

Semileptonic & Rare Charm Decays

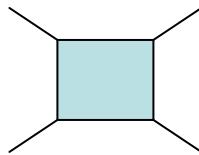
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Vanderbilt University
FPCP 2003, June 4

Rare Charm Decays

Potential FCNC Decays are Suppressed

Box and Penguin Diagrams are Smallish for Charm

No Top Quark in the loop



Short Distance

10^{-19}



$BR(D^0 \rightarrow \mu^+ \mu^-)$

10^{-16}



$BR(D^0 \rightarrow \gamma\gamma)$

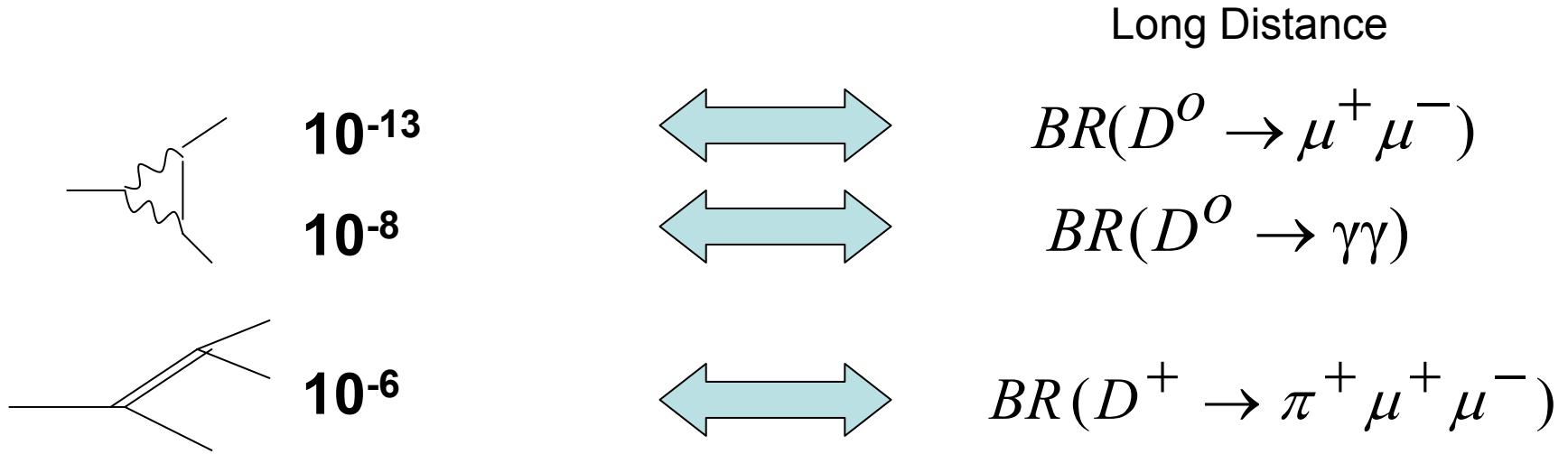
10^{-8}



$BR(D^+ \rightarrow \pi^+ \mu^+ \mu^-)$

Rare Charm Decays

Enhancement from Long Distance Effects



Room for New Physics

Even More room for decays:

$$\rightarrow \mu^+ \mu^+ X$$

$$\rightarrow X \mu^+ e^-$$

New Result from CDF $D^0 \rightarrow \mu^+ \mu^-$

Use D^* tagged D^0 's
(cut $\approx \pm 2.5\sigma_{\Delta M}$)

Use Similar Normalization Mode
Very Similar Kinematics
Keep cuts “same”

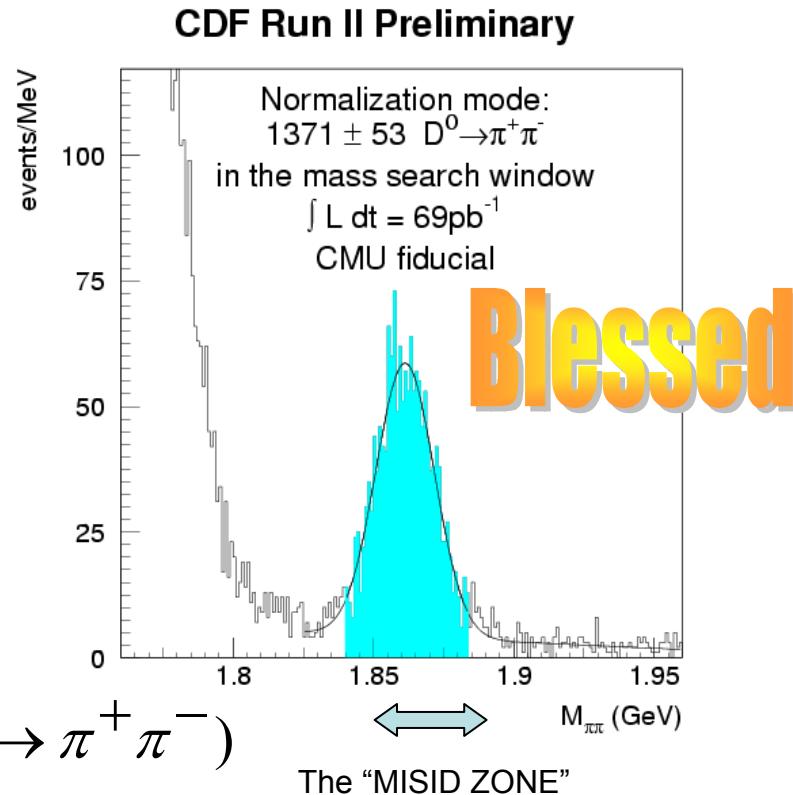
Need Anyway:
- Background from Normalization
 $\sim (\text{MISID})^2 = (0.013)^2$ or (1/5 ev.)

$$BR(D^0 \rightarrow \mu^+ \mu^-) \leq \frac{N_{RARE}}{N_{NORM}} \frac{eff_{NORM}}{eff_{RARE}} BR(D^0 \rightarrow \pi^+ \pi^-)$$

“Blind” Search

Optimal: $S / (1.5 + \sqrt{B})$

$$\pi\pi \quad \frac{\pi\pi_\mu + K_\mu \pi_\mu}{\text{Sideband} + (\text{MISID})^2}$$



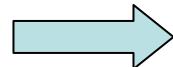
Back of the Envelope:

$$1.5E-3 (2.2/1371) = 2.4E-6$$

New Result from CDF $D^0 \rightarrow \mu^+ \mu^-$

- Expected background
 - 1.7 ± 0.7 events
 - Fake: 0.22 ± 0.2
 - Combinatorial: 1.5 ± 0.7

Open the Box



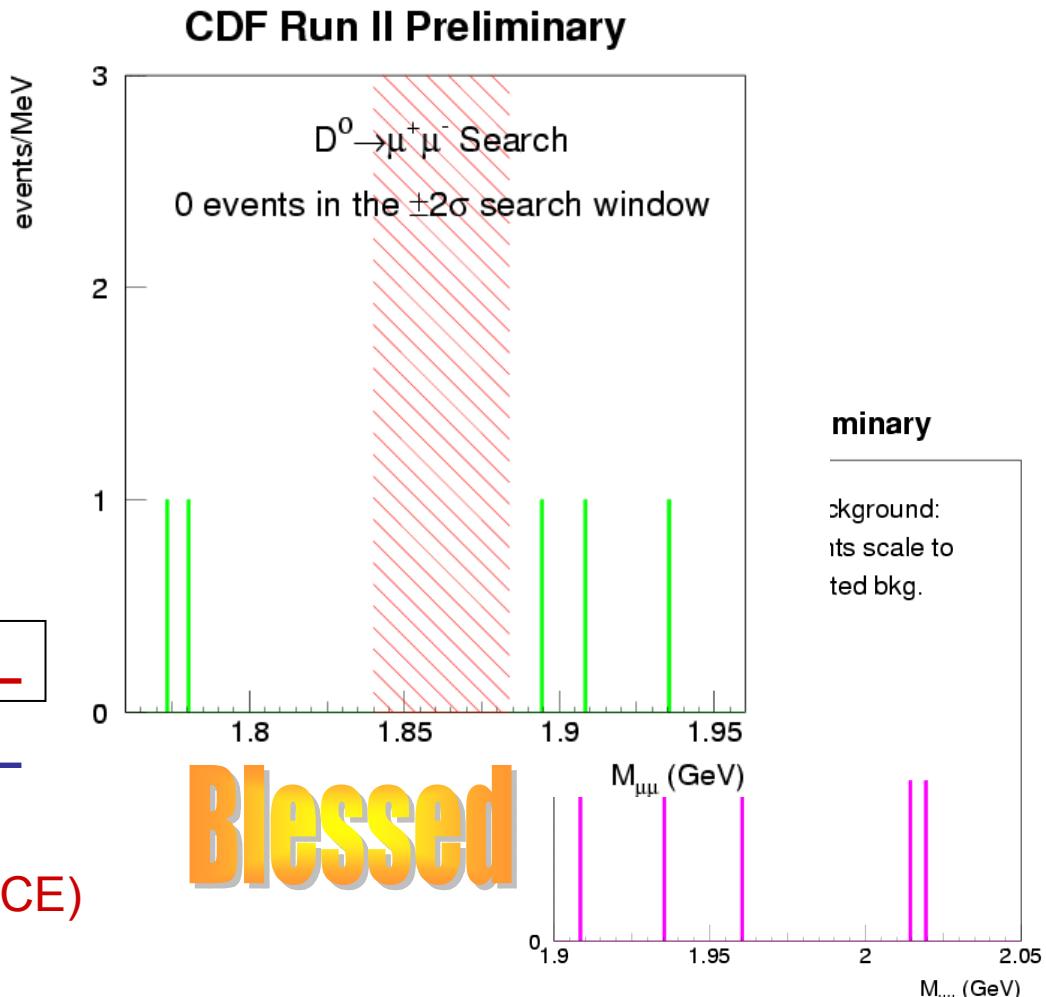
- 0 events in window
- New best limit

$\text{Br} < 2.4 \times 10^{-6}$ at 90% CL

$\text{Br} < 3.1 \times 10^{-6}$ at 95% CL

Previous Bests:

