

Looking for gluonic hybrid charmonium  
in  $e^+e^-$  at BaBar and Belle

And the accidental discovery of a new spectroscopy?

Work by FC with Clark Downum; Chris Thomas and Tim Burns

# gluonic degrees-of-freedom

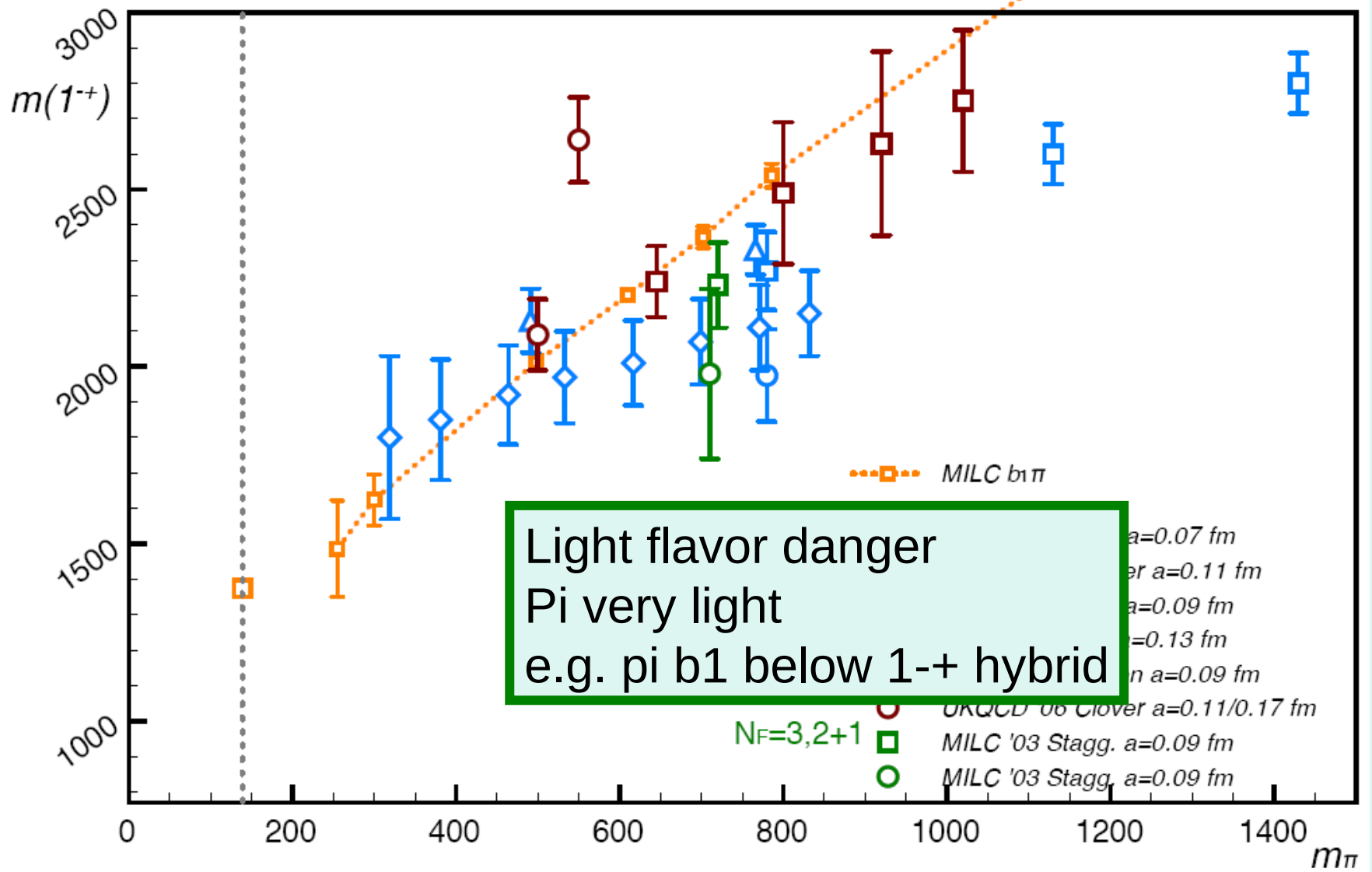


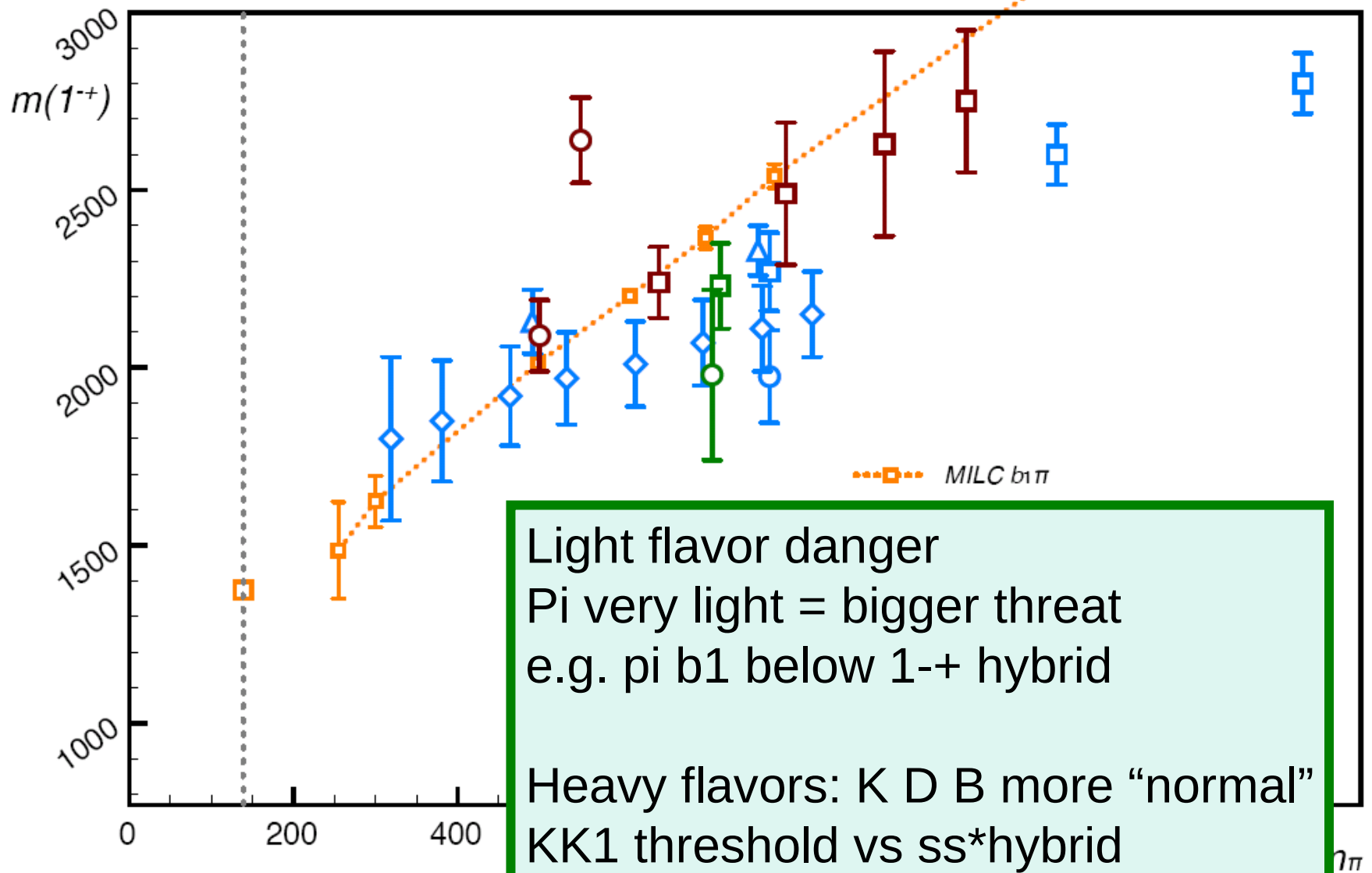
**Costs about 1 to 1.5GeV energy to excite phonon  
“ $\pi/R$ ”  
Hybrid  $qq^*$  @ 2GeV; Hybrid  $cc^*$  @ 4-4.5GeV**

Barnes FC Swanson 93

TABLE I. Predicted  $1^{-+}$  Hybrid Masses.

state	mass (GeV)	model
$H_{u,d}$	1.3-1.8	bag model
	1.8-2.0	flux tube model
-	<p>\sim 2.2 GeV <math>ss^*</math> quarks LGT</p> <p>\sim 2 GeV <math>ud</math> flavours.....</p> <p>.....but beware.....</p>	UKQCD...
-		





Light flavor danger  
 Pi very light = bigger threat  
 e.g. pi b1 below 1-+ hybrid  
 Heavy flavors: K D B more "normal"  
 KK1 threshold vs ss\* hybrid  
 DD1 threshold versus cc\* hybrid  
 BB1 threshold versus bb\* hybrid

## Predicted 1-+ Hybrid masses (with spin splittings)

---

$H_c$	$\approx 3.9$	adiabatic bag model
	4.2-4.5	flux tube model
	4.1-5.3	QCD sum rules (most after 1984)
	4.19(3) $\pm$ sys.	HQLGT

---

# charmonium

## Predicted 1-+ Hybrid masses (with spin splittings)

---

$H_c$	$\approx 3.9$	adiabatic bag model
	4.2-4.5	flux tube model
	4.1-5.3	QCD sum rules (most after 1984)
	4.19(3) $\pm$ sys.	HQLGT

---

# charmonium

Near  $D(L=0)+D(L=1)$  thresholds: **DD0; DD1; D\*D0; D\*D1**  
and strongly coupled to these channels

# Predicted 1-+ Hybrid masses (with spin splittings)

$H_c$	$\approx 3.9$	adiabatic bag model
	4.2-4.5	flux tube model
	4.1-5.3	QCD sum rules (most after 1984)
	4.19(3) $\pm$ sys.	HQLGT

## Spin hyperfine splittings

Barnes FC 82  
Chanowitz Sharpe

e+e- feebly coupled

e+e-  $\rightarrow$   $\psi$  + X?

