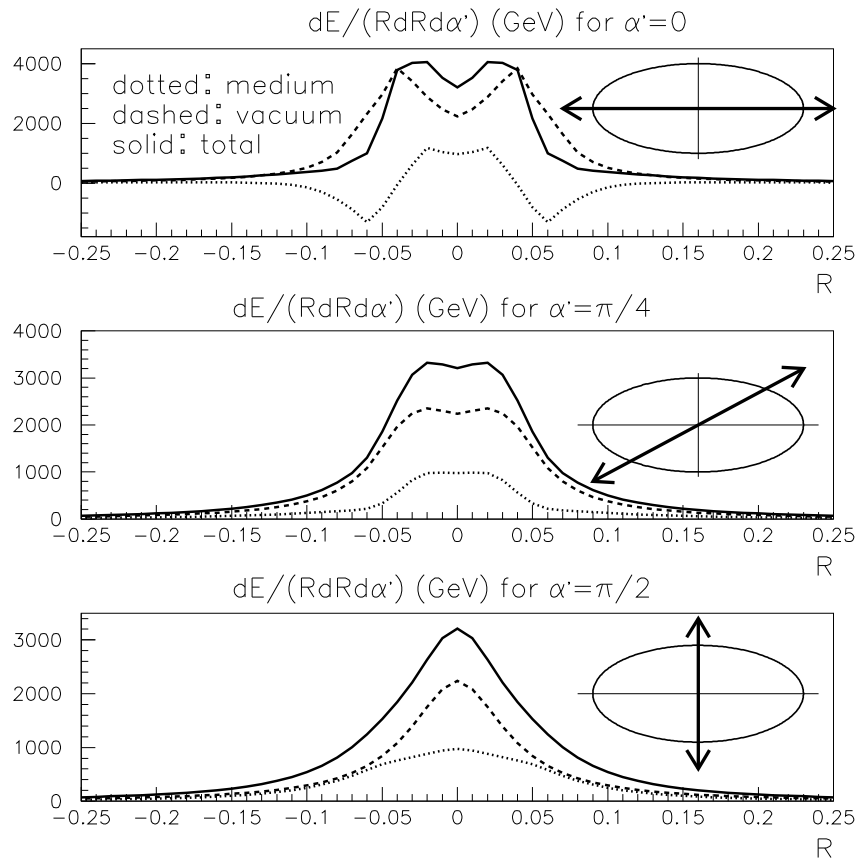


Could it be seen in the elliptic flow  $v_2$ ?



# Longitudinal flow

Jet energy distributions for a flow directed in the  $\pm z$  directions.