4.1×10^{-6} at 90% CL (BEATRICE)
 4.2×10^{-6} at 90% CL (E771)



Background Sideband
(Combinatorial Estimate)

New Result from CLEO $D^0 \rightarrow \gamma\gamma$

Form D^0 mass from 2 photons

(Cuts optimized on $D^0 \rightarrow \pi^0\pi^0$)

Mass must be within $2.5\sigma_M$ of $M(D^0)$

Veto candidate when extra photons form mass: $M(\pi^0) \pm 3\sigma_M$
 (reduces $\pi^0\pi^0$ bkgnd from 4 to 1)

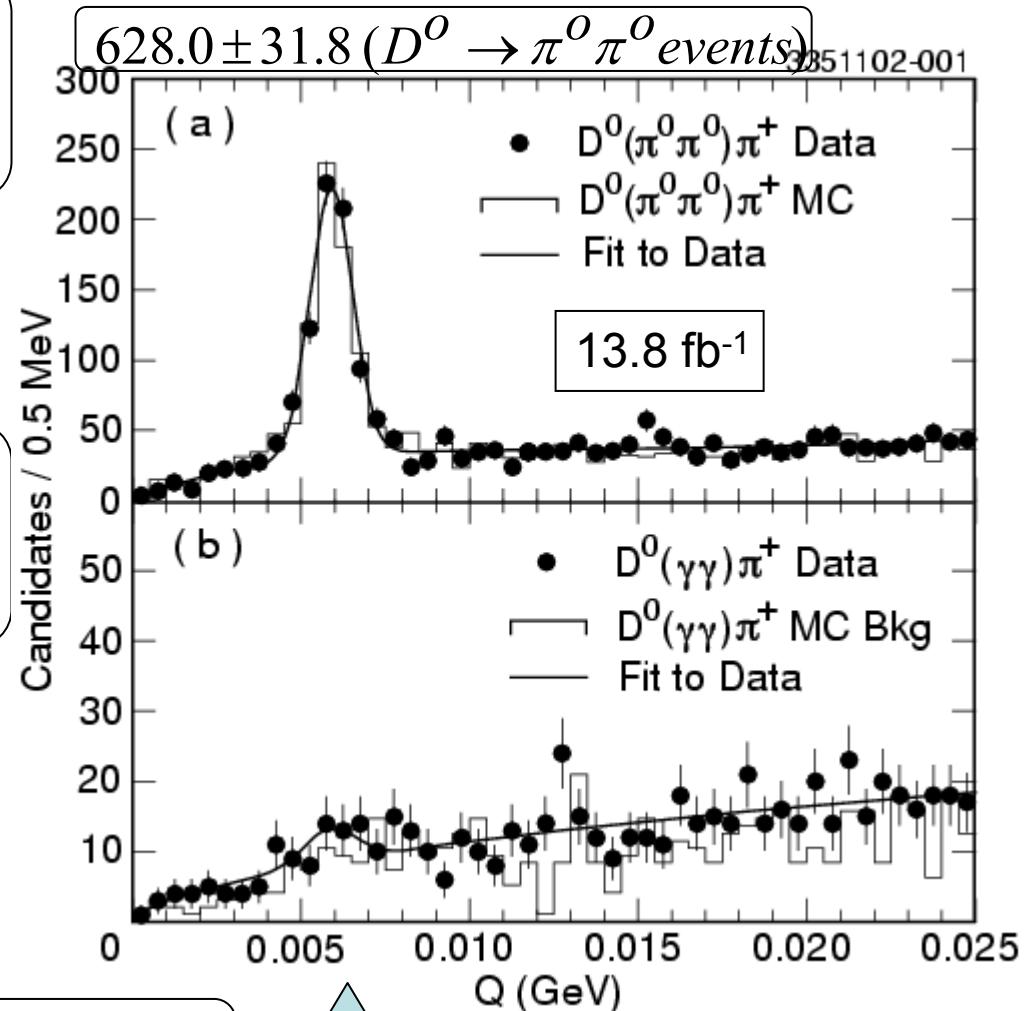
Find soft pion consistent with D momentum cuts and Particle ID

$$\text{Form } Q = M(D^{*+}) - M(D^0)$$

Fit data to Gaussian and threshold function

Gaussian width and center fixed from Monte Carlo

$19.2 \pm 9.3 (D^0 \rightarrow \gamma\gamma \text{ events})$



New Result from CLEO

$D^0 \rightarrow \gamma\gamma$

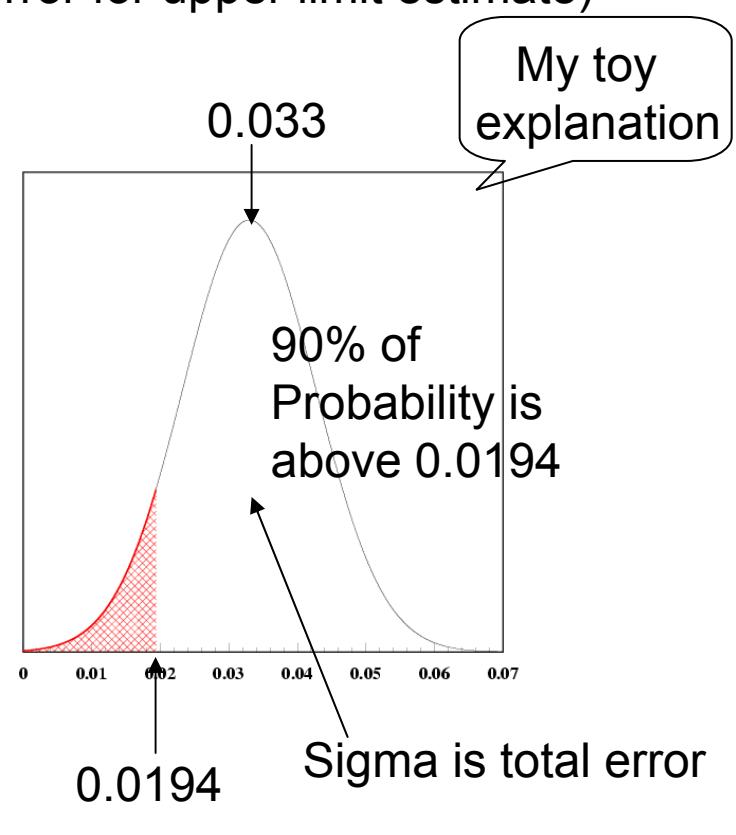
$$\frac{BR(D^0 \rightarrow \gamma\gamma)}{BR(D^0 \rightarrow \pi^0 \pi^0)} = \frac{N_{RARE}}{N_{NORM}} \frac{eff_{NORM}}{eff_{RARE}} = 0.0194 \pm 0.0094 \text{ (stat)}$$

Systematic error 13.1% from finding efficiencies, fits, MC stats, D selection, Event selection (added in quadrature with stat error for upper limit estimate)

$$\frac{BR(D^0 \rightarrow \gamma\gamma)}{BR(D^0 \rightarrow \pi^0 \pi^0)} < 0.033 \text{ @ 90% C.L.}$$

Using $BR(D^0 \rightarrow \pi^0 \pi^0) = (8.4 \pm 2.2) \times 10^{-4}$

$$BR(D^0 \rightarrow \gamma\gamma) < 2.9 \times 10^{-5} \text{ @ 90% C.L.}$$



Final Results from FOCUS

Look for 3 bodies with 2 muons

Cut Grid, based on vertexing, Particle ID

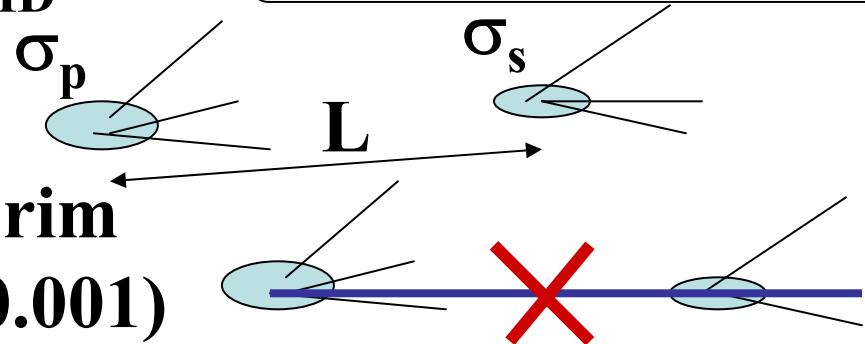
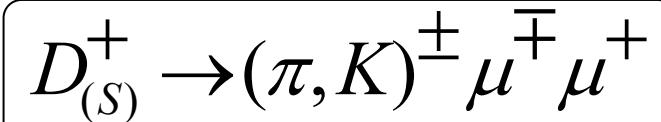
L/ σ – vary from >5-21