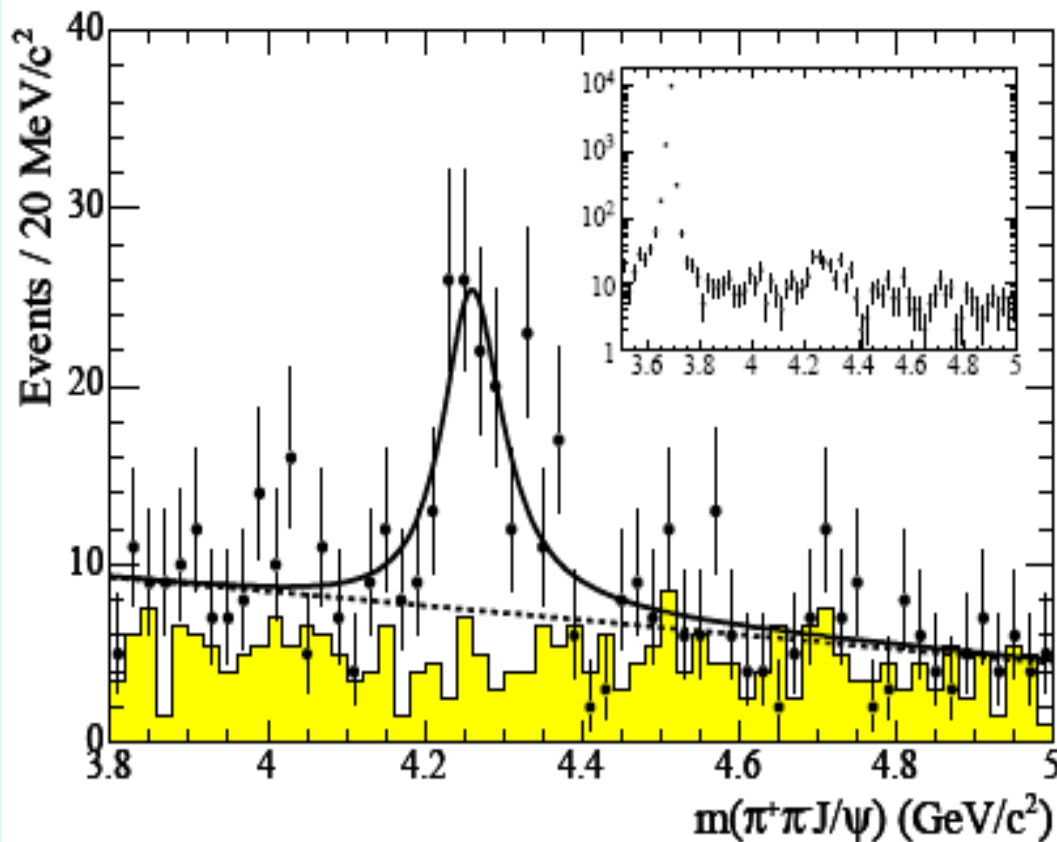
1- - (4.25) Y(4260?)

1- + (4.1) HQLGT

0- + (3.95) X(3940?)



# $e^+e^- \rightarrow \psi \pi^+ \pi^-$ BaBar sees unusual vector $cc^*$



**Y(4260)**

No sign of established  
3S/2D(4040/4160)  
4S(4400)  
in the  $\psi \pi^+ \pi^-$  data

Y(4260) thus seems  
anomalous

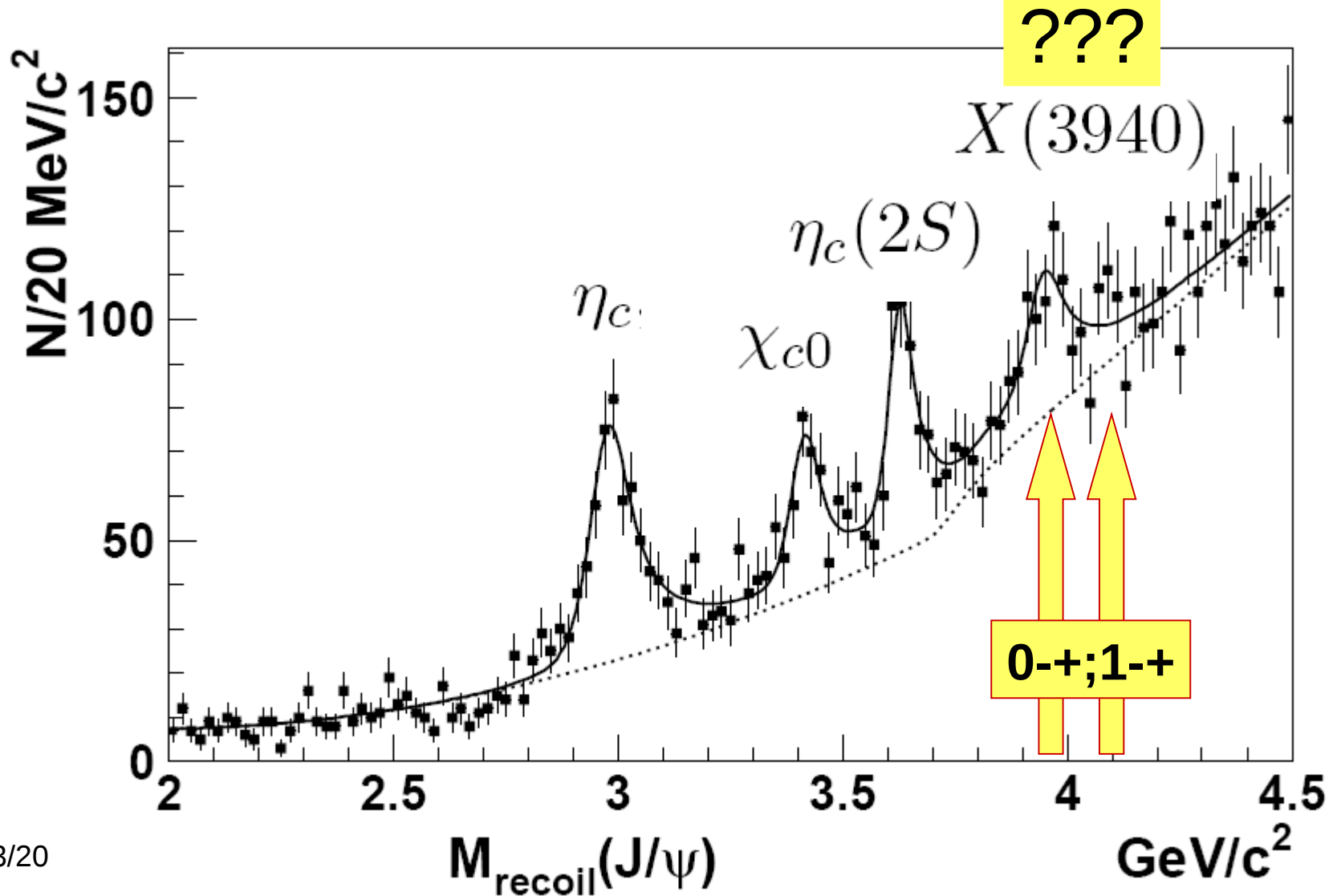
Also no place  
for extra  $cc^*$  state

$\Gamma(e^+e^-)$  5-80eV  
Compare  $\sim 1$  keV !!

But width 90MeV dominantly  $\psi \pi^+ \pi^-$  !

Belle

$e^+e^- \text{ to } \psi + X$



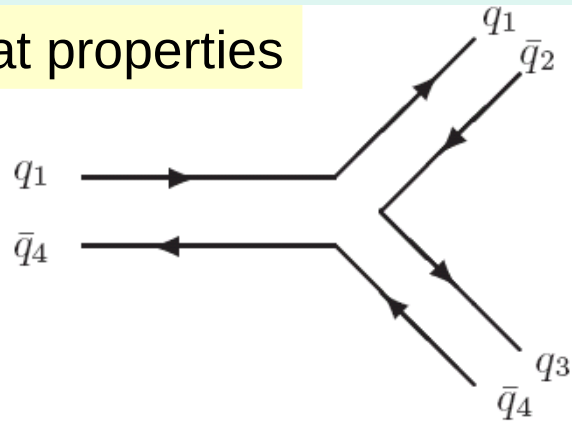
# Beyond Spectroscopy

To do more need dynamics:  
Production; decays; selection rules

What can lattice say?