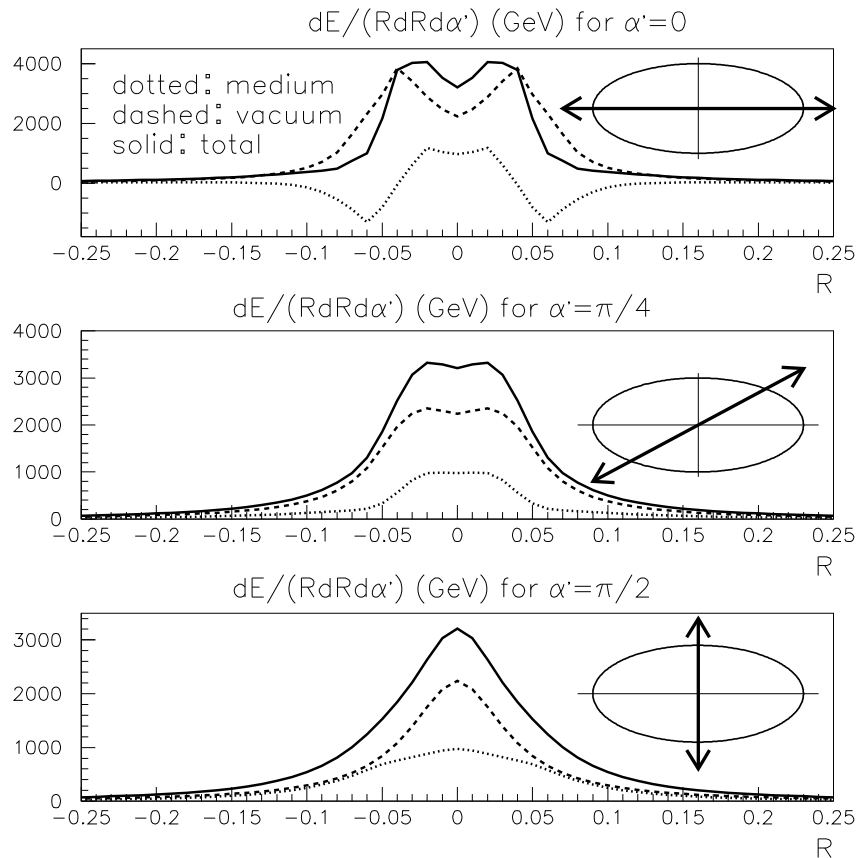


$$E_{\text{jet}} = 100 \text{ GeV}, \Delta E = 23 \text{ GeV.}$$

$$q_0 = \mu$$

# Longitudinal flow

Jet energy distributions for a flow directed in the  $\pm z$  directions.

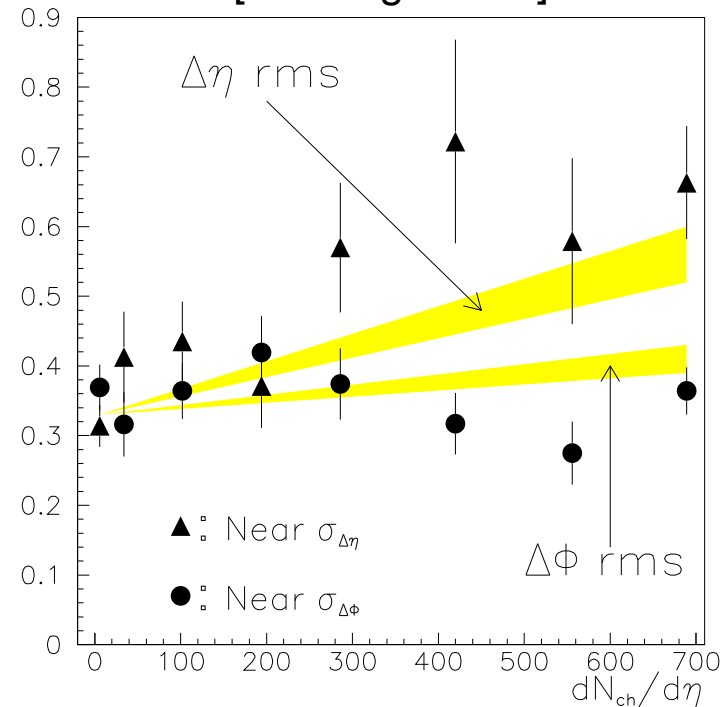


$$E_{\text{jet}} = 100 \text{ GeV}, \Delta E = 23 \text{ GeV.}$$

$$q_0 = \mu$$

Estimation of the effect for the case of RHIC (STAR preliminary)

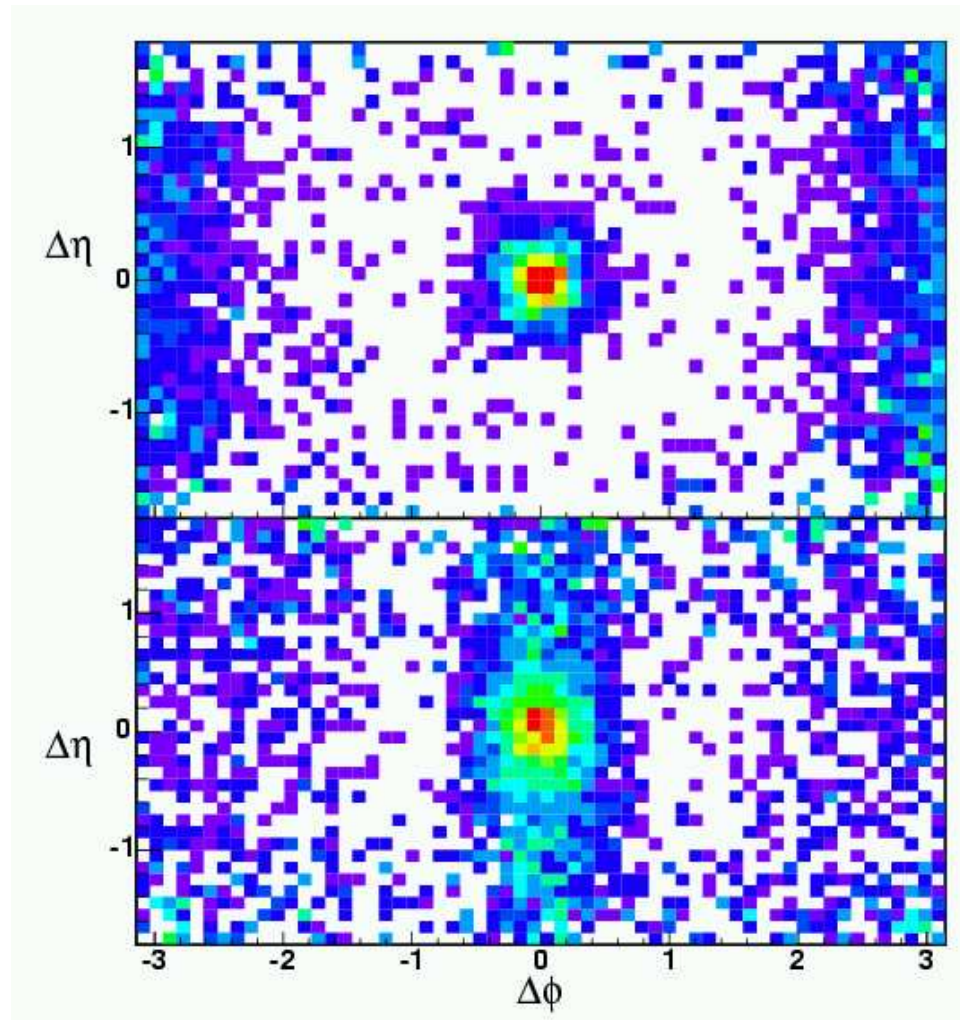
[F. Wang QM04]



