



# B meson semileptonic decays

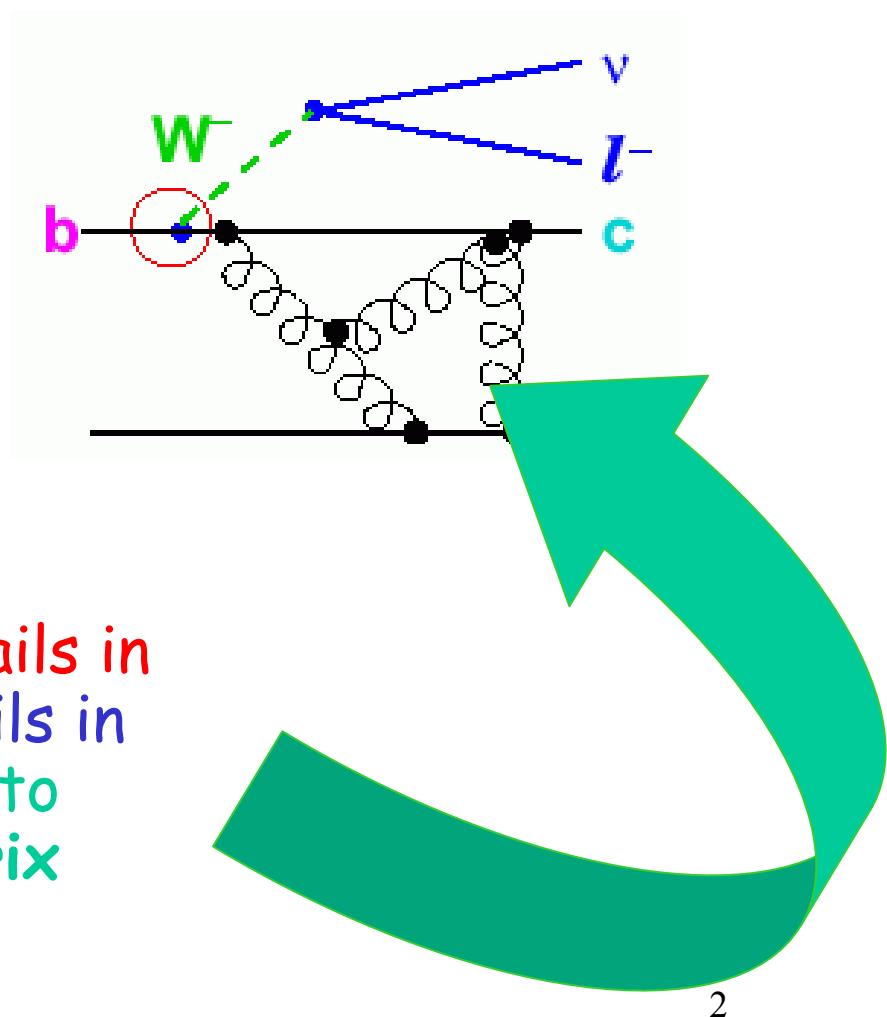
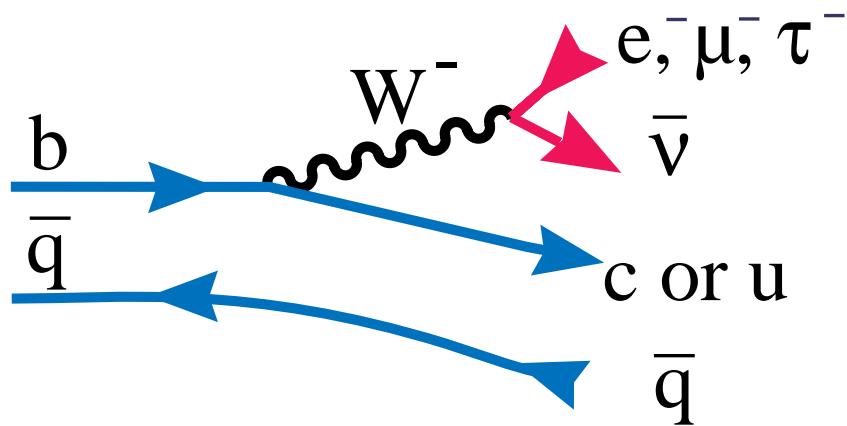
- Physics Motivation
- Inclusive properties:
  - Semileptonic width
  - Moments of inclusive quantities
- Exclusive decays
- What is the semileptonic width made of?
- Charmless semileptonic decays
- Conclusions

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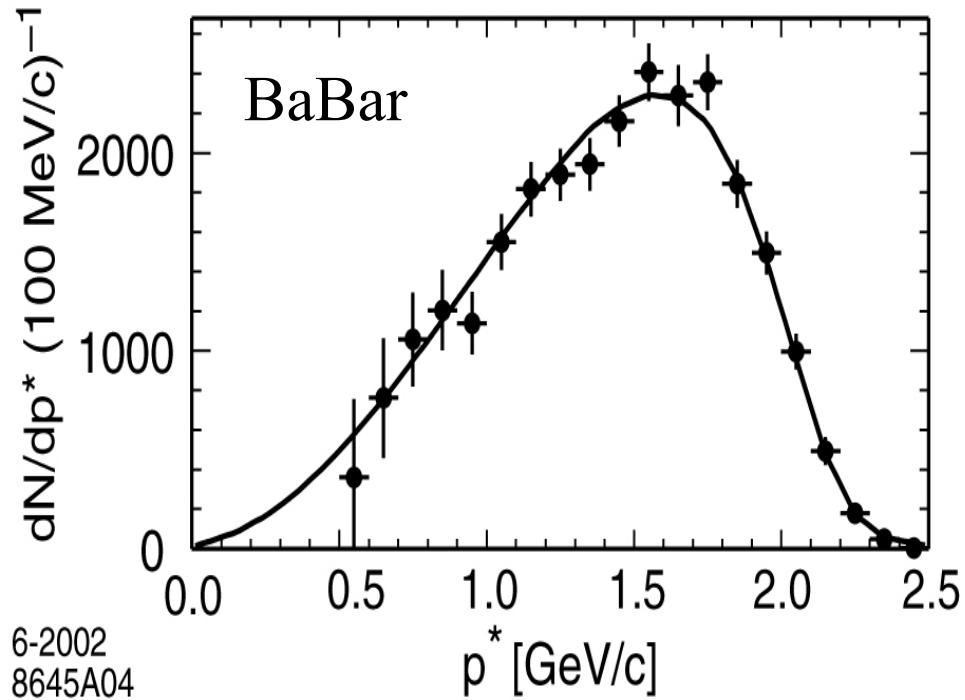
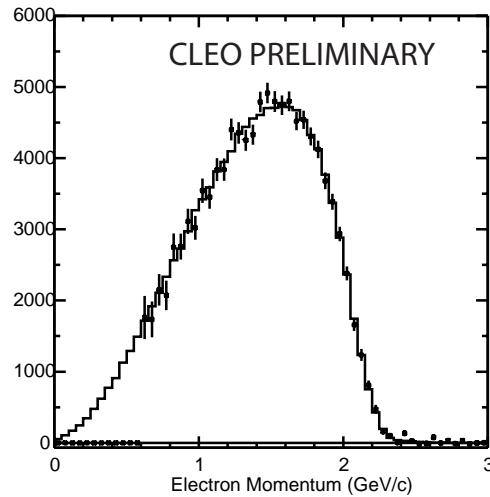
# Physics Motivation