Lattice decay and FT compare  
Factorisation of OZI  
Application to hybrids

## What properties

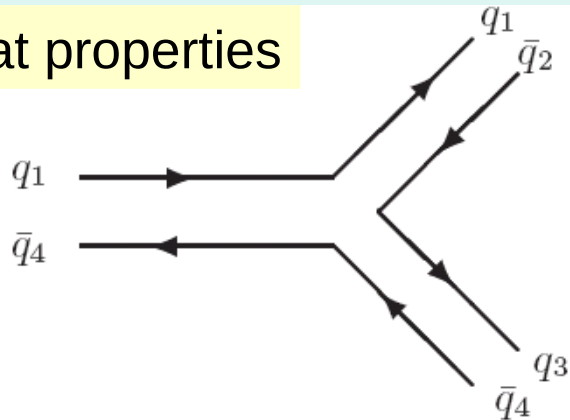


PHYSICAL REVIEW D 77, 034008 (2008)

## Dynamics of hadron strong production and decay

T. J. Burns,<sup>\*</sup> F. E. Close,<sup>†</sup> and C. E. Thomas<sup>‡</sup>

## What properties



PHYSICAL REVIEW D 77, 034008 (2008)

### Dynamics of hadron strong production and decay

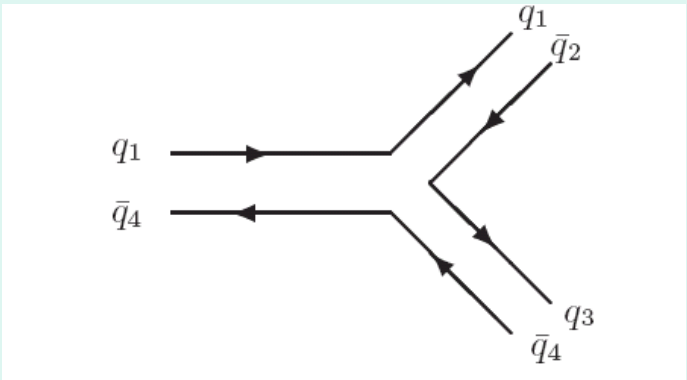
T. J. Burns,<sup>\*</sup> F. E. Close,<sup>†</sup> and C. E. Thomas<sup>‡</sup>

Lattice S-wave decays now calculated Michael McNeile  
confirms Flux Tube for hybrid:conventional

	$\pi_1 \rightarrow b_1(^1P_1)\pi$	$\pi_1 \rightarrow f_1(^3P_1)\pi$	
Lattice	$2.9 \pm 0.4$	$1.5 \pm 0.4$	← Michael McNeile 06
Flux tube	2.9	1.4	← FC Burns 06

Exactly **WHAT** is Lattice revealing about dynamics:  
What aspect(s) of Flux Tube model are being confirmed?

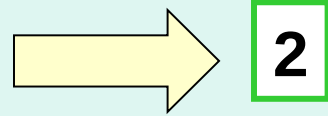
$${}^1P_1\pi : {}^3P_1\pi$$



qq\* create in S=1

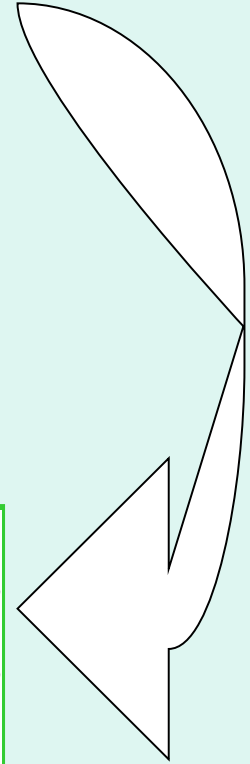
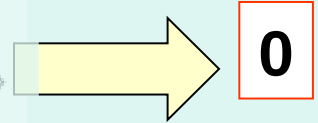
$$\left\{ \begin{matrix} 0 & 1 & 1 \\ 0 & 0 & 0 \\ 0 & 1 & 1 \end{matrix} \right\} \left\{ \begin{matrix} 0 & 1 & 1 \\ 0 & 1 & 1 \end{matrix} \right\} \left\{ \begin{matrix} 0 & 1 & 1 \\ 1 & 1 & 1 \end{matrix} \right\} \left\{ \begin{matrix} \frac{1}{2} & \frac{1}{2} & 0 \\ \frac{1}{2} & \frac{1}{2} & 0 \\ 1 & 1 & 0 \end{matrix} \right\}$$

$$\left\{ \begin{matrix} 1 & 1 & 1 \\ 0 & 0 & 0 \\ 1 & 1 & 1 \end{matrix} \right\} \left\{ \begin{matrix} 1 & 1 & 1 \\ 0 & 1 & 1 \end{matrix} \right\} \left\{ \begin{matrix} 1 & 1 & 1 \\ 1 & 1 & 1 \end{matrix} \right\} \left\{ \begin{matrix} \frac{1}{2} & \frac{1}{2} & 1 \\ \frac{1}{2} & \frac{1}{2} & 0 \\ 1 & 1 & 1 \end{matrix} \right\}$$



qq\* create in S=0

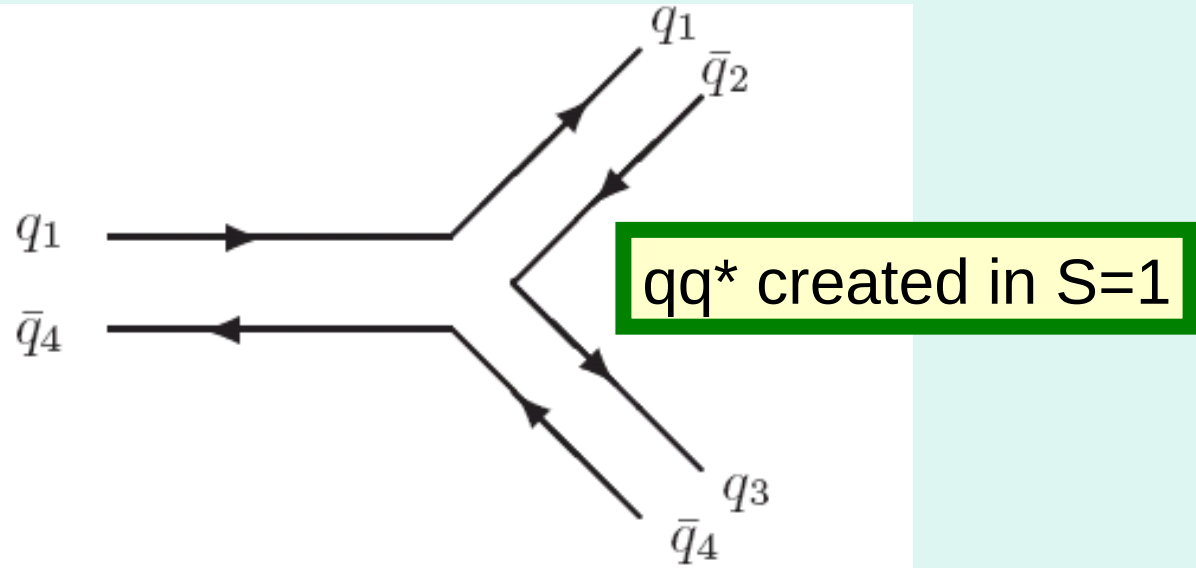
$$\left\{ \begin{matrix} \frac{1}{2} & \frac{1}{2} & 0 \\ \frac{1}{2} & \frac{1}{2} & 0 \\ 0 & 1 & 0 \end{matrix} \right\} : \left\{ \begin{matrix} \frac{1}{2} & \frac{1}{2} & 0 \\ \frac{1}{2} & \frac{1}{2} & 0 \\ 0 & 1 & 1 \end{matrix} \right\}$$



	$\pi_1 \rightarrow b_1({}^1P_1)\pi$	$\pi_1 \rightarrow f_1({}^3P_1)\pi$
Lattice	$2.9 \pm 0.4$	$1.5 \pm 0.4$
Flux tube	2.9	1.4

$$J - S = "L"$$

Factorisation of S and L



**Factorisation and S=1 creation is powerful result if generally true.**

S=0 cannot decay to S=0 + S=0 "spin singlet selection rule"

Determine nature of Y(4260) by DD\_1 pattern

SL Factorisation and S=1  
selection rules for  
 $\psi^*(cc^*) \rightarrow DD_1$

PHYSICAL REVIEW D 77, 034008 (2008)

Dynamics of hadron strong production and decay

T. J. Burns,<sup>\*</sup> F. E. Close,<sup>†</sup> and C. E. Thomas<sup>‡</sup>

$$\Gamma(^3S_1 \rightarrow D_{1H}D) = 0$$

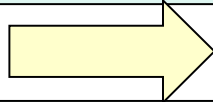
$$\Gamma(^3D_1 \rightarrow D_{1L}D) = 0$$