ISO1 – CL DK's in prim
(vary <0.1 – 0.001)

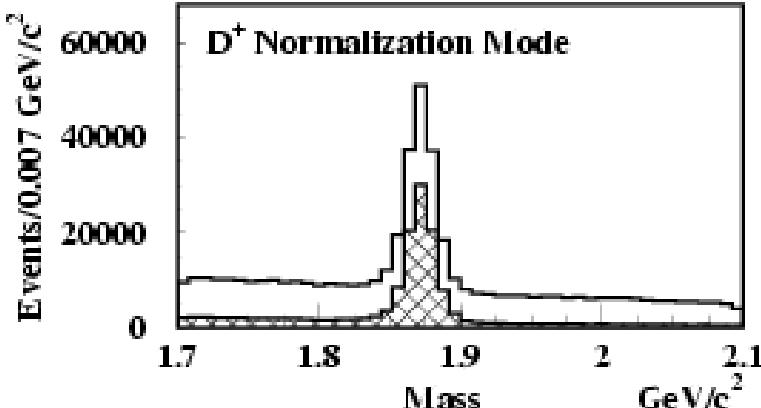
DCL – CL of DK vertex (>1 -- 4%)

MuCL – CL for Muon ID (>1 – 10%)

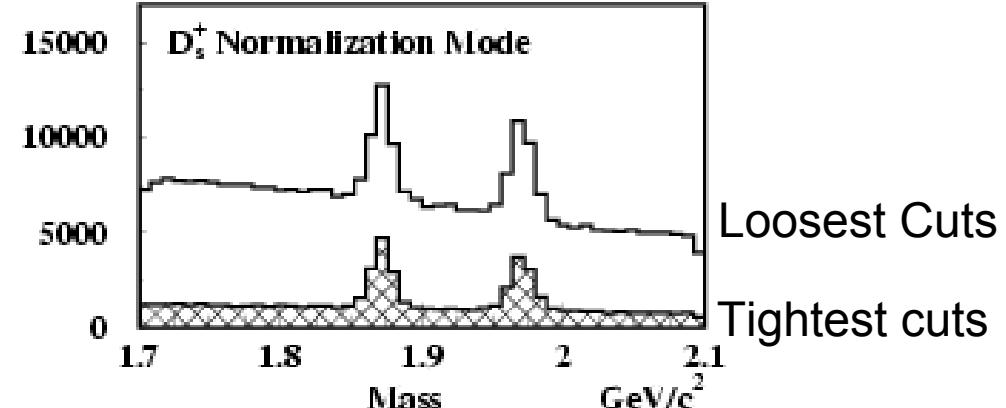
Cuts on P(μ) for μ 's, Cerenkov for π 's and K's



$K^- \pi^+ \pi^+$



$K^+ K^- \pi^+$



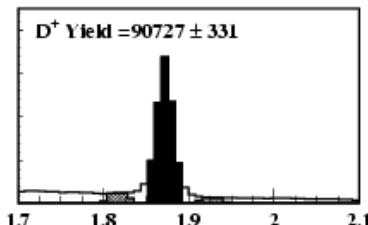
Final Results from FOCUS

Use Dual Bootstrap

$$D_{(S)}^+ \rightarrow (\pi, K)^+ \mu^+ \mu^+$$

- First Bootstrap sets cuts for optimal Sensitivity (Blind)
- Second Bootstrap calculates quoted Sensitivity and Branching Ratio

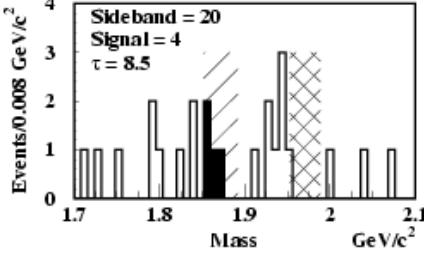
D^+
 $K\pi^+\pi^+$



Systematic Check
uses a single cut

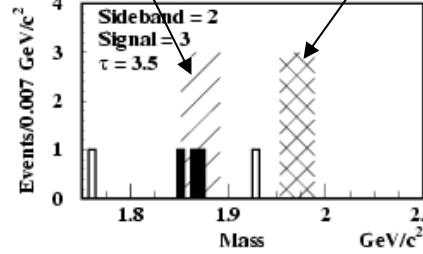
(makes better plots!)

$K^+\mu^+\mu^-$

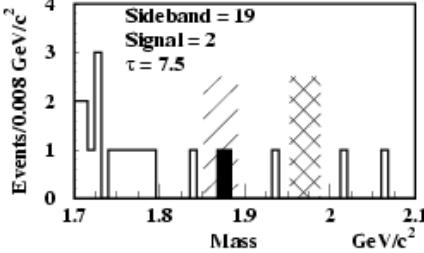


Signal Excluded

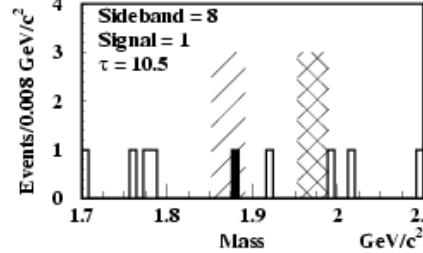
$K\mu^+\mu^+$



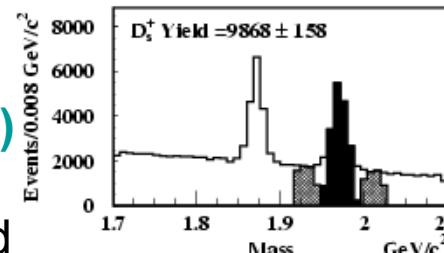
$\pi^+\mu^+\mu^-$



$\pi^-\mu^+\mu^+$

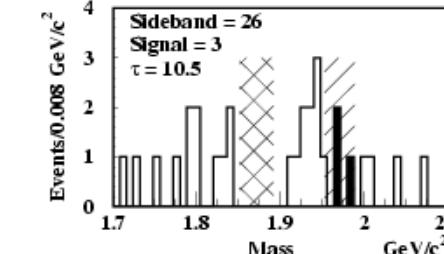


D_S^+
 $K^+\bar{K}^{\pi^+}$

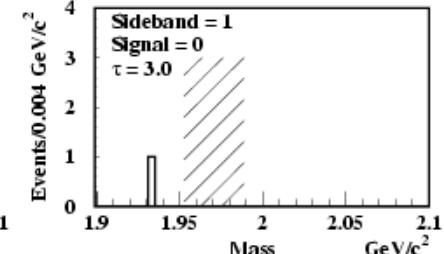


D+ Rare Decay Modes
from the single cut check

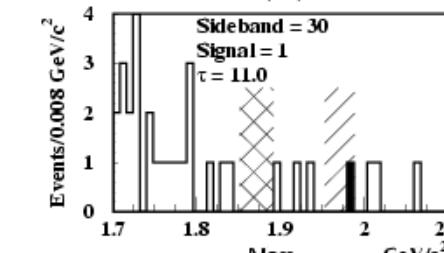
$K^+\mu^+\mu^-$



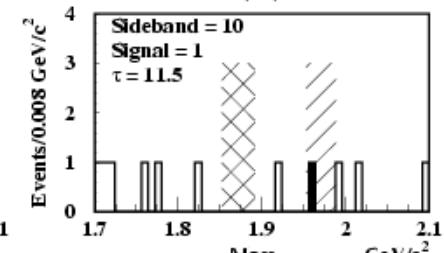
$K\mu^+\mu^+$



$\pi^+\mu^+\mu^-$



$\pi^-\mu^+\mu^+$



Final Results from FOCUS

$$D_{(S)}^+ \rightarrow (\pi, K)^\pm \mu^\mp \mu^\pm$$

Decay Mode	Dual Bootstrap	Sensitivity	Sys. Error	Result W/sys	Single Cut(w/sys)	Previous (E791)
$D^+ \Rightarrow K^+ \mu^+ \mu^-$	9.1×10^{-6}	7.5×10^{-6}	7.5%	9.2×10^{-6}	12×10^{-6}	44×10^{-6}
$D^+ \Rightarrow K^- \mu^+ \mu^+$	13×10^{-6}	4.8×10^{-6}	7.5%	13×10^{-6}	12×10^{-6}	120×10^{-6}
$D^+ \Rightarrow \pi^+ \mu^+ \mu^-$	8.8×10^{-6}	7.6×10^{-6}	7.5%	8.8×10^{-6}	7.4×10^{-6}	15×10^{-6}
$D^+ \Rightarrow \pi^- \mu^+ \mu^+$	4.9×10^{-6}	5.6×10^{-6}	7.5%	4.8×10^{-6}	5.2×10^{-6}	17×10^{-6}
$D_s^+ \Rightarrow K^+ \mu^+ \mu^-$	3.3×10^{-5}	3.3×10^{-5}	27.5%	3.6×10^{-5}	3.8×10^{-5}	1.4×10^{-4}
$D_s^+ \Rightarrow K^- \mu^+ \mu^+$	1.3×10^{-5}	2.1×10^{-5}	27.5%	1.3×10^{-5}	2.0×10^{-5}	1.8×10^{-4}
$D_s^+ \Rightarrow \pi^+ \mu^+ \mu^-$	2.4×10^{-5}	3.1×10^{-5}	27.5%	2.6×10^{-5}	1.8×10^{-5}	1.4×10^{-4}
$D_s^+ \Rightarrow \pi^- \mu^+ \mu^+$	2.6×10^{-5}	2.3×10^{-5}	27.5%	2.9×10^{-5}	2.2×10^{-5}	0.8×10^{-4}

