

V_4 FROM IDEAL AND VISCOUS HYDRODYNAMICS

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9 April 2010

Rencontres Ions Lourds

OUTLINE

- 1 INTRODUCTION/REVIEW
 - Hydrodynamics
 - Azimuthal correlations— v_2 , v_4
 - Previous results
- 2 RESULTS FROM HYDRODYNAMICS
 - RHIC results
 - LHC prediction
- 3 CONCLUSIONS

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HYDRODYNAMICS

A system close to local thermal equilibrium will behave according to hydrodynamic equations, consisting of:

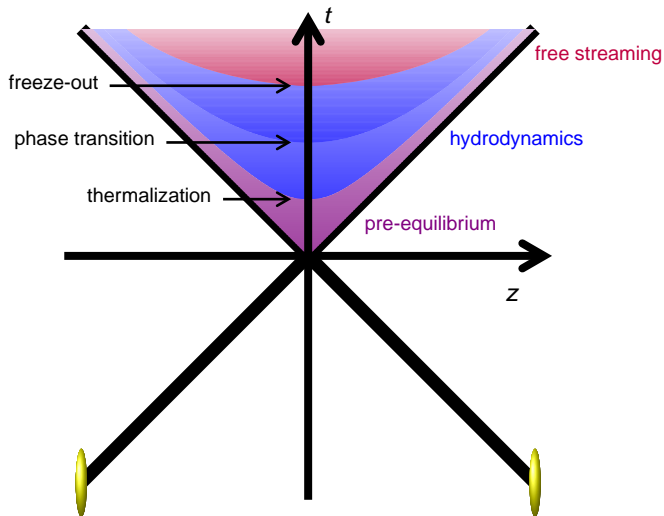
- Conservation of energy-momentum:

$$0 = \partial_\mu T^{\mu\nu} \equiv \partial_\mu (T_0^{\mu\nu} + \Pi^{\mu\nu}) = \partial_\mu ((\epsilon + p)u^\mu u^\nu - pg^{\mu\nu} + \Pi^{\mu\nu})$$

- Any other conservation laws: $\partial_\mu j^\mu = 0$
- Equation of state: $p = p(\epsilon)$

With appropriate boundary conditions, we can model a heavy ion collision.

HYDRODYNAMIC EVOLUTION OF A NUCLEAR COLLISION



FREEZE OUT

- At freeze out the fluid is converted into particles

$$\frac{dN}{dY d^2p_t} \propto \int p_\mu d\Sigma^\mu f(p^\mu)$$

- with a distribution function given by kinetic theory

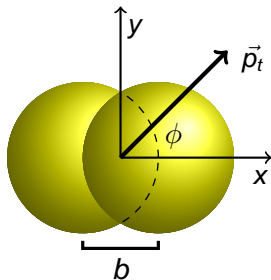
$$f = f_0 + \delta f = e^{(-E/T)} \left[1 + (g(p)?) p_i p_j \Pi^{ij} \right]$$

- (form of δf depends on microscopic dynamics)

$V_2, V_4, \text{ ETC.}$

To compare to experiment, compute azimuthal moments:

$$\frac{dN}{dY d^2p_t} = v_0 \left[1 + \sum_n 2v_n \cos(n\phi) \right]$$

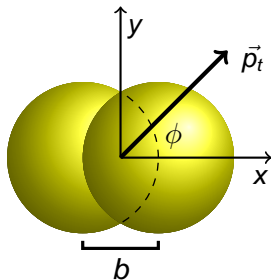


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Elliptic flow: $v_2 \equiv \langle \cos(2\phi) \rangle$



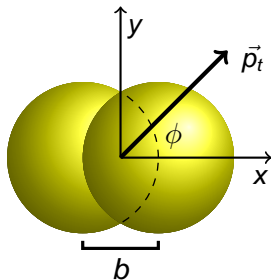
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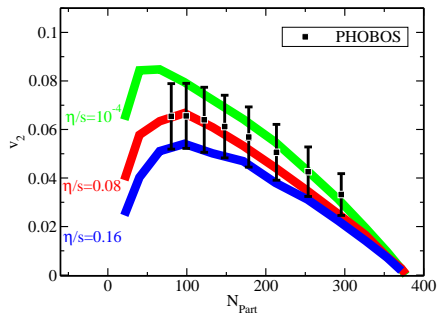
Elliptic flow: $v_2 \equiv \langle \cos(2\phi) \rangle$