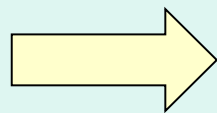
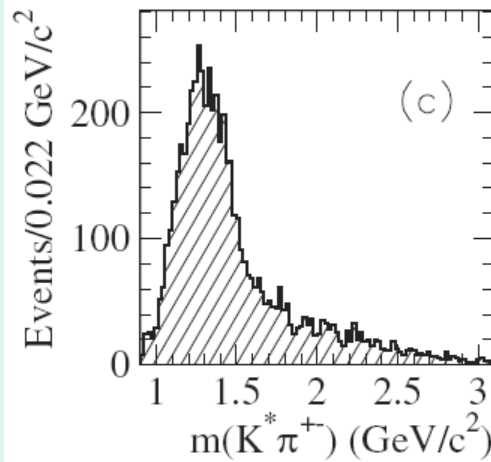
$$\Gamma(^1\Pi P_1(\text{hybrid}) \rightarrow D_1(^1P_1)D) = 0$$

Also applies to  $KK_1$  decays of  $ss^*$  vectors  
e.g. ISR around 2.2 GeV



$e^+e^- \rightarrow \pi^+\pi^-\pi^+\pi^-$ ,  $K^+K^-\pi^+\pi^-$ , and  $K^+K^-K^+K^-$  cross sections at center-of-mass energies 0.5–4.5 GeV measured with initial-state radiation

$e^+e^- \rightarrow$    $KK\_1$

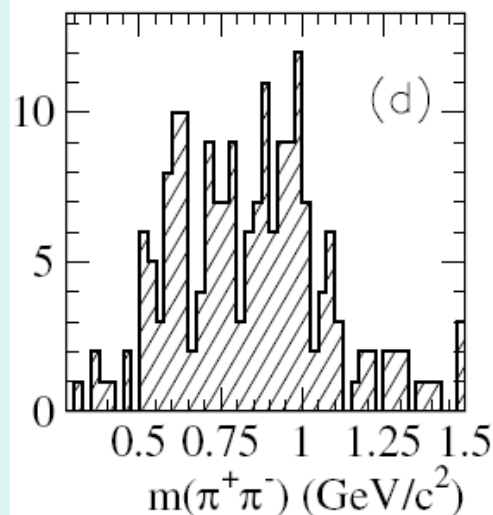
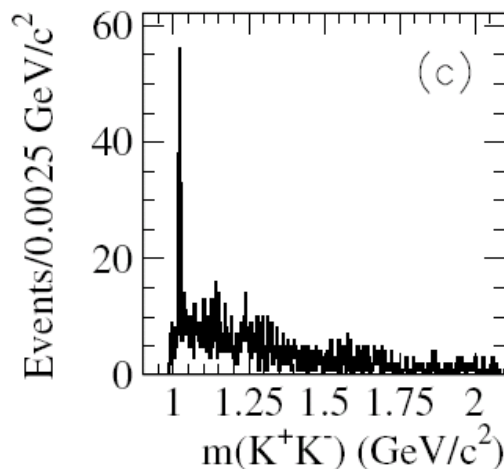


$\phi$

$\pi\pi$

Intriguing resonant signal at 2175 =  $\phi$ (hybrid)??

**2175 – m( $\phi$ ) = 4265 – m( $\psi$ ) !!??**



Jlab look in diffractive

SL Factorisation and S=1  
selection rules for  
 $\psi^*(cc^*) \rightarrow DD_1$

PHYSICAL REVIEW D 77, 034008 (2008)

Dynamics of hadron strong production and decay

T. J. Burns,<sup>\*</sup> F. E. Close,<sup>†</sup> and C. E. Thomas<sup>‡</sup>

$$\Gamma(^3S_1 \rightarrow D_{1H}D) = 0$$

$$\Gamma(^3D_1 \rightarrow D_{1L}D) = 0$$

$$\Gamma(^1\Pi P_1(\text{hybrid}) \rightarrow D_1(^1P_1)D) = 0$$

Problem is – it can fail **BIG**

Factorisation implies a **small scalar**

$$\sigma(e^+e^- \rightarrow {}^3S_1 + {}^3P_1) > \sigma(e^+e^- \rightarrow {}^3S_1 + {}^3P_0)$$

$${}^3S_1 \quad \sigma(\psi\chi_2) \rightarrow 0$$

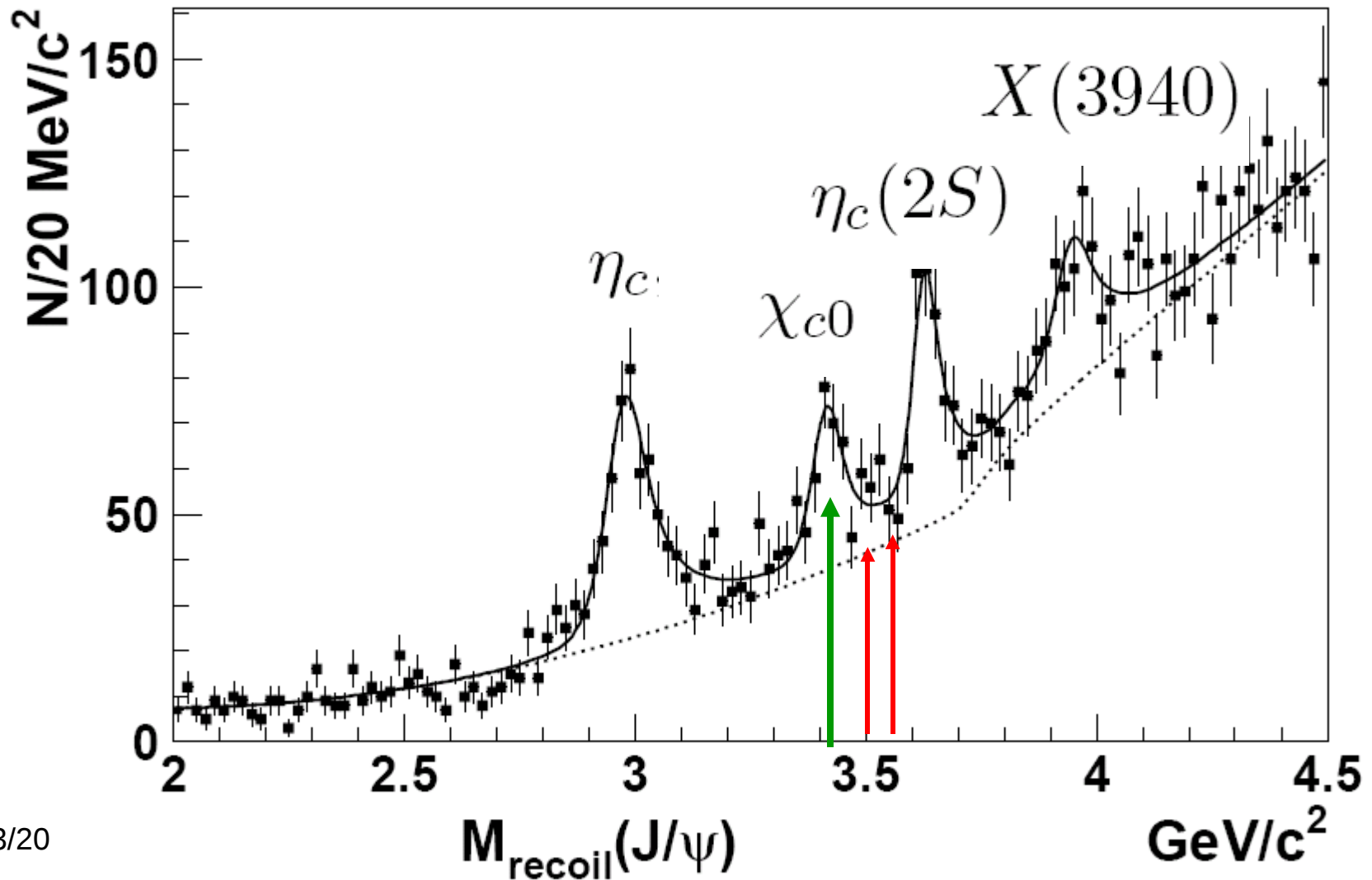
$$\sigma(\psi\chi_0) = \frac{3}{4}\sigma(\psi\chi_1).$$

$${}^3D_1 \quad \sigma(\psi\chi_0) \rightarrow 0$$

$$\sigma(\psi\chi_1) = \frac{5}{3}\sigma(\psi\chi_2)$$

Belle

$e^+e^- \text{ to } \psi + X$



Factorisation implies a small scalar

$$\sigma(e^+e^- \rightarrow {}^3S_1 + {}^3P_1) > \sigma(e^+e^- \rightarrow {}^3S_1 + {}^3P_0)$$