- Ultimate goal: a precise determination of  $V_{cb}$  (more details in M. Calvi talk) &  $V_{ub}$  (more details in E. Thorndike talk) but we need to take care of the hadronic matrix element



# Inclusive semileptonic branching fractions



High momentum lepton tag to identify  $b \rightarrow (c,u)\ell\nu$

CLEO (new-prelim) [ $10 \text{ fb}^{-1}$ ]	$10.88 \pm 0.08 \pm 0.33\%$
BaBar [ $5.07 \text{ fb}^{-1}$ ]	$10.87 \pm 0.18 \pm 0.30\%$
Belle [ $5.1 \text{ fb}^{-1}$ ]	$10.90 \pm 0.12 \pm 0.49\%$
LEP (most recent EW fit)	$10.59 \pm 0.22\%$



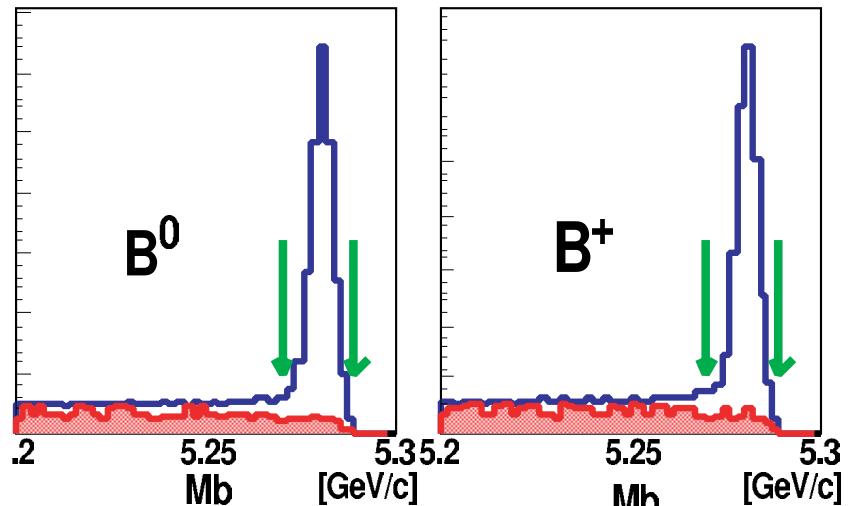
# Belle: inclusive semileptonic decays with fully reconstructed tags

Tagging modes considered:

$$\bar{B}^0 \rightarrow \left\{ \begin{array}{l} D^{*+}\pi^- / D^{*+}\rho^- / D^{*+} a_1 \\ D^+\pi^- / D^+\rho^- / D^+ a_1 \end{array} \right.$$

$$B^- \rightarrow \left\{ \begin{array}{l} D^{*0}\pi^- / D^{*0}\rho^- / D^{*0} a_1 \\ D^0\pi^- / D^0\rho^- / D^0 a_1 \end{array} \right.$$

on-res. data  
 off-res. data scaled by luminosity



$21915 \pm 202$  events     $24529 \pm 227$  events  
purity: 87.2%              purity: 85.6%

$D^0 \rightarrow K^+ \pi^-$ ,  $K^+ \pi^- \pi^0$ ,  $K^+ \pi^- \pi^0$ ,  $K^+ \pi^- \pi^+ \pi^-$ ,  $K_s \pi^- \pi^+$

$D^+ \rightarrow K^+ \pi^+ \pi^-$ ,



# Belle: inclusive charged and neutral B branching fractions

The inclusive charged and neutral B semileptonic branching fractions measured separately:

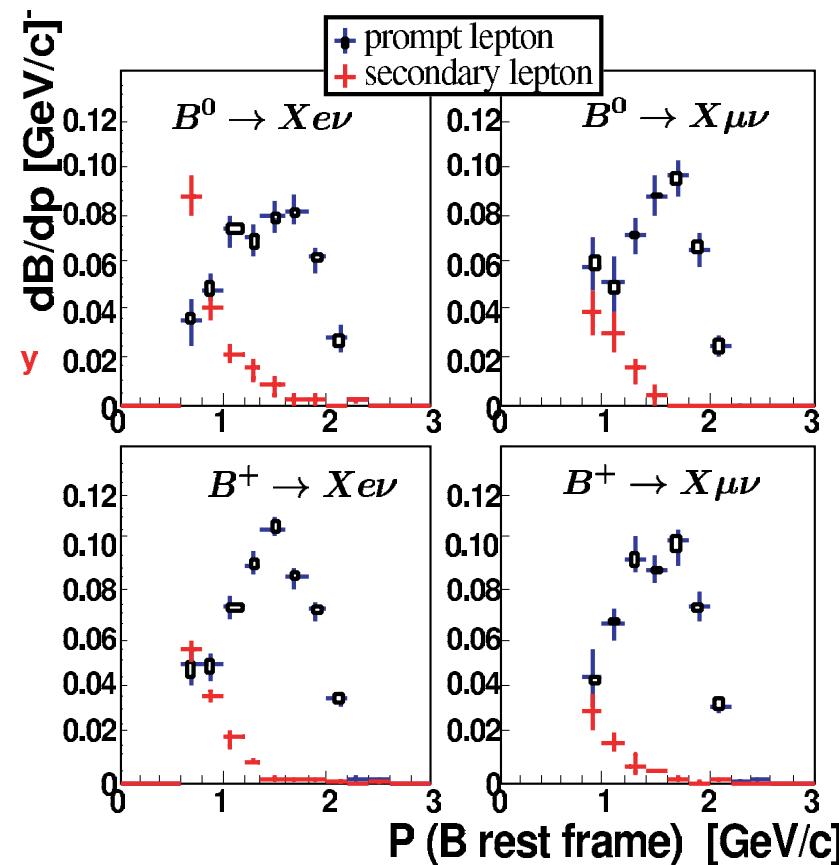
$$B(B^0 \rightarrow X\ell\nu) = (10.32 \pm 0.32 \pm 0.29)\%$$

$$B(B^+ \rightarrow X\ell\nu) = (11.92 \pm 0.26 \pm 0.32)\%$$

$$\Rightarrow f^+/f^0 = 1.14 \pm 0.04|_{\text{exp}} \pm 0.01|_{\text{theory}}$$

$$B(B \rightarrow X\ell\nu) = (11.19 \pm 0.20|_{\text{exp}} \pm 0.31|_{\text{theory}})\%$$

**preliminary**





# What makes up the $b \star c \ell \nu$ width?

PDG 2003 average HFAG  
working group

	B(%)
$B \star X \ell \nu$	$10.70 \pm 0.28$
$B \star D^* \ell \nu$	$5.53 \pm 0.23$
$B \star D \ell \nu$	$2.14 \pm 0.20$

About 27% of the semileptonic branching fraction is poorly known! This has important implications for our ability to understand HQET, OPE... we need to nail this component down with further experimental information!



# The hadronic matrix element

- Theoretical framework: Heavy Quark Expansion (more on N. Uraltsev talk)
- Issues to be explored by experiments:
  - Underlying theoretical accuracy: are all the uncertainties quantified? In particular ansatz of quark-hadron duality.
  - Experimental determination of the Heavy quark expansion parameters, in particular:
    - $m_b, m_c$  at the relevant mass scale
    - $\mu_\pi^2$  [ $\lambda_1$ ] kinetic energy of the b quark
    - $\mu_G^2$  [ $\lambda_2$ ] expectation value of chromomagnetic op.