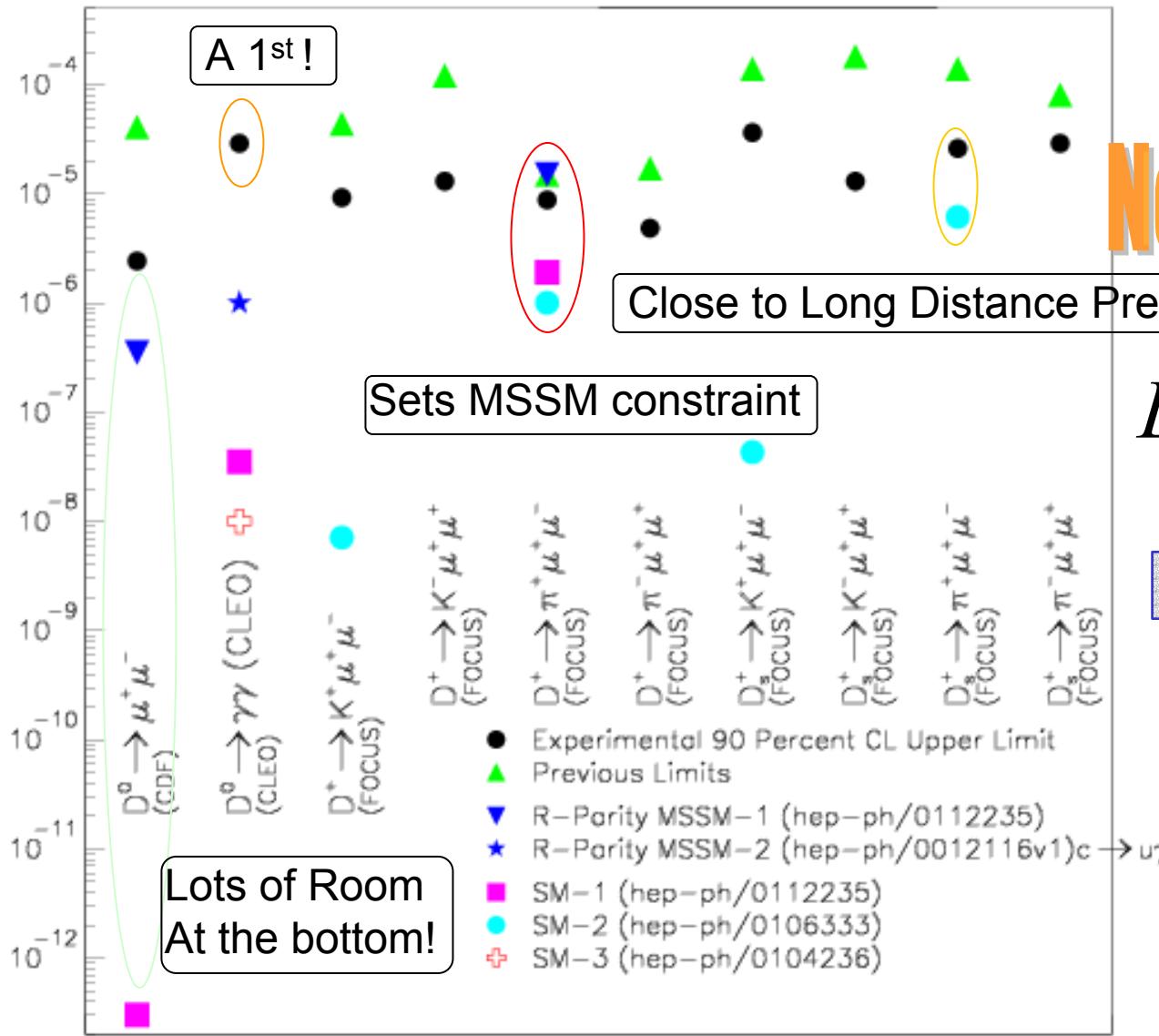
(E687)

Dominated by PDG rate to normalizing mode

Rare Decay Round-Up

Still Room for
New Physics

No Lower Limits



$D^0 \rightarrow \gamma\gamma$ A 1st!

MSSM Constraint

Closing in on
Long range
SM predictions

Semileptonic Charm Decays

$D^+ \rightarrow (K^- \pi^+) \mu^+ \nu$ (Interference)

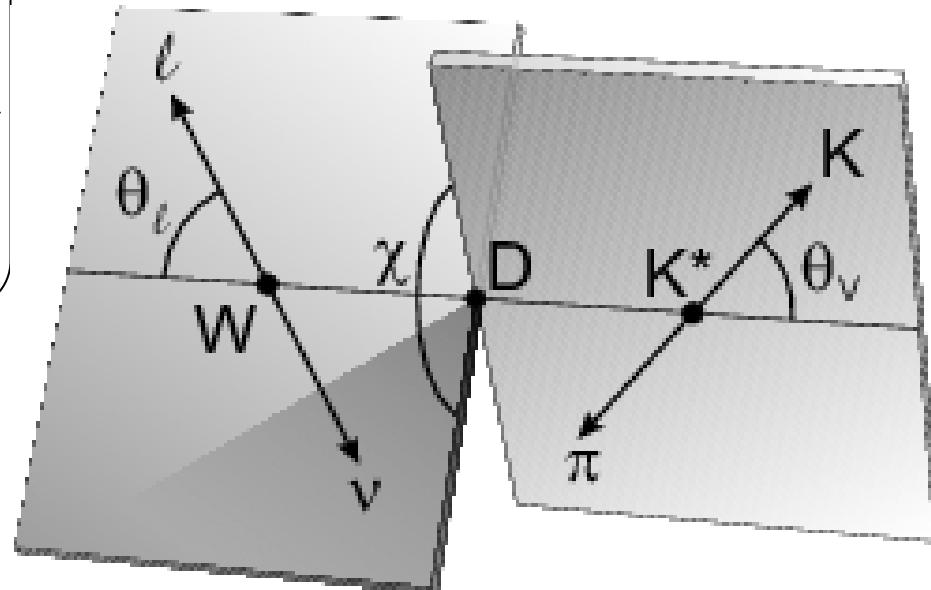
$$\frac{\Gamma(D^+ \rightarrow \bar{K}^{*0} \mu^+ \nu)}{\Gamma(D^+ \rightarrow K^- \pi^+ \pi^+)}, \frac{\Gamma(D_s^+ \rightarrow \phi \mu^+ \nu)}{\Gamma(D_s^+ \rightarrow \phi \pi^+)}$$

$D^+ \rightarrow \bar{K}^{*0} \mu^+ \nu$ (Form Factors)

$\Lambda_c^+ \rightarrow \Lambda^0 e^+ \nu$ (Form Factors, M_{Pole})

$\Lambda_c^+ \rightarrow \Lambda^0 e^+ \nu$ (CP Asymmetry)

More than just CKM measurement tools...



Simple Equation:

(D decay, No form factors, V decays to spin 0 particles)

$$\frac{d^2\Gamma}{d \cos \theta_V d \cos \theta_\ell} \propto \{(1 + \cos \theta_\ell)^2 \Gamma_+ + (1 - \cos \theta_\ell)^2 \Gamma_-\} \sin^2 \theta_V + 4 \sin^2 \theta_\ell \cos^2 \theta_V \Gamma_0$$

Neutrino is left handed

V products spinless

Prefers W spin along muon,e

Prefer $L_Z=0$

Gets Complicated...

Scalar Resonance?