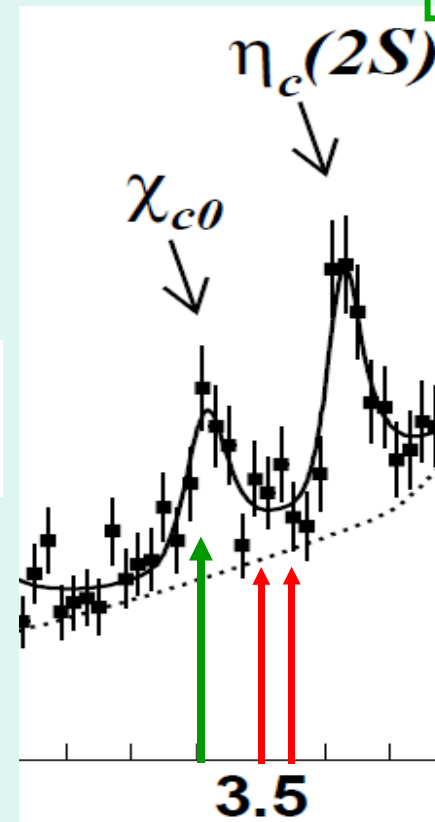
OgE implies a LARGE scalar

$$\sigma(\psi\chi_2 : \psi\chi_1 : \psi\chi_0) \sim 5 : 3 : 121.$$

Charmonium production in  $e^+e^- \rightarrow \psi + X(c\bar{c})$  and  $e^+e^- \rightarrow D^*D_J$

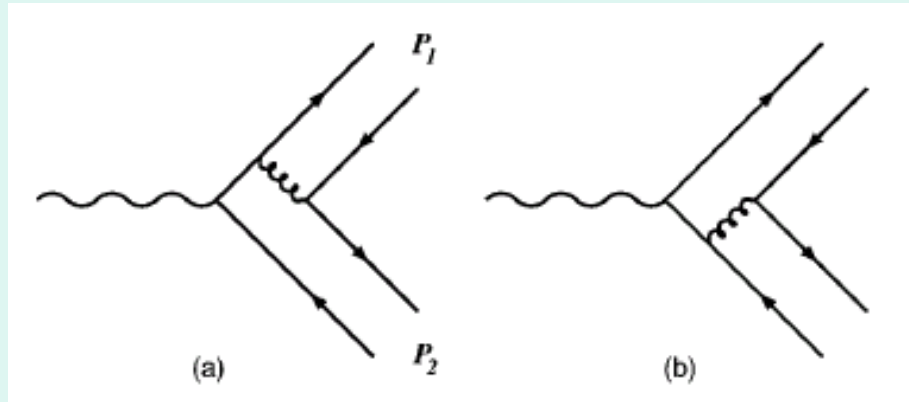
Frank Close\*  
Rudolf Peierls Centre for Theoretical Physics,  
University of Oxford,  
1 Keble Road, Oxford, OX1 3NP

Clark Downum†  
Clarendon Laboratory, University of Oxford,  
Parks Road, Oxford, OX1 3PU



Data =  
Large  
(only?)  
scalar

# Charm meson production: V+(SAT)

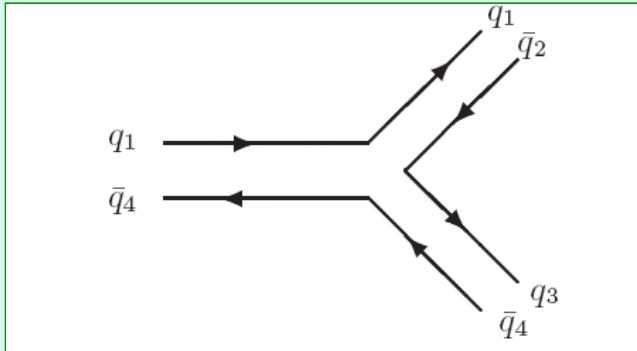


ONLY  $D^* D_0$ ; not  $D^* D_1$  or  $D^* D_2$

Test factorisation rule:

$$e^+e^- \rightarrow D^*(-)D_2(++)=0$$

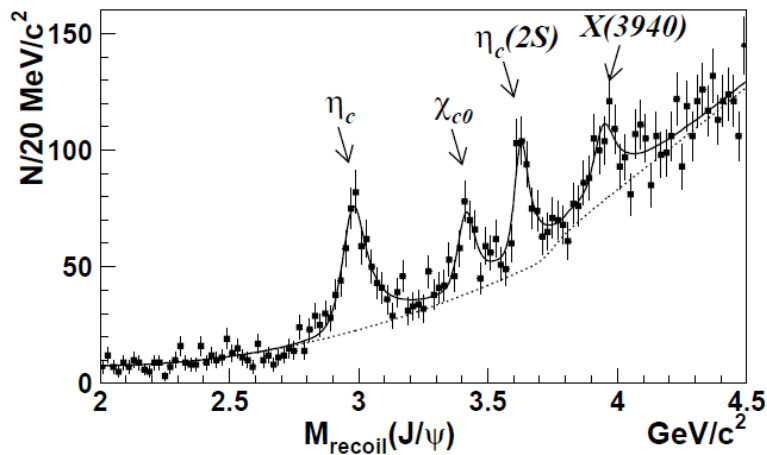
# Summary



Factorisation of J and S (L)

Dynamics driven by Clebsches

Selection rules:  $V(-)T(++)=0$



Large scalar =  $0gE$

Violates selection rules:  $V(-)T(++)$  large

4260 decays....

...using strong selection rules  
to distinguish candidates...

Conventional charmonium

Hybrid charmonium

Tetraquark  $csc^*s^*$ ;

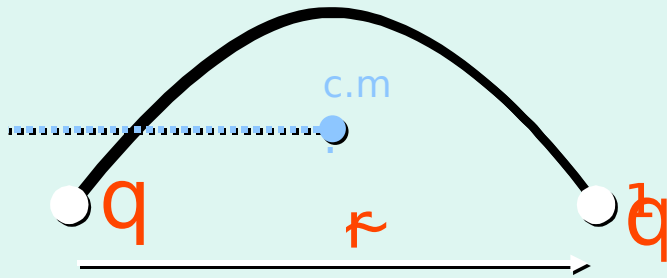
Charm molecule  $D^*D1$



# flux-tube breaking and hybrid decays

Isgur Paton 92 light exotics

FC Page 95 all

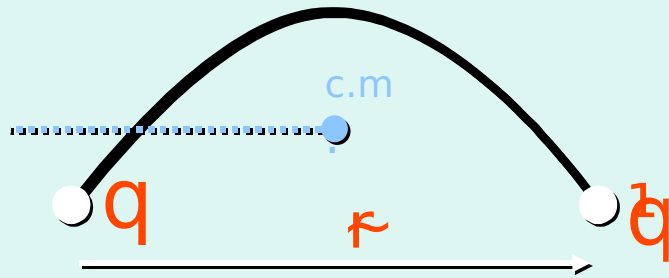


**Break tube: S+P states yes; S+S suppressed**

# flux-tube breaking and hybrid decays

Isgur Paton 92 light exotics

FC Page 95 all



**Break tube: S+P states yes; S+S suppressed**

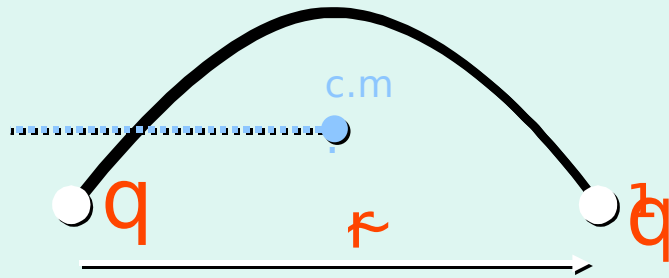
**Look for DD<sub>1</sub> and D\*D<sub>0</sub> near threshold**