# $m_b$ : a multifaceted fundamental parameter

Important for  $V_{c(u)b}$

	$m_{\text{kin}}(\text{GeV})$	$\bar{m}_b(\bar{m}_b)$ (GeV)	method
Beneke,Signer, Smirnov	-	$4.26 \pm 0.12$	Sum rules
Melnikov	$4.56 \pm 0.06$	$4.20 \pm 0.1$	Sum rules
Hoang	$4.57 \pm 0.06$	$4.25 \pm 0.09$	Sum rules
Jamin,Pich	-	$4.19 \pm 0.06$	Sum rules, no resummation
Pineda,Yndurain	-	$4.44^{-0.04}_{+0.03}$	$Q(1S)$ mass
NRQCD	-	$4.28 \pm 0.03 \pm 0.03 \pm 0.10$	Lattice HQET ( $n_f=2$ )

○ expansion

Jet observables sensitive to b mass(LEP)

+ pole mass  $m_b^{\text{pole}} \approx m_{\text{kin}} + 0.255 \text{ GeV}$  Bigi-Mannel hep/ph/0212021

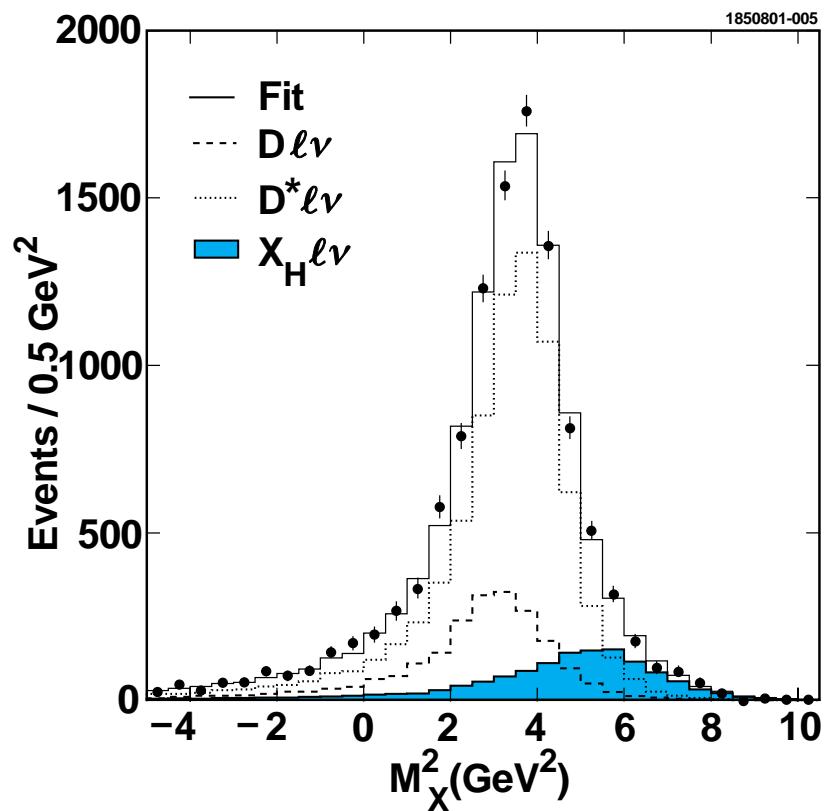


# Experimental tools: moments of the kinematic variables

- Approaches used:
  - Moments of  $E_\ell$
  - Moments of  $M_x$ , invariant mass of the hadronic system recoiling against the  $\ell-\nu$  pair
  - Multivariate analysis including  $q^2$ ,  $E_\ell$ ,  $M_x$
- Data available from CLEO, BaBar, Belle

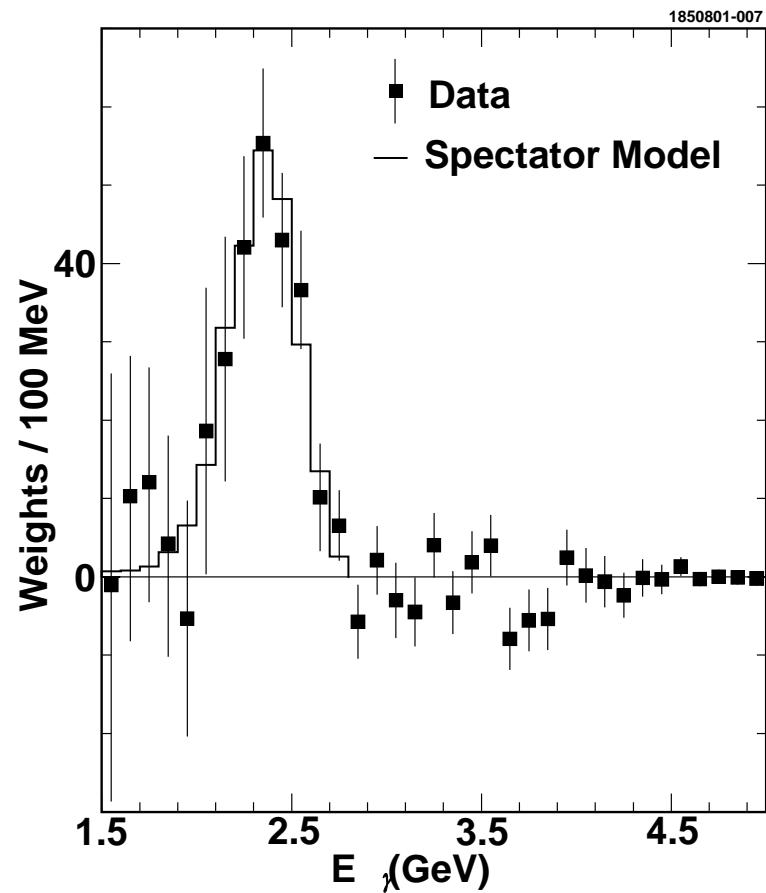


# CLEO: $M_X$ with cut $p_\ell > 1.5 \text{ GeV}/c$ and $b \rightarrow S\gamma$ (prl87[2001]251808; prl87[2001]251807)



$$\langle M_X^2 - \bar{M}_D^2 \rangle = (0.251 \pm 0.023 \pm 0.062) \text{ GeV}^2$$