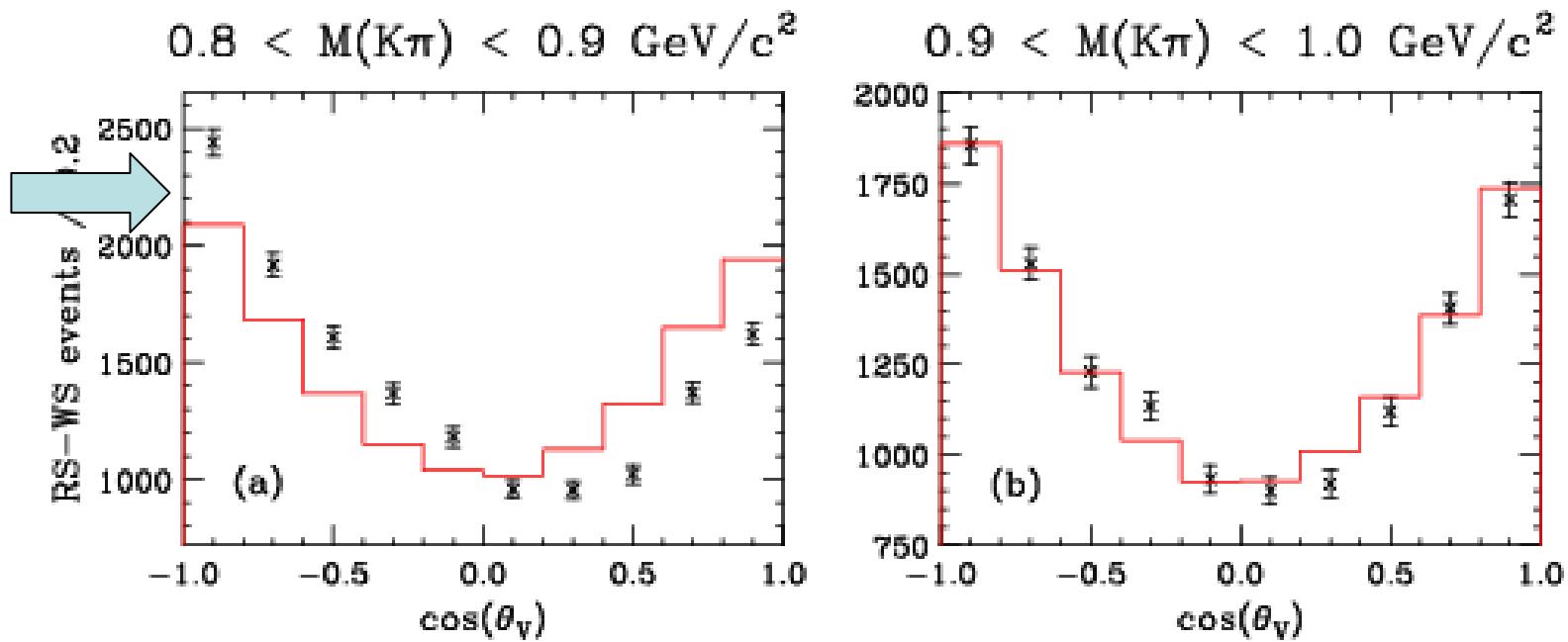
Form Factors

Baryons (spin 1/2)

CP?

FOCUS saw discrepancies in the data

yikes!



$$D^+ \rightarrow \bar{K}^{*0} \mu^+ \nu$$

(Did NOT obey)

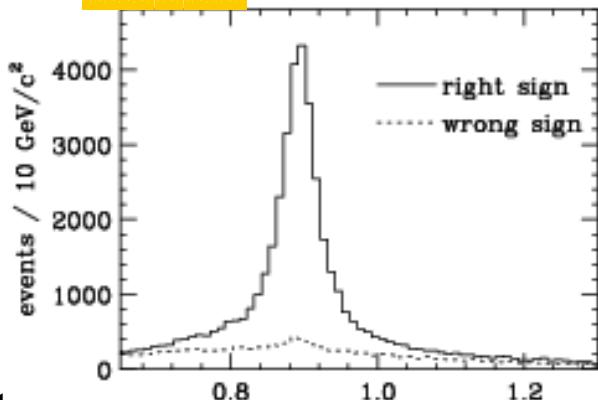
$$\frac{d^5\Gamma}{dm_{k\pi} dq^2 d\cos\theta_V d\cos\theta_\ell d\chi} \propto \left\{ \begin{array}{l} \sin\theta_V(1+\cos\theta_\ell)e^{i\chi}B_{K^{*0}}H_+(q^2) \\ -\sin\theta_V(1-\cos\theta_\ell)e^{-i\chi}B_{K^{*0}}H_-(q^2) \\ -2\cos\theta_V\sin\theta_\ell B_{K^{*0}}H_0(q^2) \end{array} \right\}$$

Phys.Lett.B535:43-51, 2002

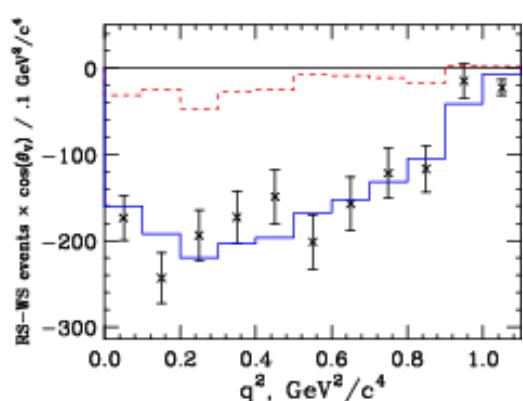
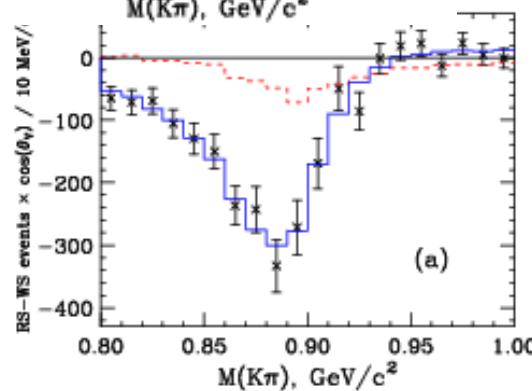
hep-ex/0203031

FOCUS added a term, things got better

With a **Clean** $K\pi\mu\nu$ signal



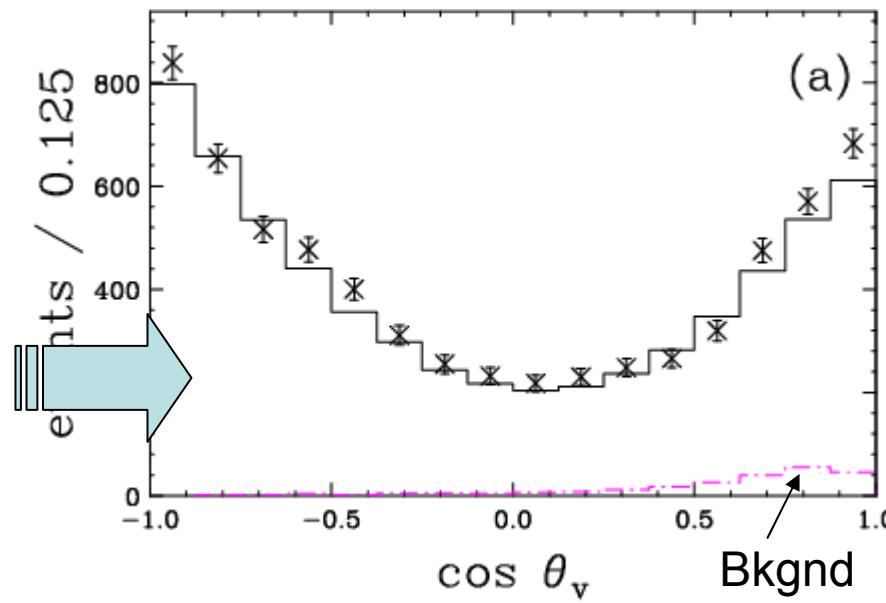
The data (error bars) preferred the L=0 ansatz (solid) over no extra term (dashed)



And the distributions were ready for fitting

$$\frac{d^5 \Gamma}{dm_{K\pi} dq^2 d \cos \theta_V d \cos \theta_\ell d \chi} \propto \left\{ \begin{array}{l} (1 + \cos \theta_\ell) \sin \theta_V e^{i\chi} B_{K^{*0}} H_+(q^2) \\ -(1 - \cos \theta_\ell) \sin \theta_V e^{-i\chi} B_{K^{*0}} H_-(q^2) \\ -2 \sin \theta_\ell (\cos \theta_V B_{K^{*0}} + Ae^{i\delta}) H_0(q^2) \end{array} \right\}^2$$

L=0 ansatz



FOCUS BR Measurements

$$\frac{\Gamma(D^+ \rightarrow \bar{K}^{*0} \mu^+ \nu)}{\Gamma(D^+ \rightarrow K^- \pi^+ \pi^+)}, \frac{\Gamma(D_s^+ \rightarrow \phi \mu^+ \nu)}{\Gamma(D_s^+ \rightarrow \phi \pi^+)}$$

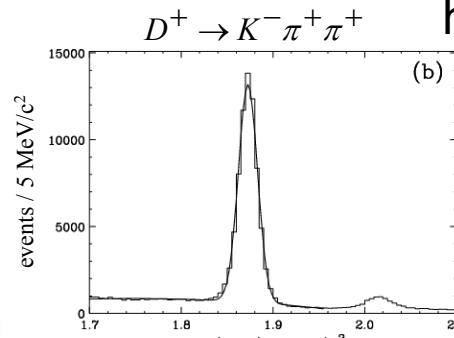
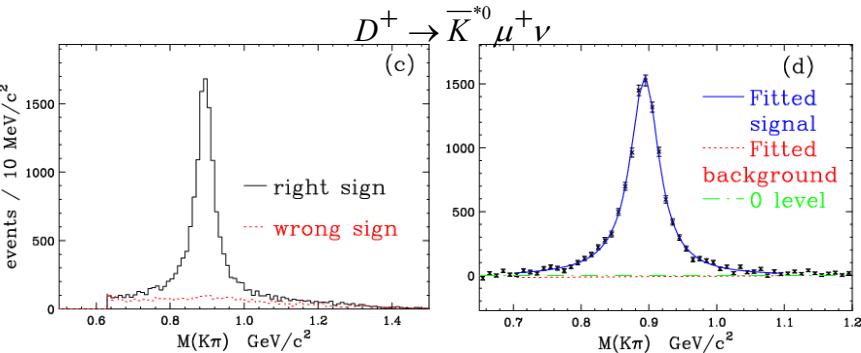
Cuts similar to rare search:

ISO1 → ISO2 – No unused tracks consistent with charm vertex (CL < 0.1%)

OoM – Charm vertex outside of target and silicon by $3\sigma_{\text{Vertex}}$

$$M(K^- \pi^+ \mu^+ \{\nu\}) - M(K^- \mu^+ \{\nu\}) > 0.18 \text{ GeV}/c^2 \text{ (cuts } D^{*+} \rightarrow D^0 \pi^+)$$

$D^+ \rightarrow \bar{K}^{*0} \mu^+ \nu$ Includes S-wave interference



Phys.Lett.B540:25-32, 2002
hep-ex/0206013

$$\frac{\Gamma(D^+ \rightarrow \bar{K}^{*0} \mu^+ \nu)}{\Gamma(D^+ \rightarrow K^- \pi^+ \pi^+)} = 0.602 \pm 0.010(\text{stat}) \pm 0.021(\text{sys})$$

Systematic errors :

expressed as a fraction of σ_{stat}

for D^+ (D_s^+):

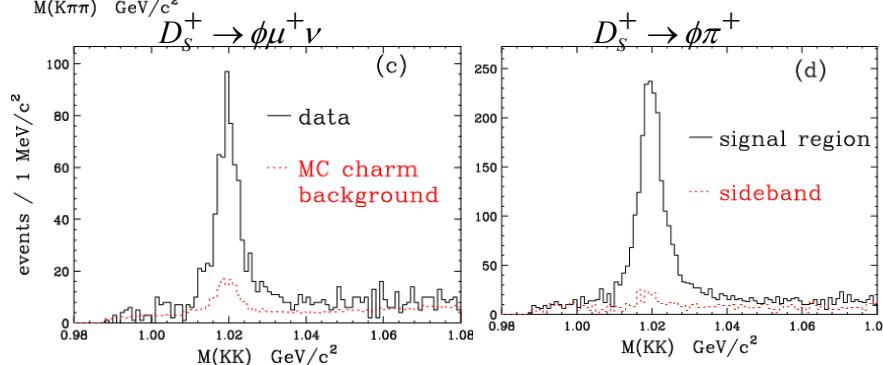
Vary Cuts ⇒ 0.71, (1.06)

Splitting Samples ⇒ 1.57, (1.12)

Vary fit (Bk, ff) ⇒ 1.57, (0.94)

Total (quadrature) ⇒ 2.2, (1.5)

(add in if > 1)



$$\frac{\Gamma(D_s^+ \rightarrow \phi \mu^+ \nu)}{\Gamma(D_s^+ \rightarrow \phi \pi^+)} = 0.54 \pm 0.033(\text{stat}) \pm 0.048(\text{sys})$$

FOCUS Form Factors

$$D^+ \rightarrow \bar{K}^{*0} \mu^+ \nu$$

$$H_{\pm}(q^2) = (M_D + m_{K\pi}) A_1(q^2) \mp 2 \frac{M_D K}{M_D + m_{K\pi}} V(q^2) \quad H_t(q^2) \text{ has } m_\mu^2 \text{ factor, set } = 0$$

$$H_0(q^2) = \frac{1}{2m_{K\pi}\sqrt{q^2}} \left[(M_D^2 - m_{K\pi}^2 - q^2)(M_D + m_{K\pi}) A_1(q^2) - 4 \frac{M_D^2 K^2}{M_D + m_{K\pi}} A_2(q^2) \right]$$

$$A_i(q^2) = \frac{A_i(0)}{1 - q^2/M_A^2}, (M_A = 2.5 \text{ GeV}/c^2) \quad V(q^2) = \frac{V(0)}{1 - q^2/M_V^2}, (M_V = 2.1 \text{ GeV}/c^2)$$

Fit to $r_v = \frac{V(0)}{A_1(0)}$ $r_2 = \frac{A_2(0)}{A_1(0)}$ and S-wave parameters, A and δ

Technique: (common – vary **generated** parameters in Montecarlo by using agreement with **reconstructed** distributions and data)

➡ Pioneered by D.M. Schmidt for E691 $K^* \nu e$ analysis: NIM A 328 (1993)

1st find S-wave with PDG r's,

3 bins in $\cos\theta_V$, 3 in $\cos\theta_\ell$, 3 in χ and 4 in $m_{K\pi}$

then fit for r's

S-wave term
Breaks symmetry

5 bins in $\cos\theta_V$, 5 in $\cos\theta_\ell$, 3 in $|\chi|$ and 3 in q^2/q_{\max}^2

S-wave term and
r's essentially
decouple

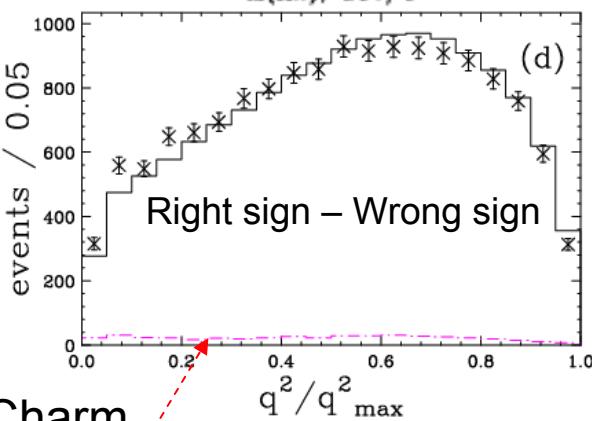
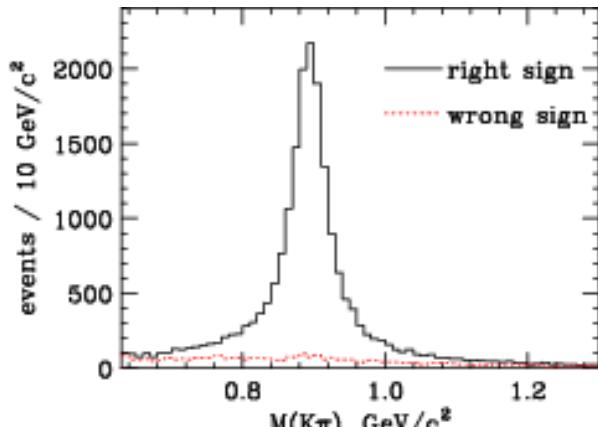
FOCUS Form Factors

$$D^+ \rightarrow \bar{K}^{*0} \mu^+ \nu$$

Cuts similar to previous, some change to get uniform acceptance, one extra

OoM – Charm vertex outside of target and silicon by $1\sigma_{\text{Vertex}}$

Cut on $q^2 < 0.2 \text{ GeV}^2/c^2$ \iff r's are flat, feeling m_μ ? Goodness of fit issue



Charm
Background

Systematic Checks

S-wave – varied cuts

35 fits – Sample Variance

Form Factor (3 sources)

- 1) Varied Cuts
- 2) Split sample

P_D , $D\bar{D}$, $m_{K\pi}$ ($0.9 \text{ GeV} / c^2$)

3) Vary MC input

Charm Backgrounds

$$-2 < \frac{A_3(0)}{A_1(0)} < 2$$

$$A = 0.330 \pm 0.022 \pm 0.015$$

$$\delta = 0.68 \pm 0.07 \pm 0.05$$

$\pm (\text{stat}) \pm (\text{sys})$

$$r_V = 1.504 \pm 0.057 \pm 0.039$$

$$r2 = 0.875 \pm 0.049 \pm 0.064$$

Results:

Phys.Lett.B544:89-96, 2002
hep-ex/0207049

CLEO Form Factors and CP $\Lambda_c^+ \rightarrow \Lambda^0 e^+ \nu$

Spin $\frac{1}{2}$ Λ baryon adds a new wrinkle...

$$\left| \frac{1}{2} 1 \right\rangle, \left| \frac{1}{2} \cancel{-1} \right\rangle, \left| \frac{1}{2} 0 \right\rangle, \left| \cancel{-1} \frac{1}{2} \right\rangle, \left| -\frac{1}{2} -1 \right\rangle, \left| -\frac{1}{2} 0 \right\rangle$$