Band corresponds to  $q_0/\mu = 2 \div 4$   
**Broadening in the  $\eta$ -direction more important than in  $\phi$ -direction.**

# Elongation in $\eta$ -direction

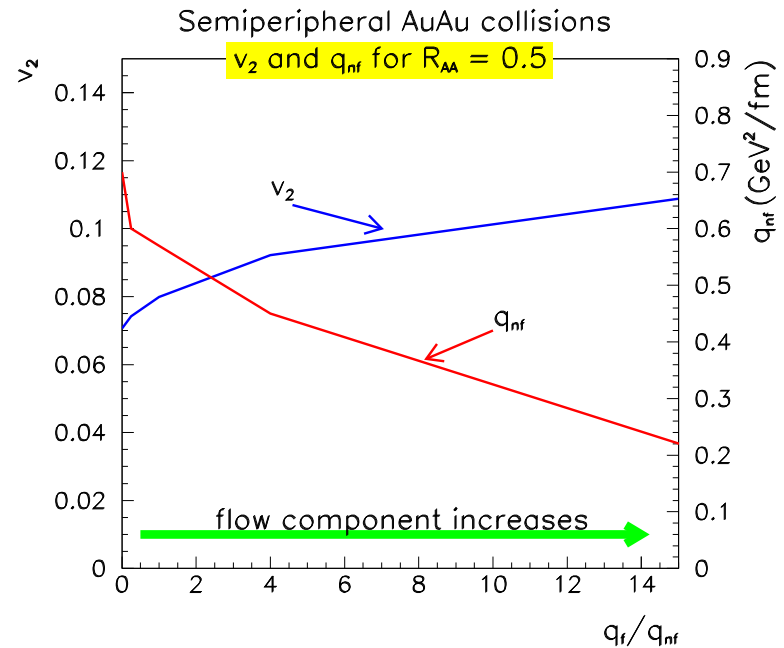
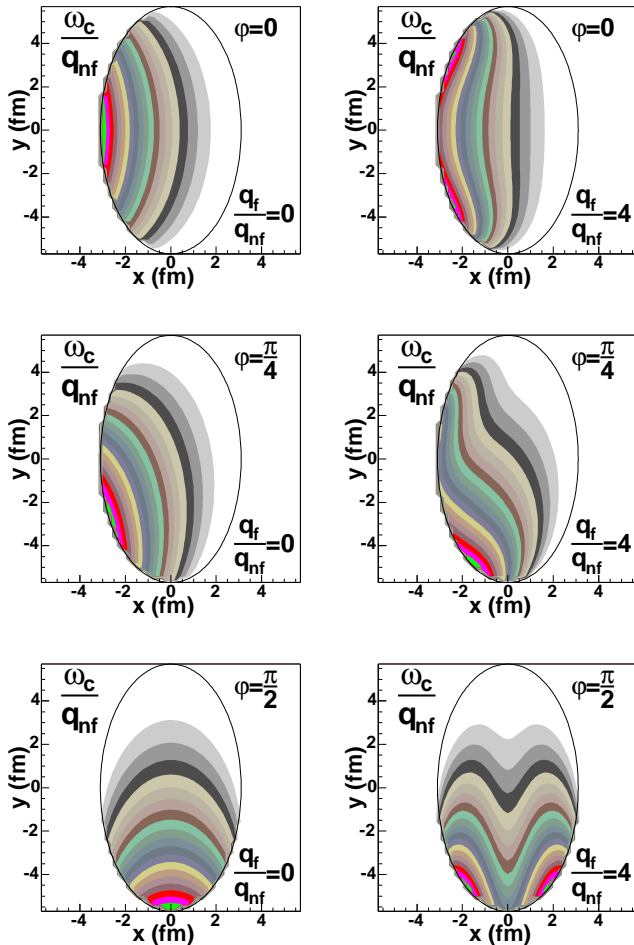
[STAR preliminary, D. Magestro HP04]