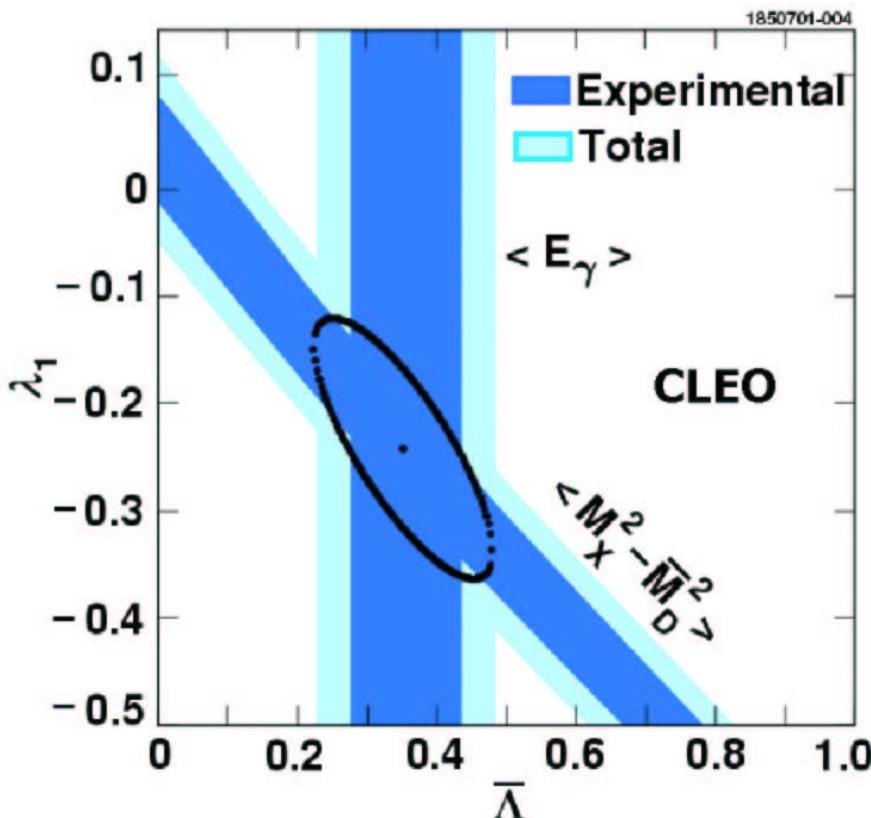
$$\langle (M_X^2 - \bar{M}_D^2)^2 \rangle = (0.639 \pm 0.056 \pm 0.178) \text{ GeV}^2$$



$$\langle E_\gamma \rangle = (2.346 \pm 0.032 \pm 0.011) \text{ GeV}$$



# The HQE parameters



$$\bar{\Lambda} = (0.35 \pm 0.07 \pm 0.10) \text{ GeV}$$

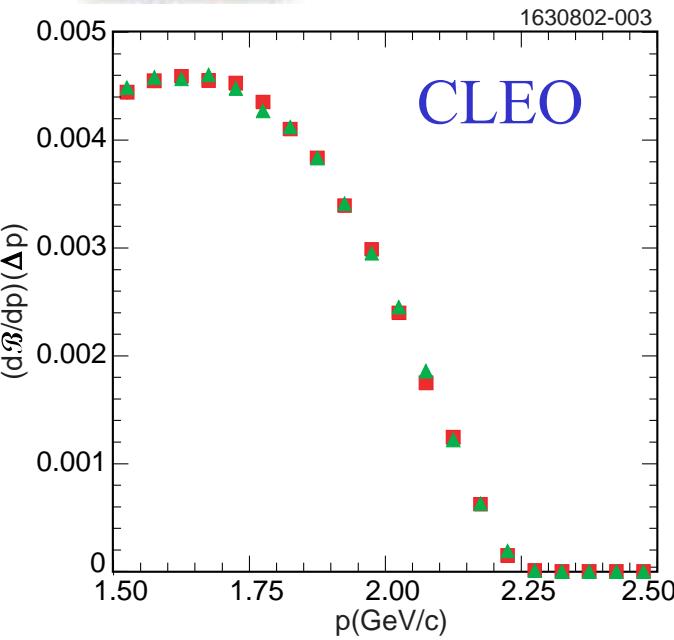
$$\lambda_1 = (-0.238 \pm 0.071 \pm 0.078) \text{ GeV}^2$$

Scheme dependent

MS to order  $1/M^3$ ,  $\beta_0 \alpha_s^2$



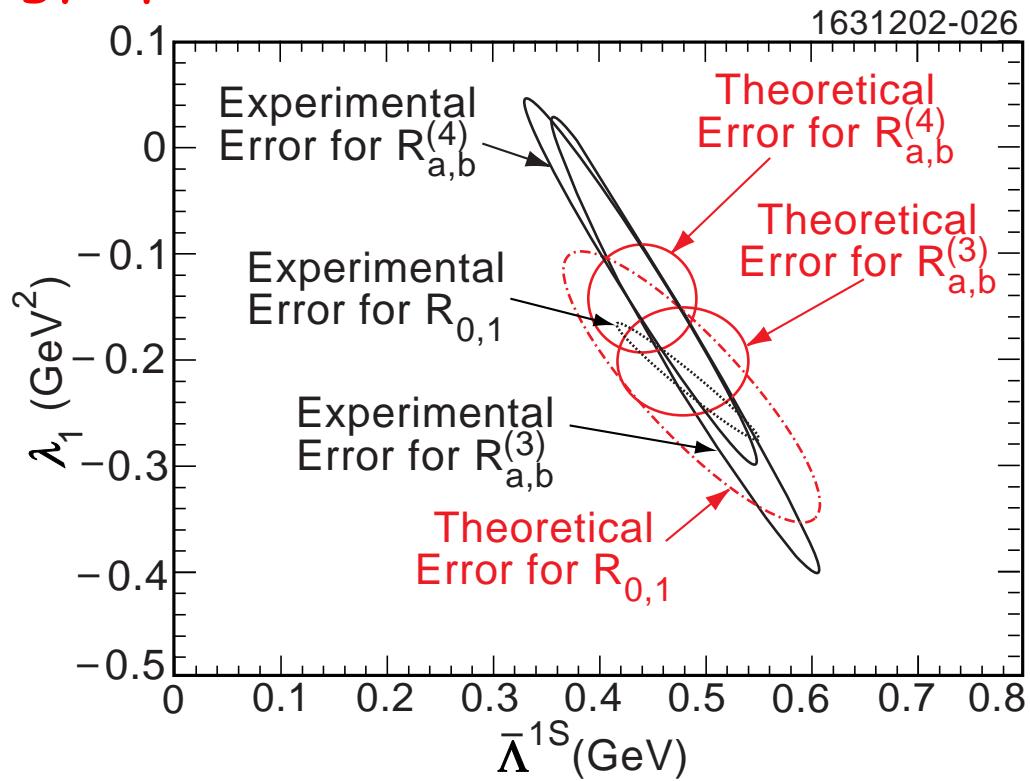
# Truncated moments of the lepton energy spectrum



$$R_0 = \frac{\int_{1.7 GeV}^{\infty} \left( \frac{d\Gamma}{dE_l} \right) dE_l}{\int_{1.5 GeV}^{\infty} \left( \frac{d\Gamma}{dE_l} \right) dE_l}$$

$$R_1 = \frac{\int_{1.5 GeV}^{1.7 GeV} E_l \left( \frac{d\Gamma}{dE_l} \right) dE_l}{\int_{1.5 GeV}^{\infty} \left( \frac{d\Gamma}{dE_l} \right) dE_l}$$

Gremm, Kapustin, Ligeti, Wise  
PRL77(1996)20



$m_b(\text{pole}) = (4.90 \pm 0.08 \text{ | exp} \pm 0.13 \text{ | th}) \text{ GeV} \Leftrightarrow$   
 $m_b(\text{pole}) = (4.82 \pm 0.06) \text{ GeV}$  analysis of  
beauty production at threshold

$$m_b^{1S} = (4.82 \pm 0.07 \text{ [exp]} \pm 0.11 \text{ [th]}) \text{ GeV}/c^2$$

$$\lambda_1 = (-0.25 \pm 0.02 \pm 0.05 \pm 0.14) \text{ GeV}^2$$



# Summary of the CLEO measurements

method	$\bar{\Lambda}(\text{GeV})$	$\lambda_1(\text{GeV}^2)$
$b \rightarrow s\gamma, M_x$	$0.35 \pm 0.07 \pm 0.1$	$-0.238 \pm 0.071 \pm 0.078$
Truncated lepton energy mom	$0.39 \pm 0.03 \pm 0.06 \pm 0.12$	$-0.25 \pm 0.02 \pm 0.05 \pm 0.14$