**Look for psi pipi and h1c eta**

# flux-tube breaking and hybrid decays

Isgur Paton 92 light exotics

FC Page 95 all



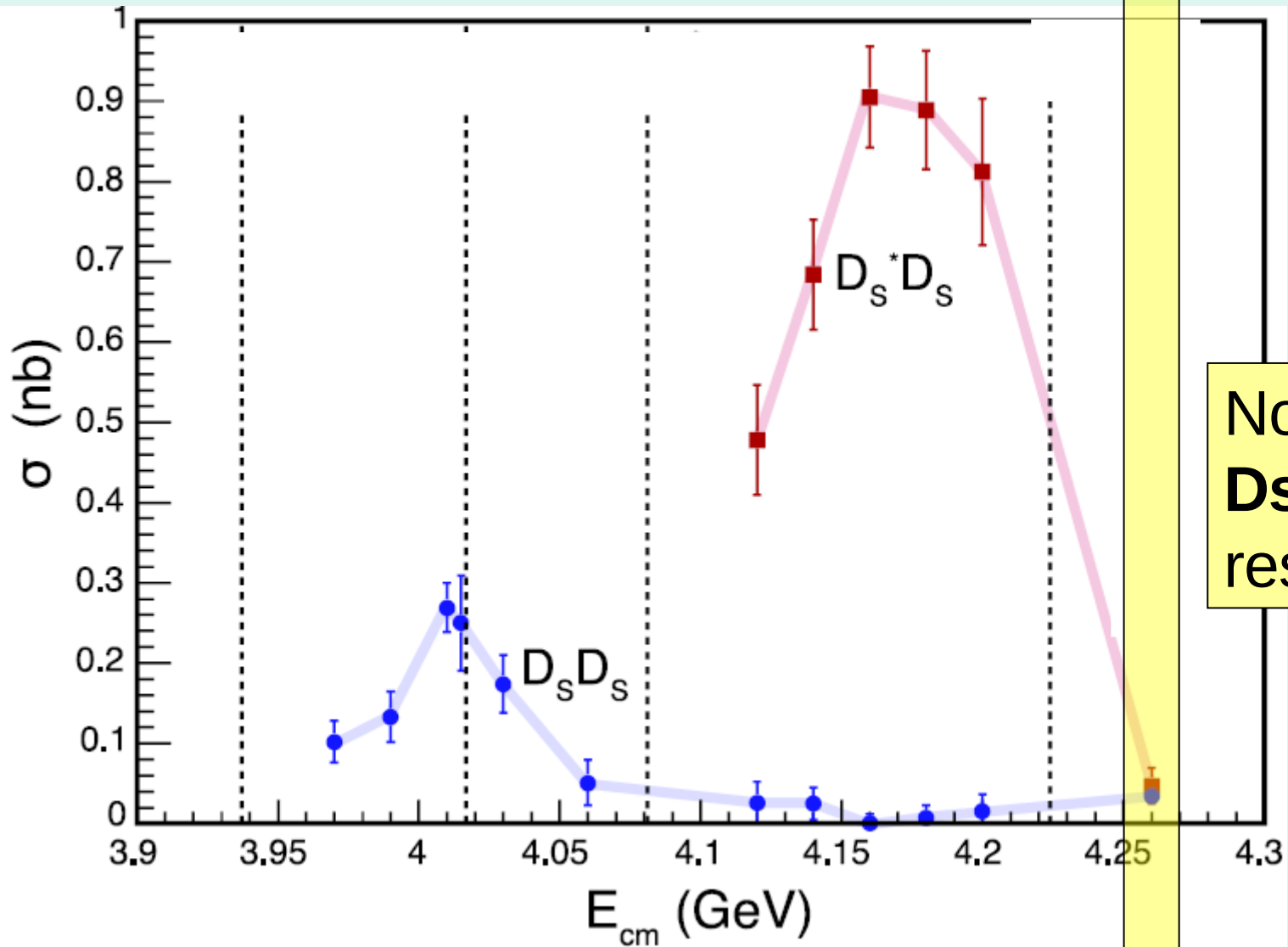
**Break tube: S+P states yes; S+S suppressed**

**Look for DD<sub>1</sub> and D\*D<sub>0</sub> near threshold**

**Look for psi pipi and h1c eta**

**Absence of DD; DD\*; DsDs ...**

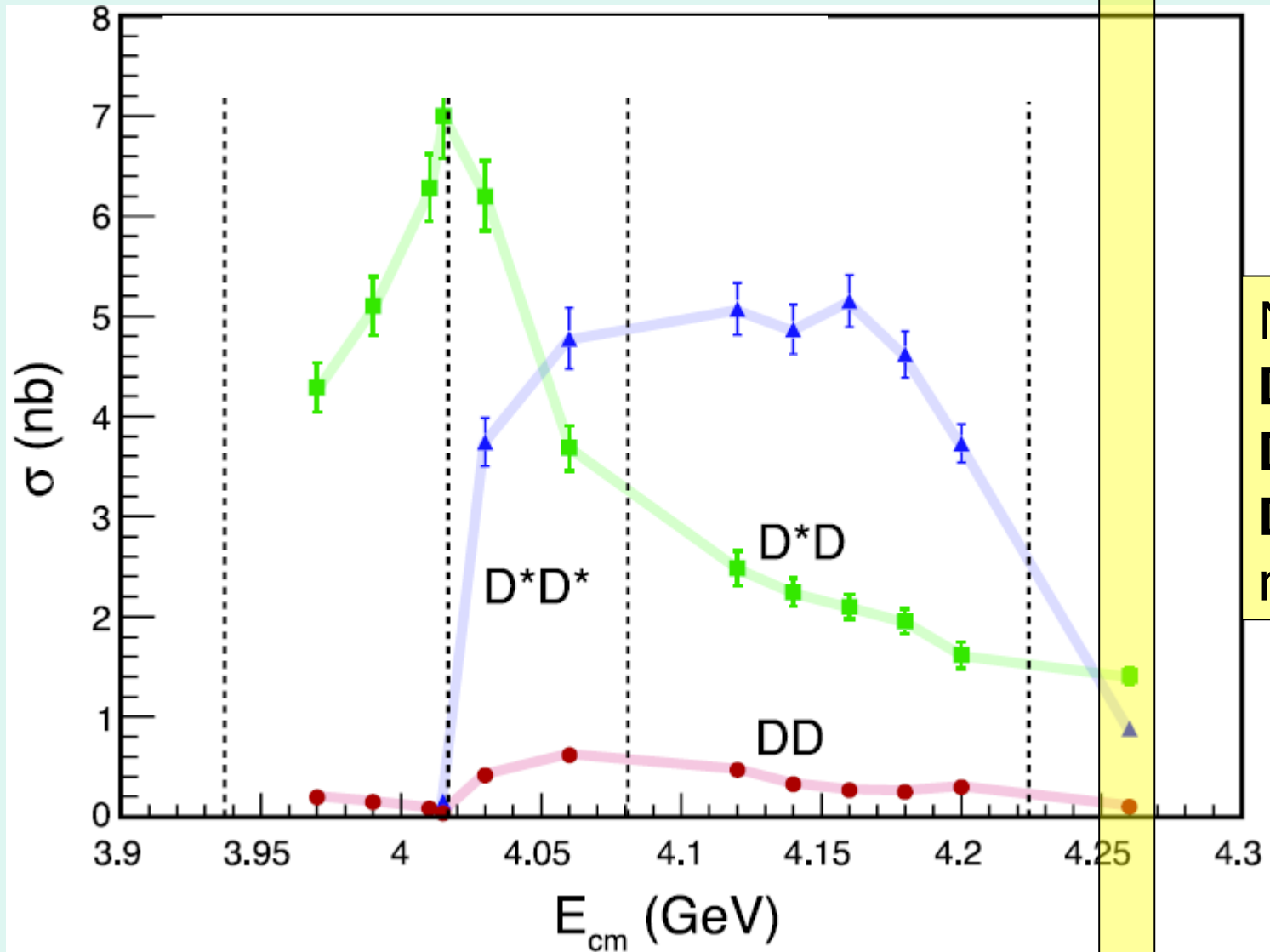
# Y(4260): $D_s$ and $D_s^*$ channels



No  
**DsDs**  
resonance

eliminates  
tetraquark  
 $csc^*s^*$

# Y(4260): D and D\* channels



No  
DD  
DD\* or  
D\*D\*  
resonance

# All consistent with **predictions** for hybrid charmonium

FC+Page 1995

*The mass coincides with the  $D_1(2420)D$  threshold:*

*The decay modes  $\psi\sigma/\eta$ ,  $\psi f_0(980)/a_0(980)$  appear to dominate:*

*$\Gamma(Y(4260) \rightarrow e^+e^-)$  is much smaller than all other  $1^{--}$  charmonia:*

$$5.5 \text{ eV} \leq \Gamma(Y(4260) \rightarrow e^+e^-) \lesssim 62 \text{ eV},$$

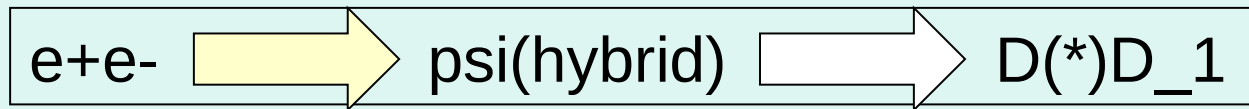
*$\Gamma(Y(4260) \rightarrow \psi\pi^+\pi^-)$  is much larger than all  $1^{--}$  charmonia:*

$$\Gamma(Y(4260) \rightarrow \psi\pi^+\pi^-) \gtrsim 7.8 \text{ MeV}.$$

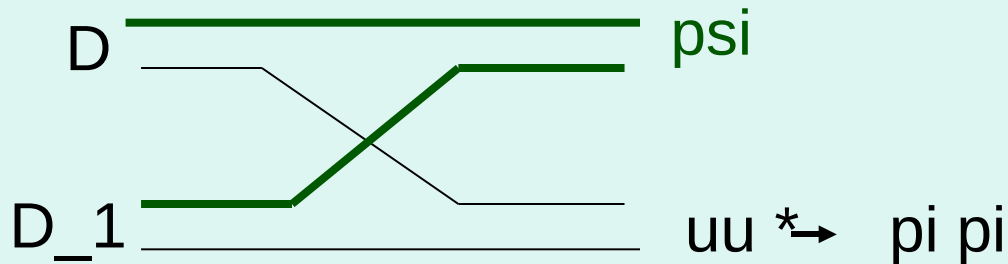
**Search  $DD_1$  and  $D^*D_0$  in  $DD\pi\pi$**