Hexadecapole flow: $v_4 \equiv \langle \cos(4\phi) \rangle$

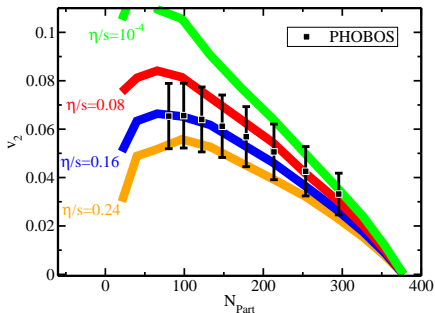


ELLIPTIC FLOW (v_2)

Glauber



CGC



(ML / Romatschke arXiv:0804.4015)

- Large measured v_2 indicates small viscosity, but exact value depends on initial eccentricity.

IDEAL HYDRODYNAMICS PREDICTION: $v_4/(v_2)^2 = 1/2$

Perform a saddle point approximation:

$$\frac{dN}{dY d^2p_t} = \frac{d}{(2\pi)^3} \int p_\mu d\Sigma^\mu e^{(-\frac{p \cdot u}{T})}$$

For large p_t , saddle point is at the maximum u parallel to momentum:

$$u_{\max}(\phi) = U(1 + 2V_2 \cos(2\phi) + 2V_4 \cos(4\phi) + \dots)$$

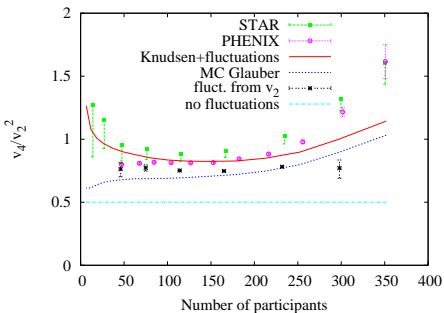
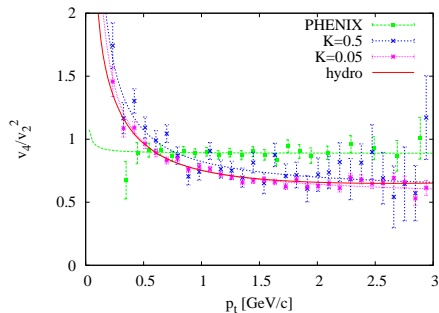
$$\implies v_2(p_t) = \frac{V_2 U}{T} (p_t - m_t v)$$

$$\begin{aligned} v_4(p_t) &= \frac{1}{2} \frac{(V_2 U)^2}{T^2} (p_t - m_t v)^2 + \frac{V_4 U}{T} (p_t - m_t v) \\ &= \frac{1}{2} v_2(p_t)^2 + \frac{V_4}{V_2} v_2(p_t) \end{aligned}$$

$$(v \equiv U/\sqrt{1+U^2})$$

(Borghini / Ollitrault nucl-th/0506045)

EXISTING DATA / CALCULATIONS FOR $v_4/(v_2)^2$



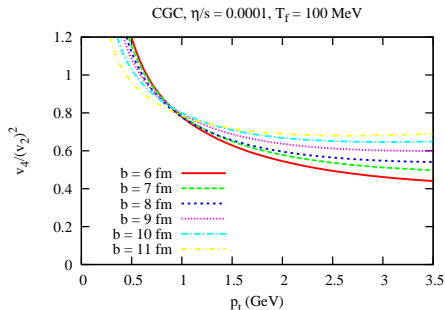
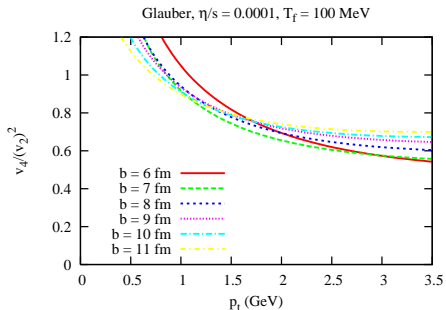
(Gombeaud / Ollitrault arXiv:0907.4664)

- Experimental results are larger than 1/2.
- Most of the discrepancy can be understood from fluctuations.