Agreement even too good!  $1/m_b^3$  dominant uncertainty

Consistent with  $m_b$  extracted from b production at threshold



## DELPHI study of spectral moments

- Measured first 3 moments of  $E_\ell$  and  $M_x$ , using a multiparameter fit (more details in M. Calvi's talk)

$$\bar{\Lambda} = 0.40 \pm 0.10 \pm 0.02 \text{ GeV}$$

$$\lambda_1 = (-0.15 \pm 0.07 \pm 0.03) \text{ GeV}^2$$

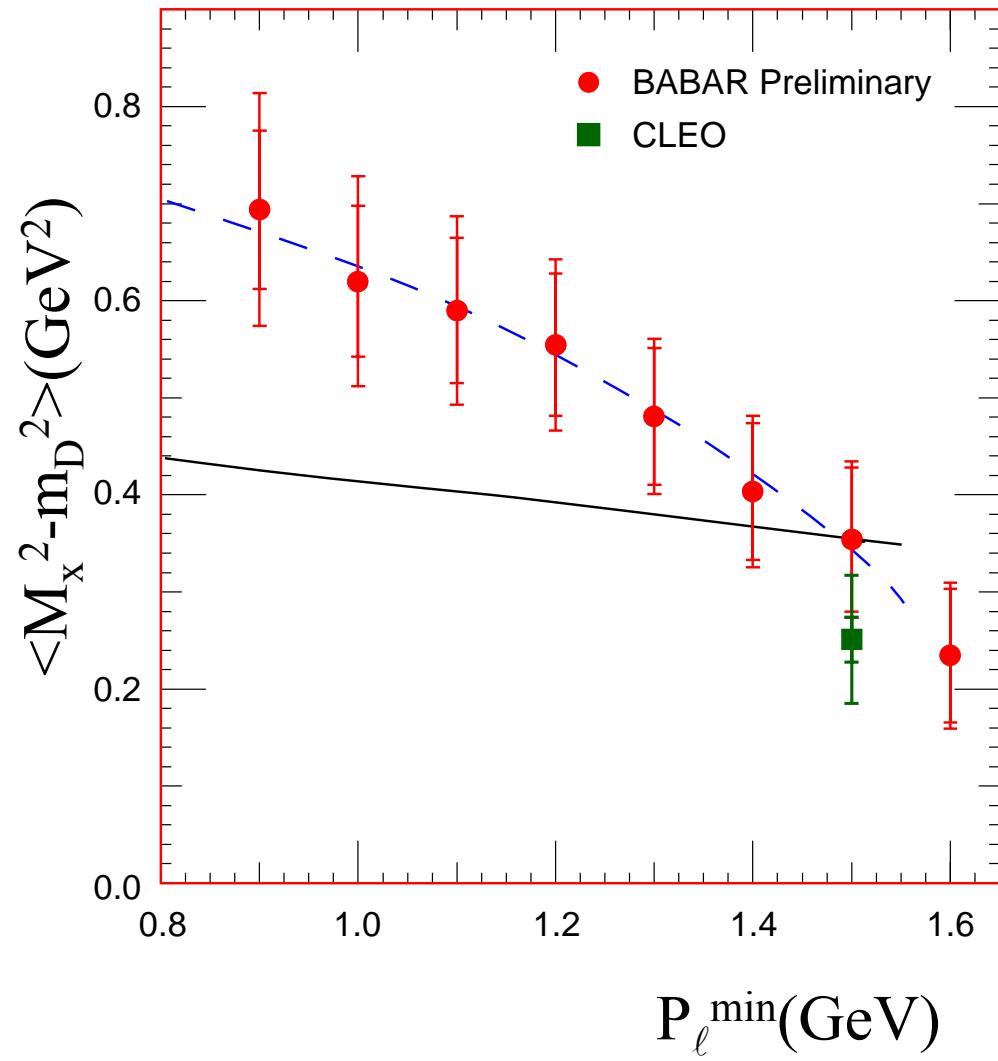
Consistent with CLEO results

Amazingly small systematic errors



# First moment of $M_x$ from BaBar

- Data seem to show that average mass higher if momentum cut is relaxed: tail of high mass states predicted by N. Isgur [plb448(1999)111]?
- "Underlying assumptions of HQE + OPE require further scrutiny"
- Updated results from BaBar and CLEO expected at summer conferences





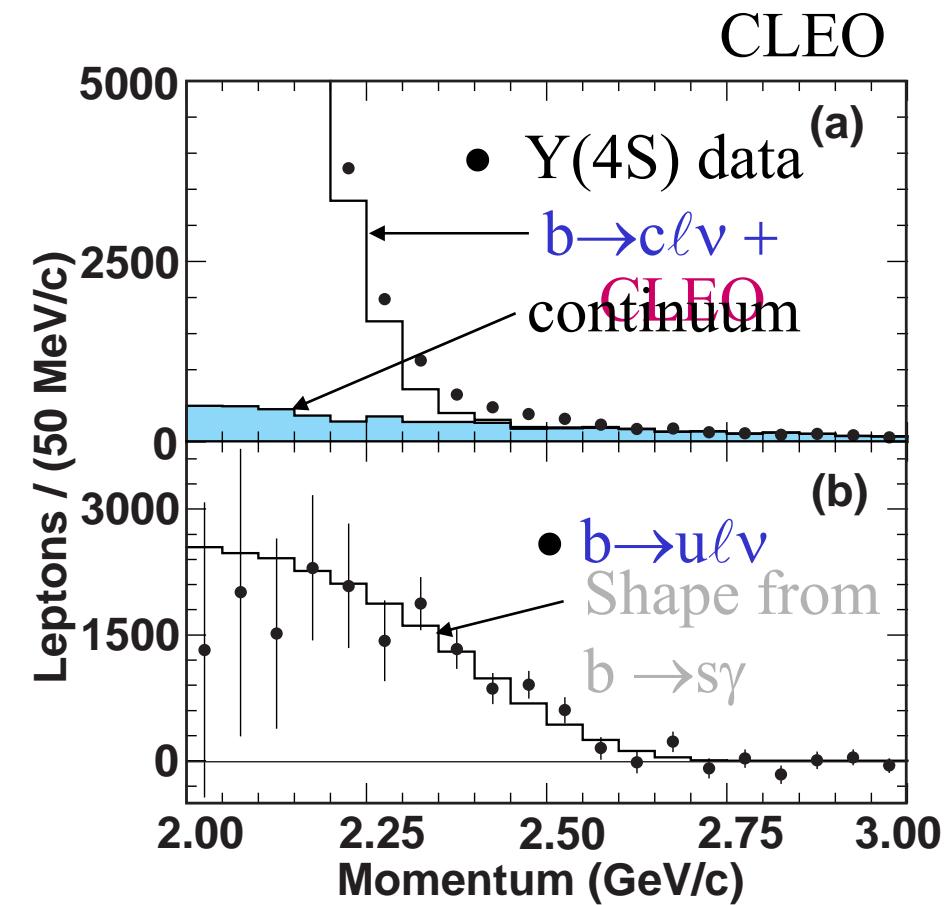
# The quest for $b \rightarrow ulv$ decays: inclusive approach