Körner and Krämer use supplementary definitions for X and the lepton angle

$$\frac{d^4 \Gamma}{dq^2 d \cos \theta_\Lambda d \cos \theta_W d \chi} \propto$$

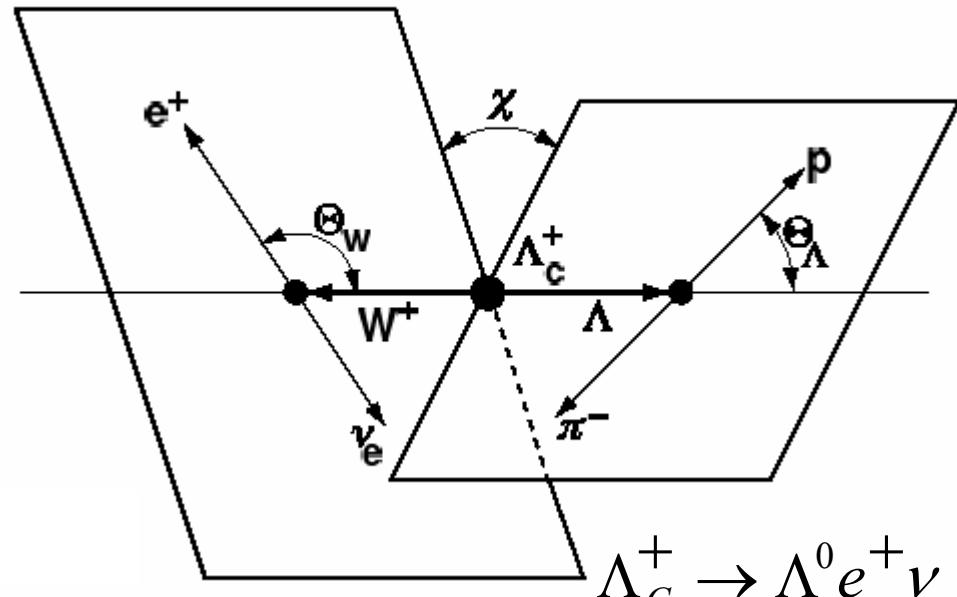
$$\begin{aligned} & \{|H_{\frac{1}{2}1}\rangle|^2 \left(\frac{3}{8}(1 \pm \cos \theta_W)^2(1 + \alpha_\Lambda \cos \theta_\Lambda)\right) + \\ & |H_{\frac{1}{2}-1}\rangle|^2 \left(\frac{3}{8}(1 \mp \cos \theta_W)^2(1 - \alpha_\Lambda \cos \theta_\Lambda)\right) + \\ & |H_{\frac{1}{2}0}\rangle|^2 \frac{3}{4} \sin^2 \theta_W (1 + \alpha_\Lambda \cos \theta_\Lambda) + \\ & |H_{-\frac{1}{2}0}\rangle|^2 \frac{3}{4} \sin^2 \theta_W (1 - \alpha_\Lambda \cos \theta_\Lambda) + \\ & \text{Re}(H_{\frac{1}{2}0}\rangle H_{\frac{1}{2}1}^*) \alpha_\Lambda \cos \chi \sin \theta_W \sin \theta_\Lambda \frac{3}{2\sqrt{2}} (1 \pm \cos \theta_W) + \\ & \text{Re}(H_{\frac{1}{2}0}\rangle H_{\frac{1}{2}-1}^*) \alpha_\Lambda \cos \chi \sin \theta_W \sin \theta_\Lambda \frac{3}{2\sqrt{2}} (1 \mp \cos \theta_W) \} \end{aligned}$$

Integrate over variables and look at asymmetries:

(other choices possible)

$$\frac{d^2 \Gamma}{dq^2 d \cos \theta_\Lambda} \propto (1 + \alpha_{\Lambda_c} \alpha_\Lambda \cos \theta_\Lambda)$$

(no sign change for particle and anti-particle)



One pole mass describes the decay

$$f(q^2) = \frac{f(q_{Max}^2)}{1 - q^2/M_{Pole}^2} (1 - q^2/M_{Pole}^2)^2$$

Helicity H's made from 2 form factors:

$$\text{expect } |f_1(q^2)| > |f_2(q^2)|$$

spin is *sticky* ($\Lambda_B \rightarrow \Lambda_C, f_2 \approx 0$)

CLEO Form Factors and CP $\Lambda_C^+ \rightarrow \Lambda^0 e^+ \nu$

13.4 fb⁻¹ from CLEO II and II.5

Look for Λe^+ pairs where $\Lambda \rightarrow p \pi^-$

$P(\nu) = ?$ Find $P(\Lambda_C)$ direction

- Event thrust axis for direction
- Try to close kinematics:

$$\vec{P}_{\Lambda_C}^2 = (\vec{P}_\Lambda + \vec{P}_e + \vec{P}_\nu)^2$$

(use fragmentation to break ambg)

Technique:

(again the Schmidt meth)

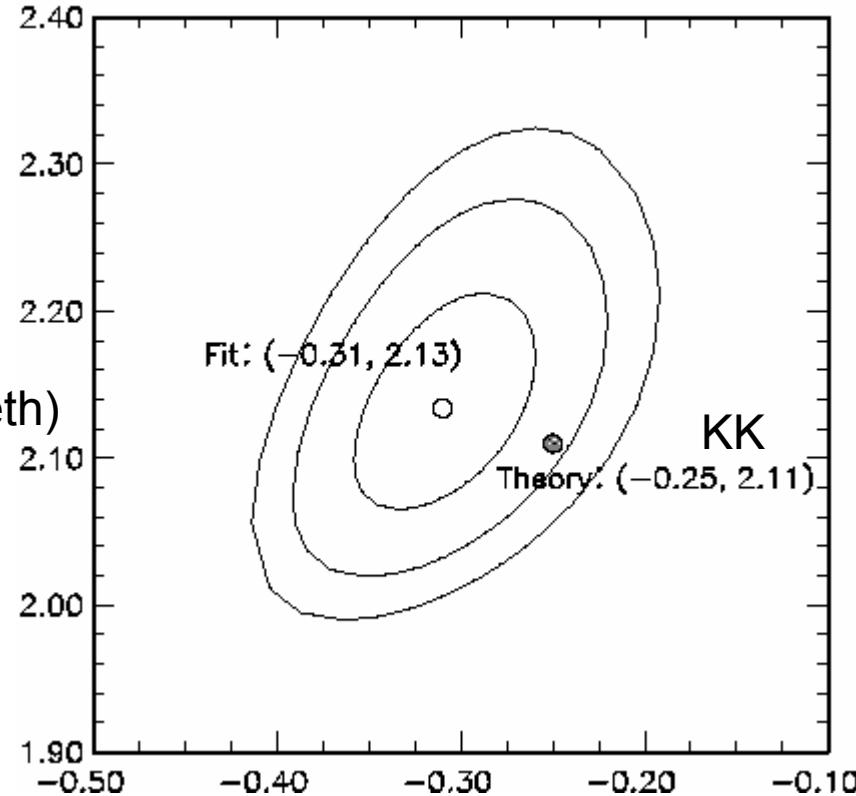
4-D r and pole mass
2-D asymmetry

Systematics:

- Background Normalizations
- Kinematic Closing
- Fitting simulation
- Efficiencies

Results:

(To be sent to PRL)



$$R = f_2 / f_1 = -0.31 \pm 0.05(stat) \pm 0.04(sys)$$

$$M_{pole} = 2.13 \pm 0.07(stat) \pm 0.10(sys) \text{ GeV}/c^2$$

CLEO Form Factors and CP $\Lambda_c^+ \rightarrow \Lambda^0 e^+ \nu_e$

Mikhail Dubrovin

CLEO

8

FF & Search for CPV in $\Lambda_c^+ \rightarrow \Lambda e^+ \nu_e$ (cont.)

- Distributions of four kinematic variables and (unbinned) fit projections \Rightarrow
- Integrating the dif. rate over χ and $\cos\theta_W$

$$\frac{d\Gamma}{dq^2 d\cos\theta_\Lambda} \propto (1 + \alpha_{\Lambda_c^+} \alpha_\Lambda \cos\theta_\Lambda)$$

- Extract from the fit
the decay asymmetry parameter:

$$\alpha_{\Lambda_c^+} = -0.85 \pm 0.03_{\text{stat}} \pm 0.02_{\text{syst}} \\ @ <q^2> = 0.67 \text{ (Gev/c}^2)$$

for world average $\alpha_\Lambda = 0.642 \pm 0.013$

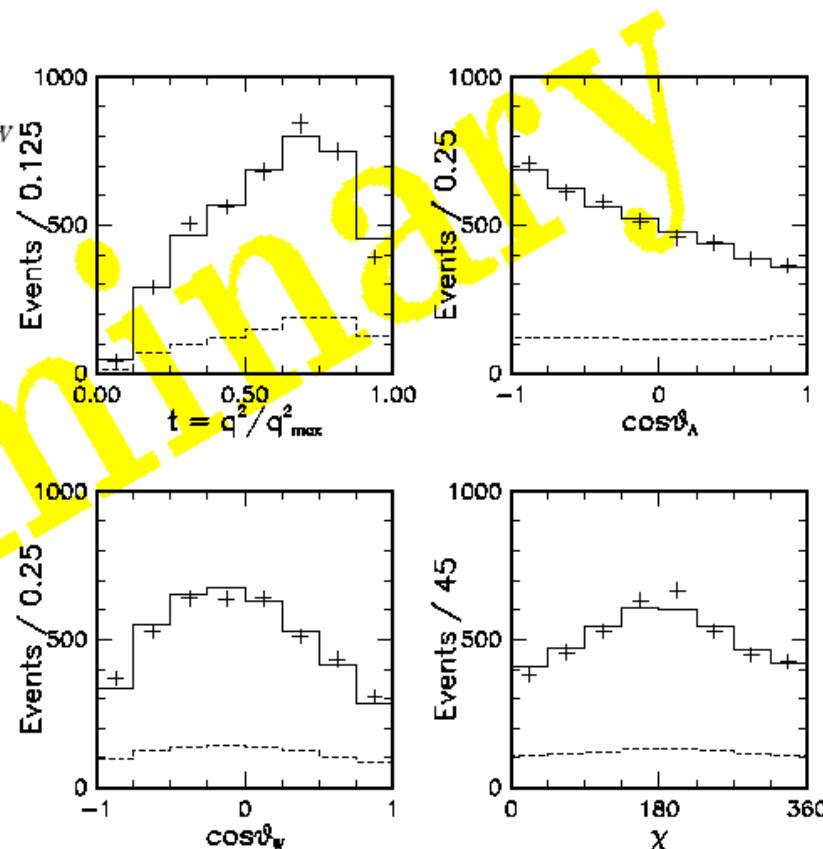
Search for CPV

- Split statistics for two charge conjugate states:

$$\alpha_{\Lambda_c^+} \alpha_\Lambda = -0.561 \pm 0.026_{\text{stat}} \\ \alpha_{\Lambda_c^-} \alpha_{\bar{\Lambda}} = -0.535 \pm 0.024_{\text{stat}}$$