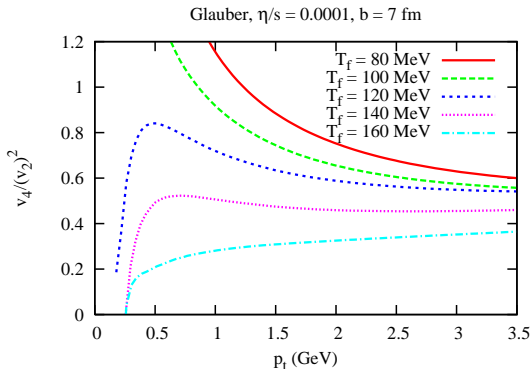
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COMPARE TO PREVIOUS RESULTS: IDEAL HYDRO WITH $T_f = 100$ MeV



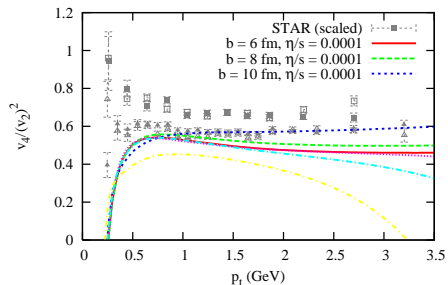
- Like previous calculations: Asymptotes to $\sim 1/2$ with corrections like $1/p_t$
- Some unexpected impact parameter dependence, but **not** due to initial eccentricity.

SENSITIVITY TO T_f 

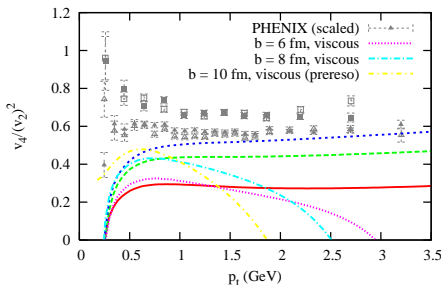
- $v_4/(v_2)^2$ sensitive to T_f
- (For ideal hydro) best-fit T_f for other observables (140 MeV) also results in flat $v_4/(v_2)^2$

VISCOUS RESULTS AT REALISTIC $T_f = 140$ MeV

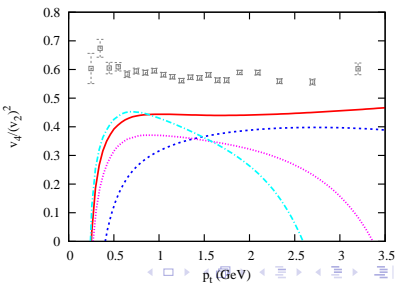
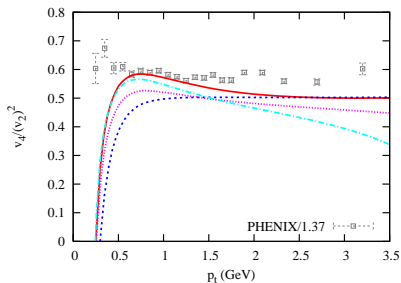
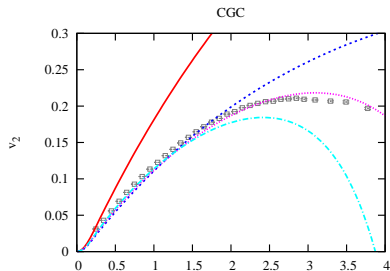
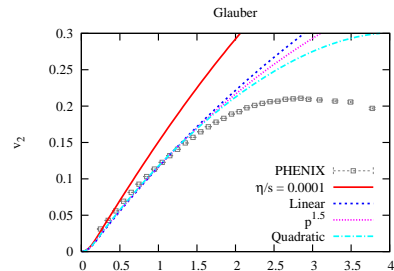
Glauber