- The experimental challenge: single out the tiny  $b \rightarrow ulv$  component from the dominant  $b \rightarrow clv$
- Approaches taken:
  - Single out endpoint of lepton spectrum
  - $M_x$  below  $M_D$
  - More complex multivariate analysis, fitting explicitly for  $b \rightarrow clv$  contribution.
- All the suppression techniques introduce theoretical uncertainties that need to be addressed



## b $\rightarrow$ ulv from lepton endpoint

- This technique gave the first evidence for b $\rightarrow$ ulv decays
- Momentum cut reduced predictive power of OPE, but, up to  $1/m_b$  corrections, shape can be extrapolated from b $\rightarrow$ s $\gamma$  → use measured b $\rightarrow$ s $\gamma$  shape to reduce theoretical error



$$B(b \rightarrow u\ell\nu) = (1.77 \pm 0.29 \pm 0.38) \times 10^{-3}$$

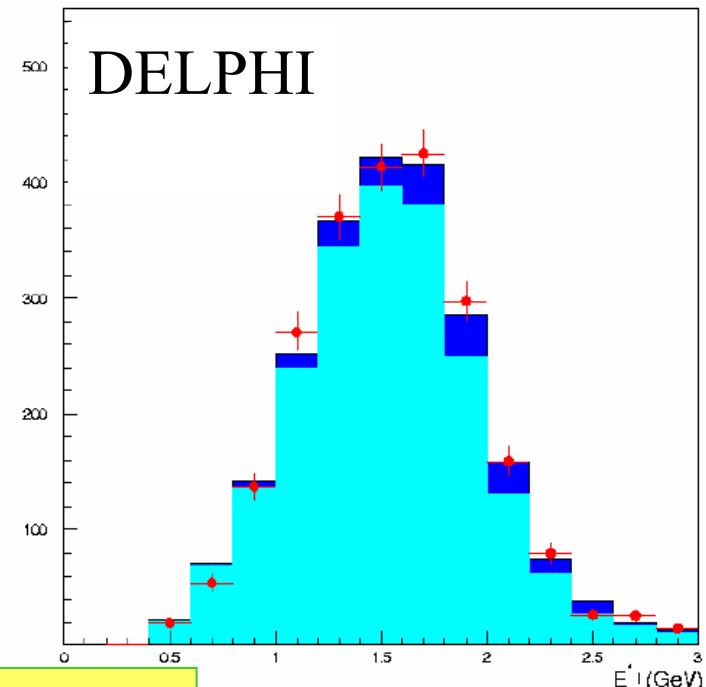
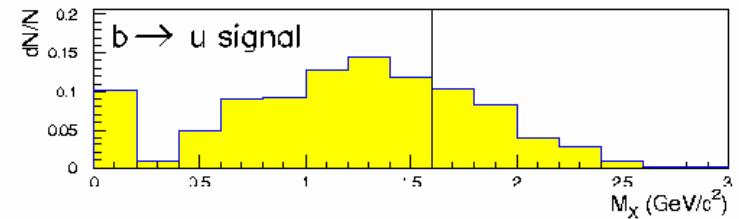


## b $\rightarrow$ u $\ell\nu$ using $M_x$ distribution

- ALEPH & DELPHI, OPAL select samples of charm-poor semileptonic decays with a large number of selection criteria
- Can they understand  $b \rightarrow c\ell\nu$  feedthrough < 1% ?

LEP combined results

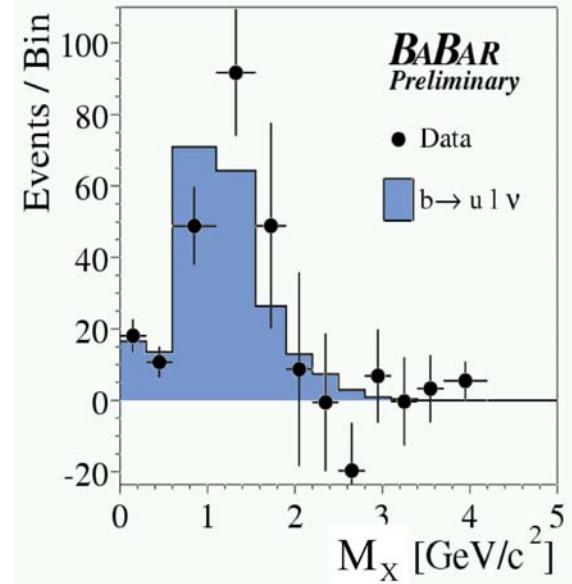
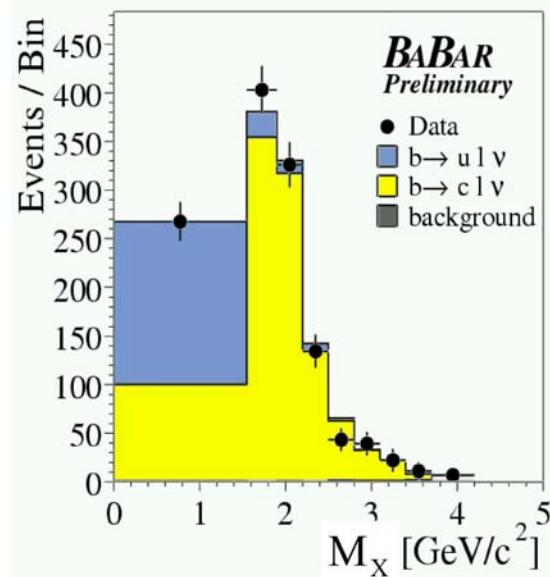
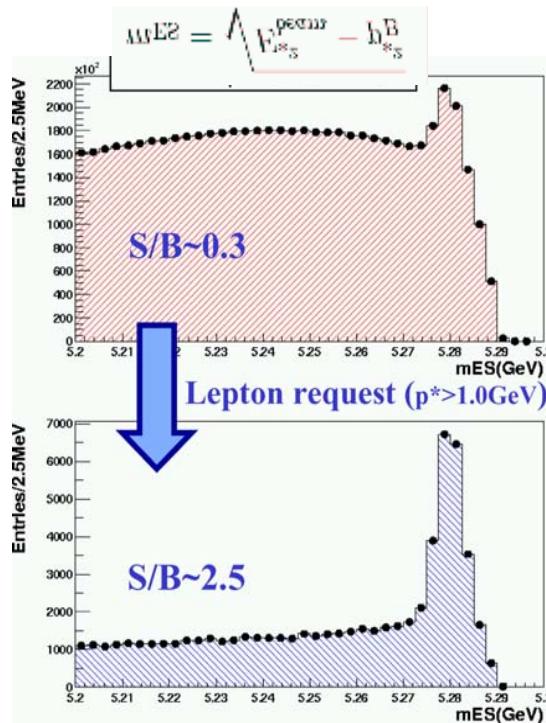
$$B(b \rightarrow u\ell\nu) = (1.71 \pm 0.31)_{\text{stat+det}} \pm 0.37 |_{b \rightarrow c} \pm 0.21 |_{b \rightarrow u} \times 10^{-3}$$