**If NOT hybrid  $cc^*$  then why not/where is it ?!**

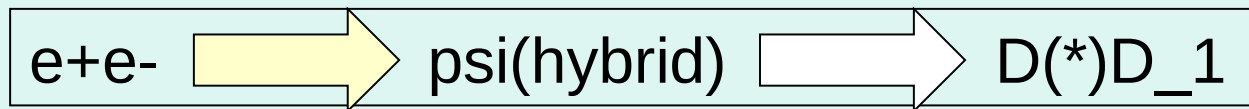
# The large $\psi + \pi \pi = \text{hint of large } D^{(*)}D_1$



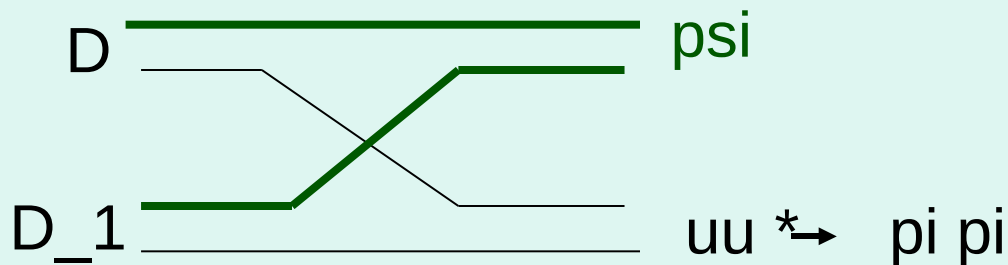
S-wave, relative mom  $\sim 0$ ;  
 $D D_1$  interchange constituents to make  $\psi \pi \pi$  “strongly”



# The large $\psi + \pi \pi = \text{hint of large } D^{(*)}D_1$



S-wave, relative mom  $\sim 0$ ;  
 $D D_1$  interchange constituents to make  $\psi \pi \pi$  “strongly”



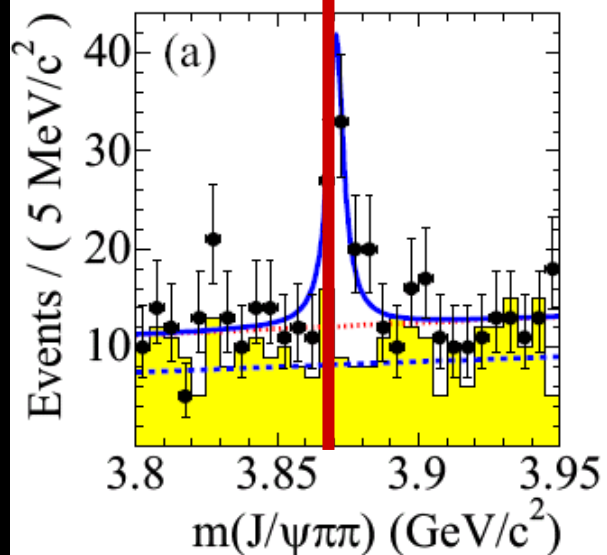
Problem: Heavy  $cc^*$  preserve their spin.  
 $\psi$  has  $cc^*$  with  $S=1$   
 Hybrid has  $cc^*$  with  $S=0$

Problem: and other states: 4360;4430...



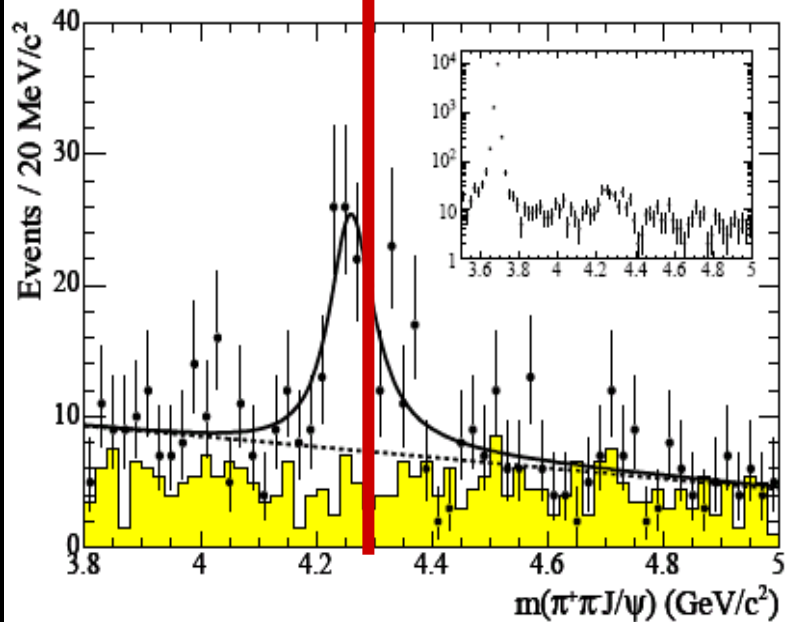
1<sup>++</sup>(3872)

DD\*



1<sup>--</sup>(4260)

DD1

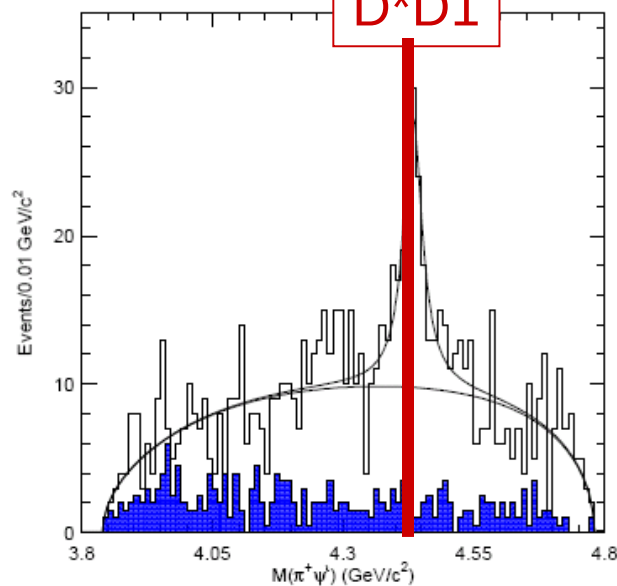


JPC?(4430)

|=1 !?

Pi psi\*  
What about  
Pi psi??

D\*D1



Hybrid affected by thresholds

Attractive force from pi exchange:

4260 a result of  $D_1 D^*$  (!! ) threshold:  
look for  $e^+e^- \rightarrow D D\bar{b} + 3\pi$

And what about 4360 in  $\psi'$   $\pi\pi$   
and 4430 in  $\psi'$   $\pi$  .....????