- CP asymmetry:

$$A_{\Lambda_c^+} = \frac{\alpha_{\Lambda_c^+} + \alpha_{\Lambda_c^-}}{\alpha_{\Lambda_c^+} - \alpha_{\Lambda_c^-}} = 0.01 \pm 0.03_{\text{stat}} \pm 0.01_{\text{syst}} \pm 0.02_{\alpha_\Lambda}$$



Semileptonic Round-up

$$D^+ \rightarrow \bar{K}^{*0} \mu^+ \nu$$

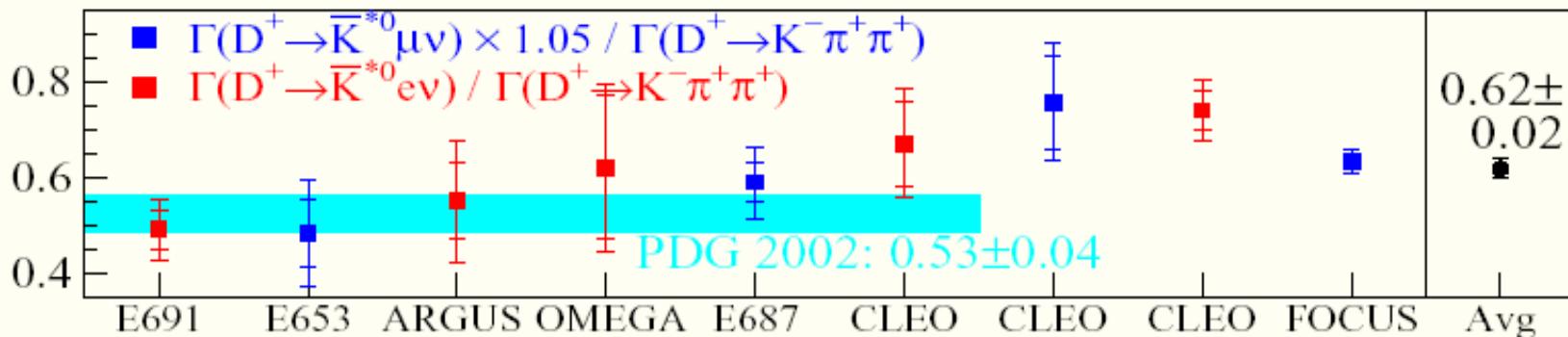
Interference effects

Need other experiments to look

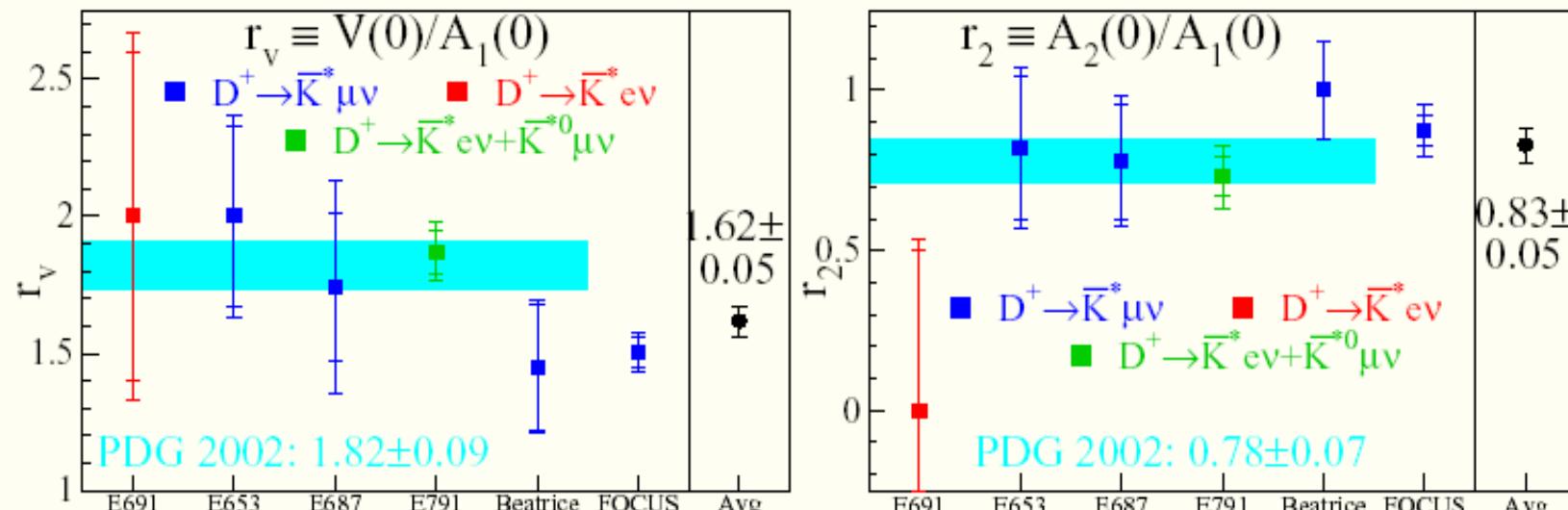
Very Interesting!

Probably more in there...

Branching ratio: (FOCUS includes effect of scalar interference) Lowers by 5.5%



Form factors: (FOCUS includes effect of scalar interference)

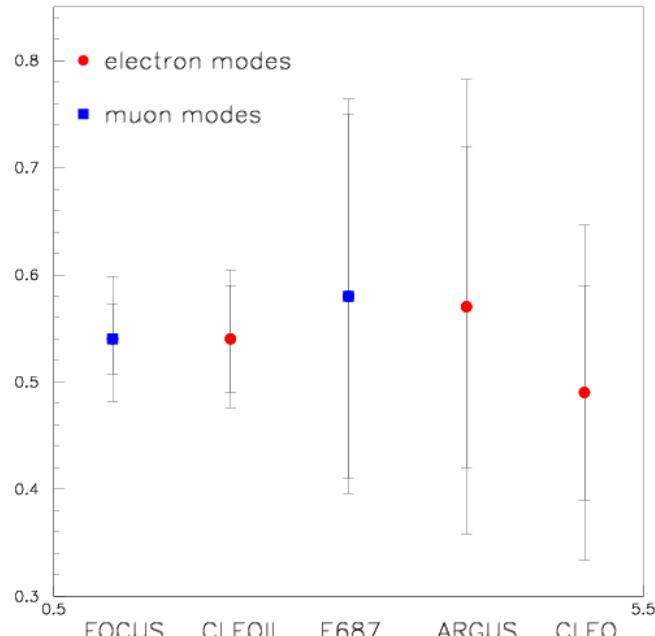


(From K. Stenson's APS review)

Semileptonic Round-up

$$\frac{\Gamma(D_s^+ \rightarrow \phi \mu^+ \nu)}{\Gamma(D_s^+ \rightarrow \phi \pi^+)}$$

We all seem to agree!



$$\Lambda_c^+ \rightarrow \Lambda^0 e^+ \nu$$

No Surprises!

No CP violation

f_2 / f_1 close to expected

α_{Λ_c} Expect ~-1 from HQET

Good agreement
in the Distributions

I didn't miss 'em!

$\Omega_C^0 \rightarrow \Omega^- \ell^+ \nu_\ell$ BELLE (Ruslan Chistov will cover in Spectroscopy)

$D^0 \rightarrow K^{*+} e^- \nu$ CLEO (Too preliminary)

$\Omega_C^0 \rightarrow \Omega^- e^+ \nu_e$ CLEO (Too preliminary)

$D_s^+ \rightarrow \eta \ell \nu$ CLEO (Too preliminary)

Would be nice to measure:

$D^0 \rightarrow \pi^+ e^- \nu_e$, $D^0 \rightarrow K^+ e^- \nu_e$

$D^+ \rightarrow \bar{K}^{*0} \mu^+ \nu$ Interference effects confirmed

$D \rightarrow P \ell \nu / D \rightarrow V \ell \nu$

Rare Decays from CDF, BELLE and BARBAR