$$3 \text{ GeV} < p_t^{\text{trigg}} < 6 \text{ GeV}; \quad 2 \text{ GeV} < p_t^{\text{assoc}} < p_t^{\text{trigg}}$$

# Inclusive particle and elliptic flow

$$\Delta E \sim \omega_c(\mathbf{r}_0, \phi) = \int d\xi \xi (q_{nf} + q_f |u_T(\mathbf{r}_0(\xi)) \cdot \mathbf{n}_T|^2) \Omega(\mathbf{r}_0, \phi)$$

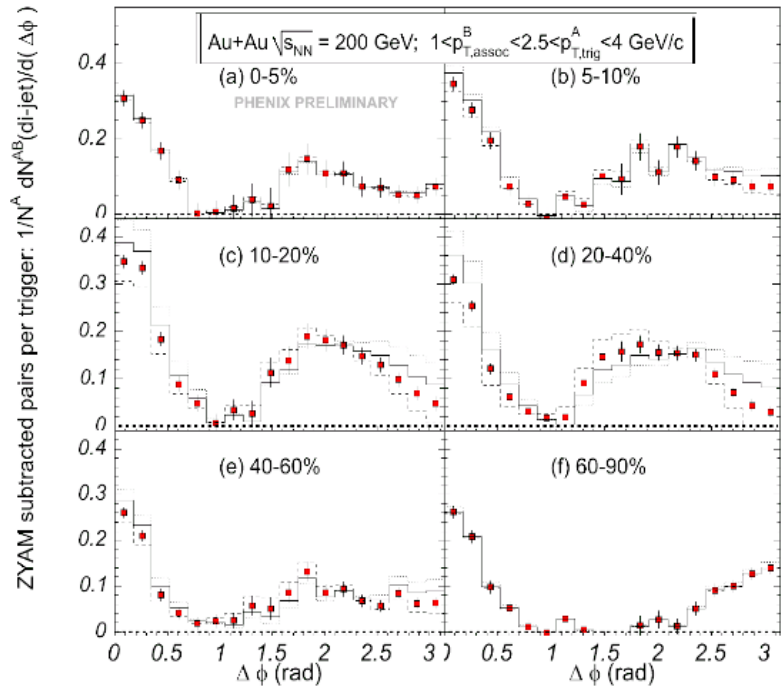
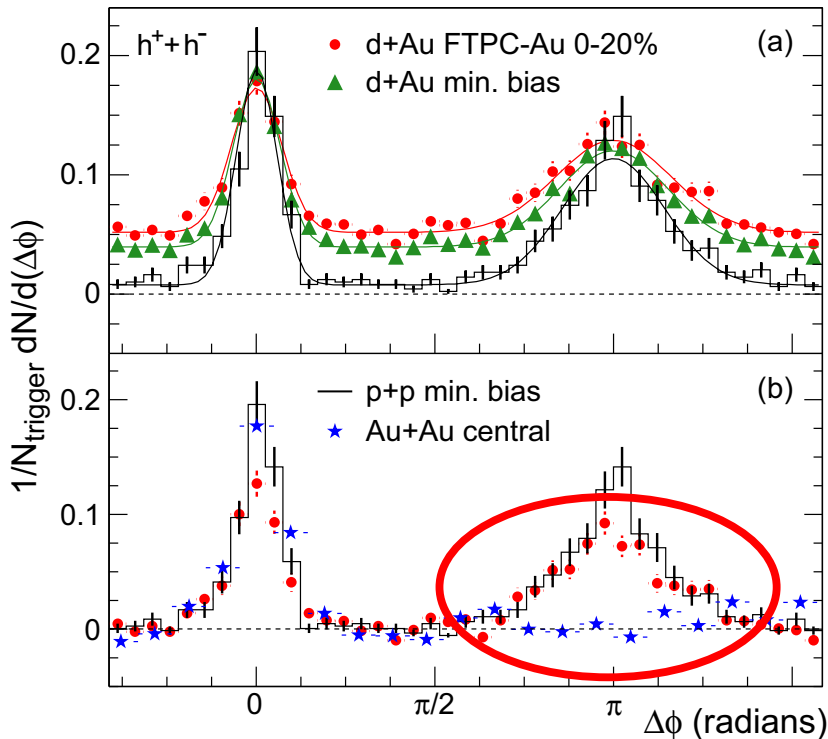