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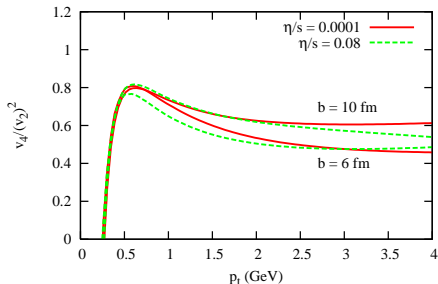


- Viscosity *lowers* $v_4/(v_2)^2$
- Standard “quadratic ansatz” for δf destroys flat curve and increases dependence on b
- Using a different δf can fix some of this:

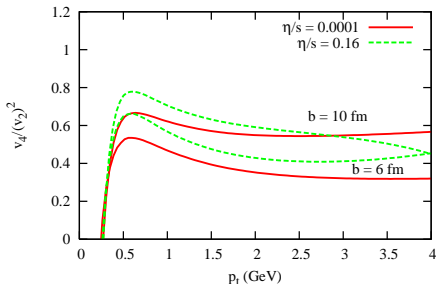
δf DEPENDENCE

LHC PREDICTION

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- Similar to RHIC results at slightly lower freeze out temperature
- Viscous corrections are smaller, making choice for δf less relevant.

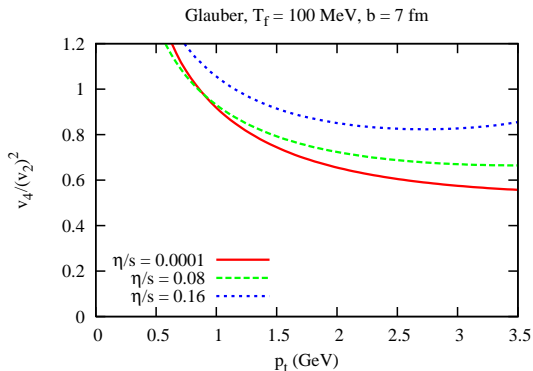
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SUMMARY/CONCLUSIONS

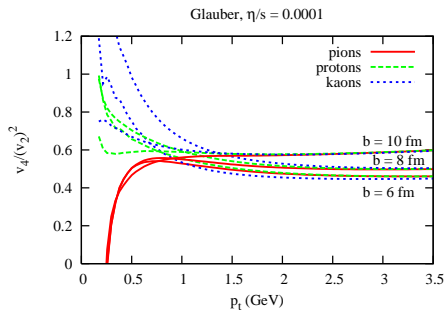
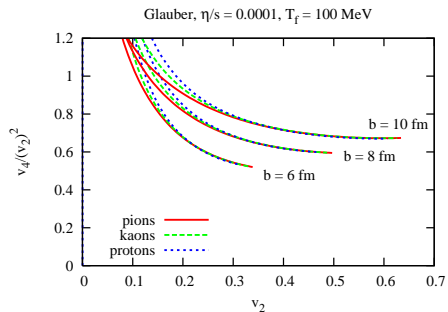
- Hydrodynamic simulations confirm expectation of $v_4/(v_2)^2 \sim 1/2$
- Sensitive to T_f , with 140 MeV giving a flat dependence on p_t in ideal hydro (and for δf with weak p_t dependence)
- $v_4/(v_2)^2$ is insensitive to initial eccentricity (unlike v_2)
- Viscosity tends to decrease $v_4/(v_2)^2$ for a realistic T_f
- Viscosity increases impact parameter dependence for standard quadratic ansatz for δf , but *decreases* it for weaker p_t dependence.
- $v_4/(v_2)^2$ at LHC should be similar to RHIC

VISCOUS EFFECTS



- Like in transport calculations, viscosity increases $v_4/(v_2)^2$ (but only with a small T_f)

IDENTIFIED PARTICLES



- Identified particles have same $v_4/(v_2)^2$