# $b \rightarrow u \ell \bar{\nu}$ from BaBar: study of $M_x$ with B tags

- Use fully reconstructed B tags

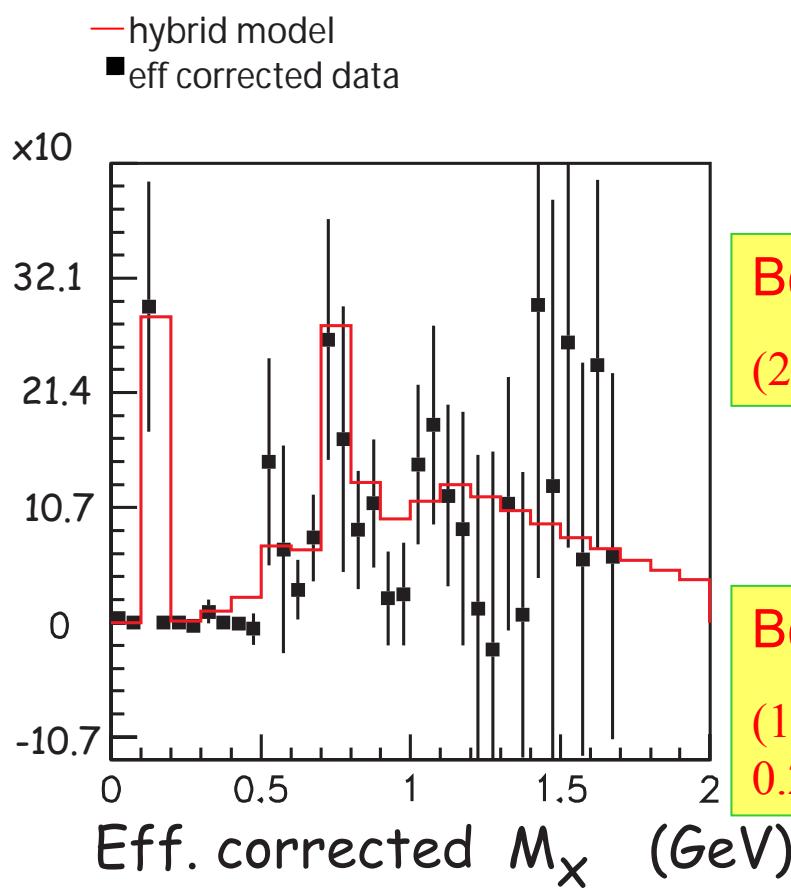


Preliminary

$$\mathcal{B}(B \rightarrow X_u \ell \bar{\nu}) = (2.14 \pm 0.29(\text{stat}) \pm 0.25(\text{syst}) \pm 0.37(\text{theo})) \times 10^{-3}$$



# Inclusive $b \rightarrow u \ell v$ from Belle



- Measure  $B(b \rightarrow u \ell v)$  using:
  - Pseudo full reconstruction of the  $\Upsilon(4S)$  [ $D^{(*)}\ell$  tags]

$$B(b \rightarrow u \ell v) =$$

$$(2.62 \pm 0.63|_{\text{stat}} \pm 0.23|_{\text{sys}} \pm 0.05|_{b \rightarrow c} \pm 0.41|_{b \rightarrow u}) \times 10^{-3}$$

- Advanced  $v$  reconstruction

$$B(b \rightarrow u \ell v) =$$

$$(1.64 \pm 0.14|_{\text{stat}} \pm 0.36|_{\text{sys}} \pm 0.28|_{b \rightarrow c} \pm 0.22|_{b \rightarrow u} \pm 0.29|_{\text{theory}}) \times 10^{-3}$$

preliminary



# Summary of inclusive $b \rightarrow u \ell \nu$ determinations

Experiment	Method	$BF(B \rightarrow u \ell \nu) (\times 10^3)$
CLEO	Endpoint(2.2-2.6 GeV)	$1.77 \pm 0.29 _{\text{exp}} \pm 0.38 _{\text{fu}}$
LEP(Vub WG ave)	$M_x$	$1.71 \pm 0.31 \pm 0.37 \pm 0.21$
BaBar	Endpoint(2.3-2.6)+ $f_u$ CLEO	$2.05 \pm 0.27 _{\text{exp}} \pm 0.46 _{\text{fu}}$
BaBar	$M_x$	$2.14 \pm 0.29 \pm 0.25 \pm 0.37$
BELLE	$D^{(*)} \ell$ tags	$2.62 \pm 0.63 \pm 0.23 \pm 0.05 \pm 0.41$
BELLE	Improved v reco	$1.64 \pm 0.14 \pm 0.36 \pm 0.28 \pm 0.22$

Additional theoretical uncertainties may need to be added (higher twist effects,  $M_x$  or other  $b \rightarrow u$  enhancing cuts)!



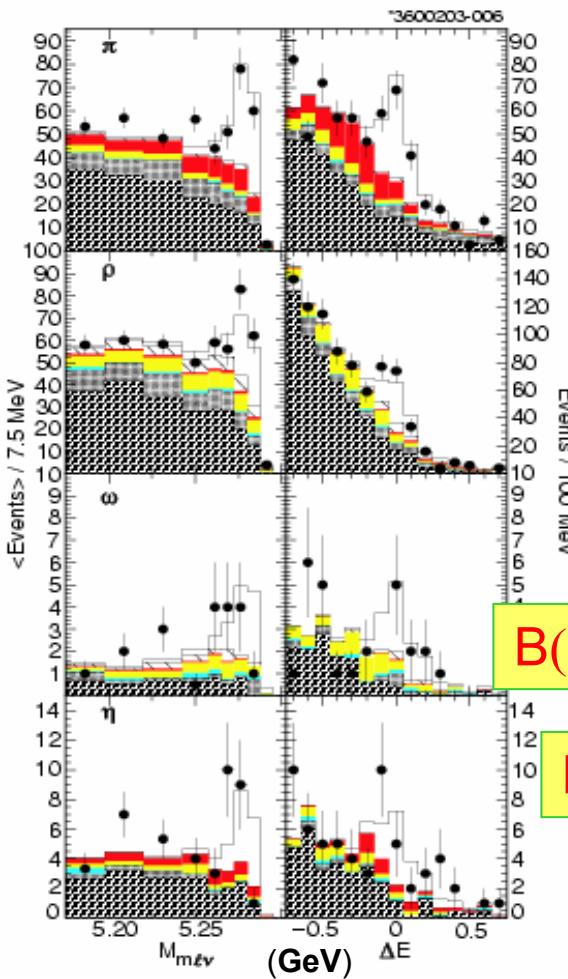
## Exclusive decays: $B \rightarrow \rho l \nu / \pi l \nu$

- Important to extract  $V_{ub}$ , especially when  $q^2$  dependence will be mapped precisely & more refined input from lattice calculations will be available [see talk by D. Becirevic,M.A.]
- No simple HQET effective theory available (light quark in the final state): evaluation of theoretical uncertainties difficult
- Study of  $q^2$  dependence and V/P ratio are very useful checks on theory [historically they have helped in ruling out quark model calculations of  $B \rightarrow \rho l \nu / \pi l \nu$ .]