- ⇒ Correlation of the suppression w.r.t the reaction plane ( $v_2$ ) affected by the flow component.
- ⇒ More flow  $\Rightarrow$  smaller density for the same suppression

[Armesto, Salgado, Wiedemann (2004)]

# Associated particles

Where does the 'away-side jet' go?  $\implies$  smaller  $p_t$  associated particles.



[PHENIX preliminary]

$\implies$  Not jet-like structure in the backwards hemisphere

$\implies$  Thermalization of the high- $p_t$  particle??

$\implies$  Sonic shock waves?? [Casalderrey-Solana, Shuryak, Teaney]

# Large angle radiation

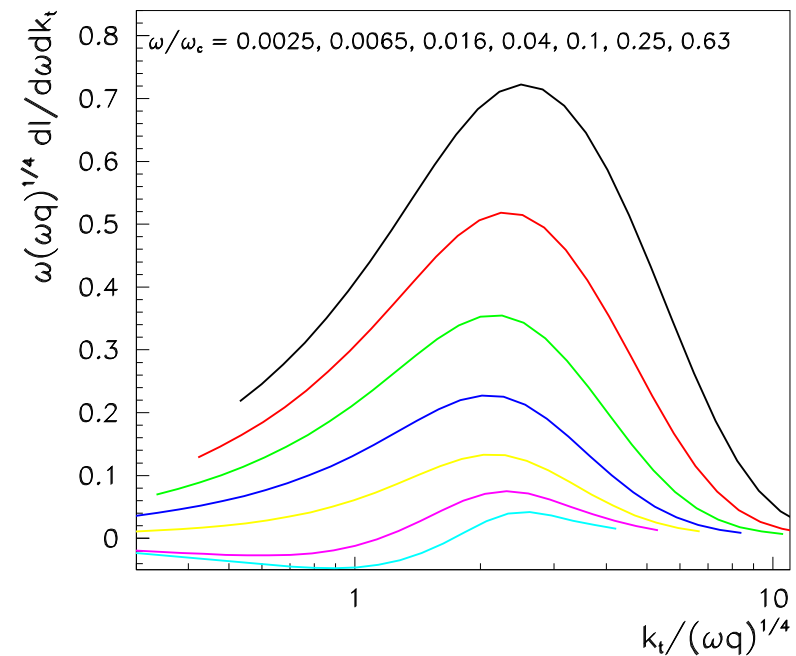
Remember the spectrum

The radiation is suppressed for

$$\sin \theta \lesssim \sqrt{\sqrt{\frac{\hat{q}}{\omega^3}}}$$

Radiation is large angle for

$$\omega \lesssim \omega_{\min} \sim \hat{q}^{1/3}$$



In qualitative agreement with the away-side signal ?

# Conclusions

- ⇒ Inclusive particle production presents limitations in the characterization of the medium.
  - ↪ Study less inclusive observables
- ⇒ Heavy quarks: Smaller medium-induced radiation
  - ↪ Surface emission makes the mass effect smaller
  - ↪ LHC will measure mass effects in a large  $p_t$  range with  $B$  mesons
- ⇒ Jet-broadening directly related to energy loss by medium-induced gluon radiation.
  - ↪ Measure jet structure in HIC (control over multiplicity background).
- ⇒ A flow field in the medium produces additional (anisotropic) gluon radiation
  - ↪ Asymmetric jet shapes (elongation in  $\eta$ -direction).
  - ↪ Contributes to  $v_2$  and suppression (can this explain the opacity problem?)