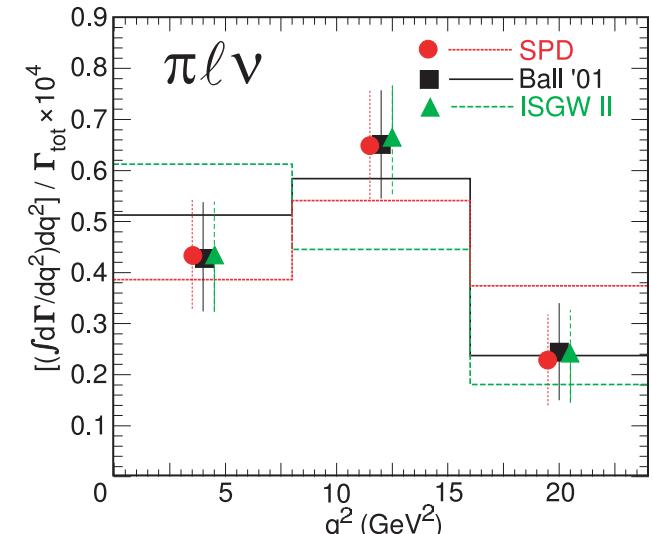
## B $\rightarrow$ p $\ell\nu$ / $\pi\ell\nu$ (CLEO)

- ◆ Use detector hermeticity to reconstruct  $\nu$
- ◆ CLEO finds rough  $q^2$  distribution



$$B(B^0 \rightarrow \pi^- \ell \nu) = (1.33 \pm 0.18|_{\text{stat}} \pm 0.11|_{\text{exp}} \pm 0.01|_{\text{ff,sig}} \pm 0.07|_{\text{ff,cf}}) \times 10^{-4}$$

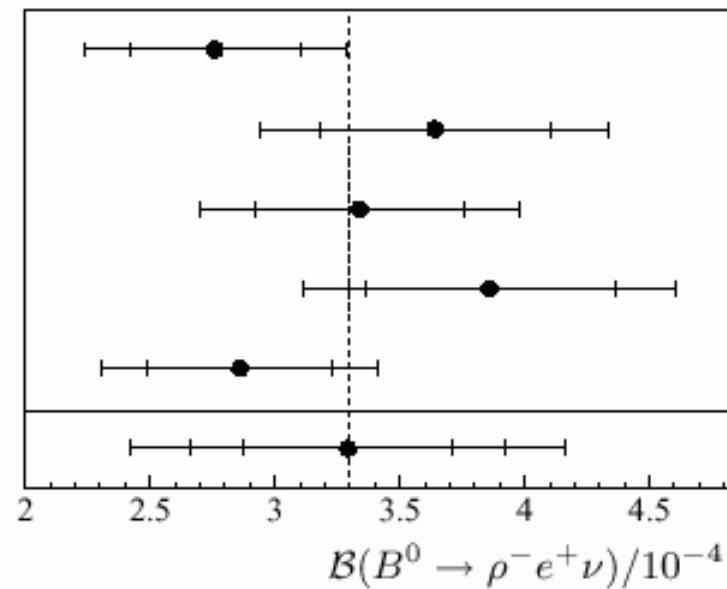
$$B(B^0 \rightarrow \rho^- \ell \nu) = (2.17 \pm 0.34|_{\text{stat}}^{+0.47} \pm 0.54|_{\text{sys}} \pm 0.41|_{\text{ff,sig}} \pm 0.01|_{\text{ff,cf}}) \times 10^{-4}$$





# B $\rightarrow$ $\rho l \nu$ BaBar

- Used 50.5 1/fb on-resonance and 8.7 1/fb 40 MeV below  $\Upsilon(4s)$  resonance
- Study 5 modes  $B \rightarrow H_u e \bar{\nu}$  where  $H_u = \rho^0, \rho^\pm, \omega, \pi^0, \pi^\pm$  in 2 lepton energy ranges:
  - LOLEP :  $2.0 < E_e < 2.3$  GeV (large  $b \rightarrow c$   $e \bar{\nu}$  backgrounds)
  - HILEP :  $2.3 < E_e < 2.7$  GeV (large continuum backgrounds)



ISGW2:  
 $2.76 \pm 0.34 \pm 0.40$

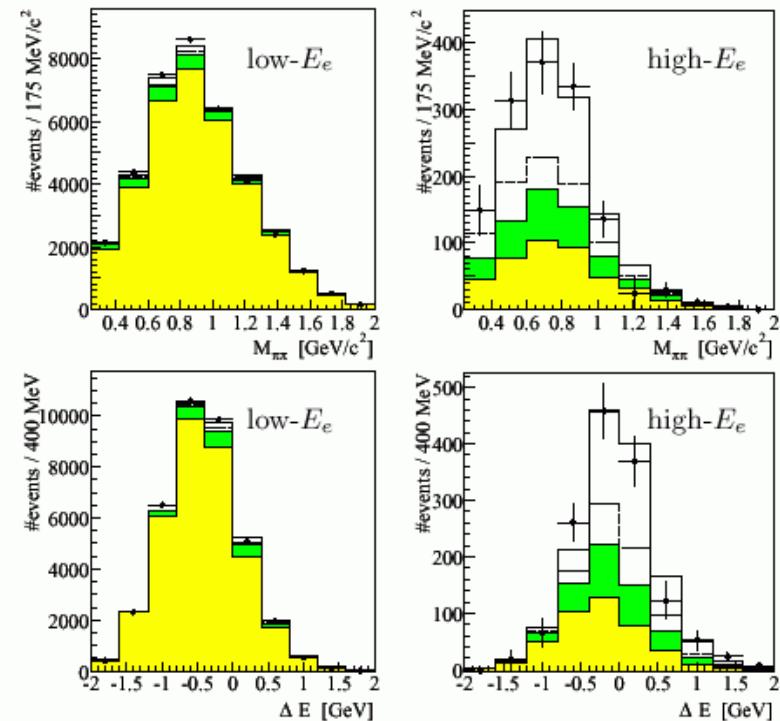
Beyer/Melikhov:  
 $3.64 \pm 0.46 \pm 0.52$

UKQCD:  
 $3.34 \pm 0.42 \pm 0.48$

LCSR:  
 $3.86 \pm 0.50 \pm 0.56$

Ligeti/Wise:  
 $2.86 \pm 0.37 \pm 0.41$

Combined:  
 $3.29 \pm 0.42 \pm 0.47 \pm 0.60$



BABAR PRELIMINARY



## Summary on $B \rightarrow \rho \ell \nu / \pi \ell \nu$

experiment	Decay mode	B.F ( $\times 10^{-4}$ )
CLEO	$B \rightarrow \pi \ell \nu$	$1.33 \pm 0.18 \pm 0.11 \pm 0.01 \pm 0.07$
CLEO	$B \rightarrow \rho \ell \nu$	$2.17 \pm 0.34 \begin{array}{l} +0.47 \\ -0.54 \end{array} \pm 0.41 \pm 0.01$
BaBar (prel)	$B \rightarrow \rho \ell \nu$	$3.29 \pm 0.42 \pm 0.47 \pm 0.60$



# Conclusions

- Experimental studies of  $b \rightarrow (c,u) \ell \nu$  have reached a great level of sophistication, but several key issues need still to be tackled
  - Full understanding of the composition of the semileptonic width
  - Precise determination of the theory parameters
  - Assessment of non-quantified theory errors [quark hadron duality, effects of higher twists...]
  - Reliable determination of the theoretical errors in exclusive  $B \rightarrow p \ell \nu / \pi \ell \nu$  transitions
- Large data sample at b-factories will allow to pursue analyses that are likely to have more controlled theoretical errors
- Charm data at threshold will help in the understanding of theoretical error [more on this later...]