# The Answer: A new spectroscopy

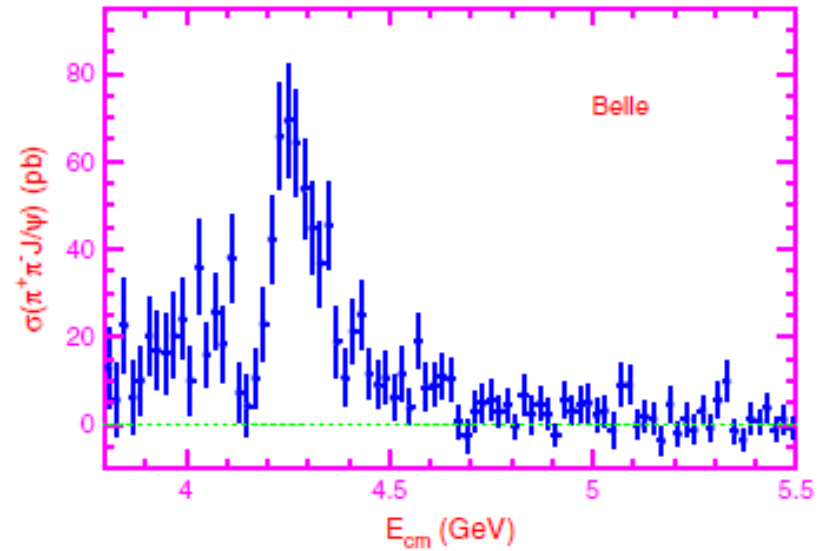
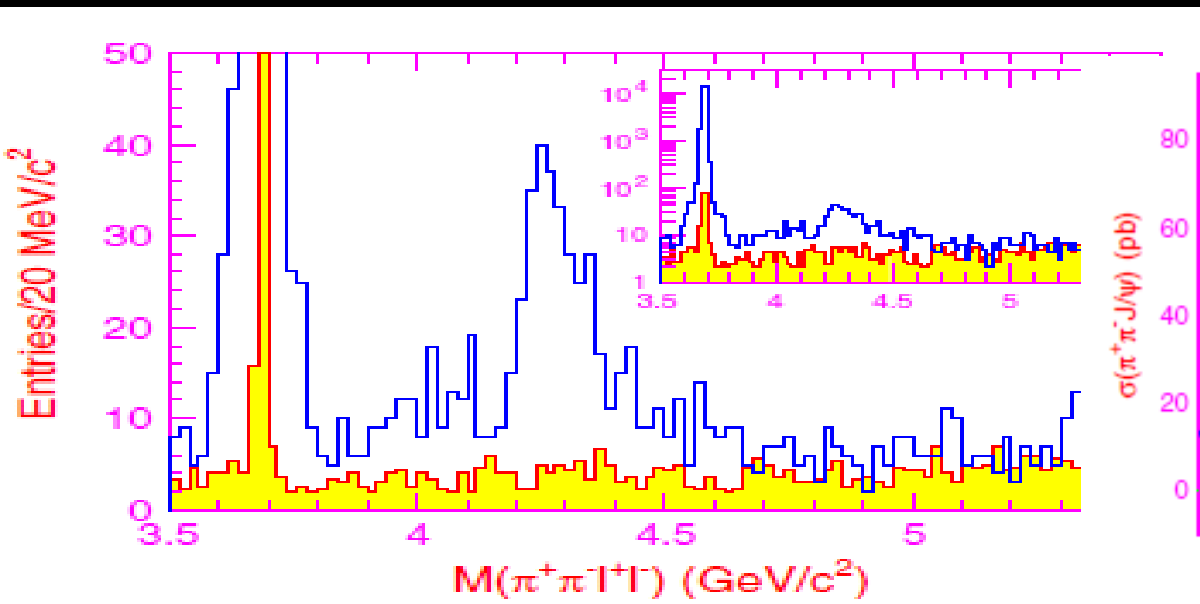
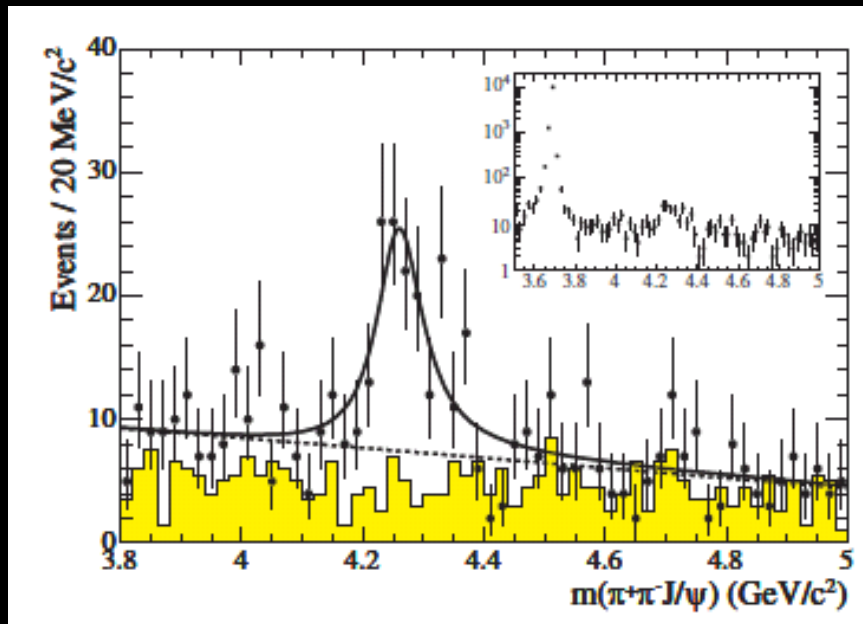
- At least.....something unexpected!
- $1^{++}(3872)$   $DD^*$  via  $\pi$  exchange in p-wave
- $1^-$  (4260 etc)  $D_1D^*$  via  $\pi$  exchange

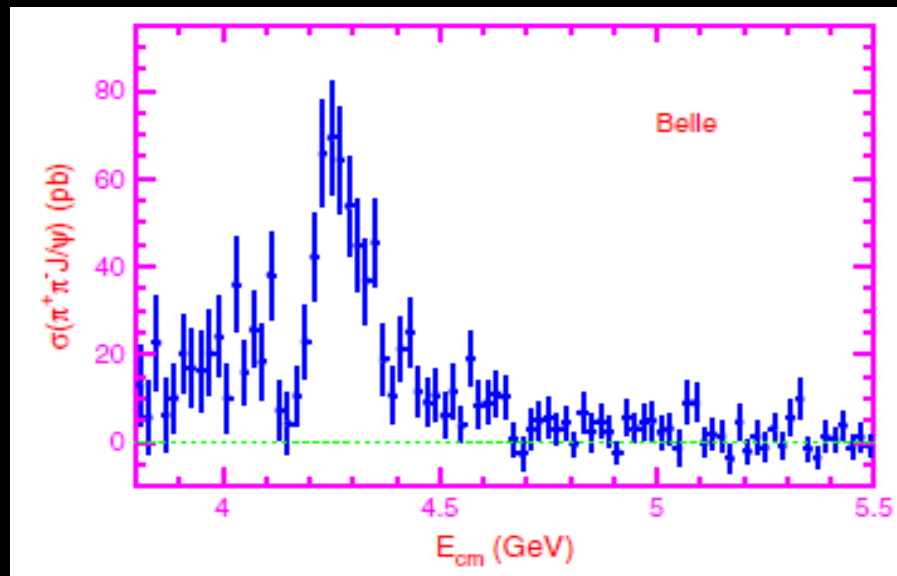
.....

# The Answer: A new spectroscopy

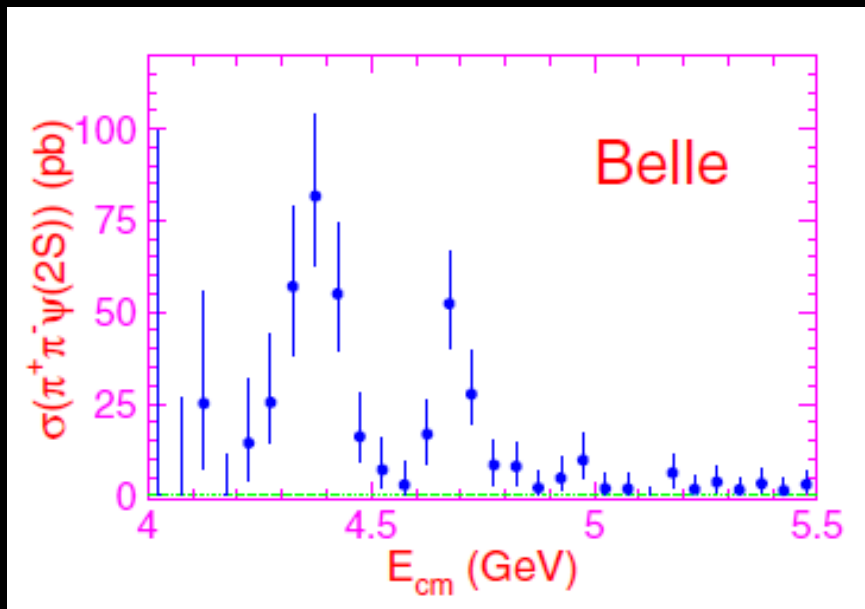
- At least.....something unexpected!
- $1^{++}(3872)$   $DD^*$  via  $\pi$  exchange in p-wave
- $1^-$  (4260 etc)  $D_1D^*$  via  $\pi$  exchange  
in **s-wave!**

# Psi ppi (4260)





**Psi(1S)pipi (4260)**



**Psi(2S)pipi (4360) and (?) 4600**

# On the possibility of Deeply Bound Hadronic Molecules from single Pion Exchange

Frank Close\*

*Rudolf Peierls Centre for Theoretical Physics, University of Oxford,  
1 Keble Road, Oxford, OX1 3NP*

Clark Downum†

*Clarendon Laboratory, University of Oxford,  
Parks Road, Oxford, OX1 3PU*

$$V_P(\mathbf{q}) = -\frac{g^2}{f_\pi^2} \frac{(\boldsymbol{\sigma}_i \cdot \mathbf{q})(\boldsymbol{\sigma}_j \cdot \mathbf{q})}{|\mathbf{q}|^2 + \mu^2} (\boldsymbol{\tau}_i \cdot \boldsymbol{\tau}_j)$$

N N pi: deuteron; **O(1 MeV)**

D\* to D pi (**P** wave) **O(q<sup>2</sup>)**

DD\* to D\*D binding **O(1 MeV)**

X(3872)

# On the possibility of Deeply Bound Hadronic Molecules from single Pion Exchange

Frank Close\*

*Rudolf Peierls Centre for Theoretical Physics, University of Oxford,  
1 Keble Road, Oxford, OX1 3NP*

Clark Downum†

*Clarendon Laboratory, University of Oxford,  
Parks Road, Oxford, OX1 3PU*

$$V_P(\mathbf{q}) = -\frac{g^2}{f_\pi^2} \frac{(\boldsymbol{\sigma}_i \cdot \mathbf{q})(\boldsymbol{\sigma}_j \cdot \mathbf{q})}{|\mathbf{q}|^2 + \mu^2} (\boldsymbol{\tau}_i \cdot \boldsymbol{\tau}_j)$$

N N pi: deuteron; **O(1 MeV)**

D\* to D pi (**P** wave) **O(q<sup>2</sup>)**

DD\* to D\*D binding **O(1 MeV)**

X(3872)

$$V_S(\mathbf{q}) = -\frac{h^2}{2f_\pi^2} \frac{(m_A - m_B)^2}{|\mathbf{q}|^2 + \mu^2}$$

D1 to D\* pi (**S** wave) **O(m<sub>A</sub>-m<sub>B</sub>)<sup>2</sup>**

D1 D\* binding **O(100 MeV)**

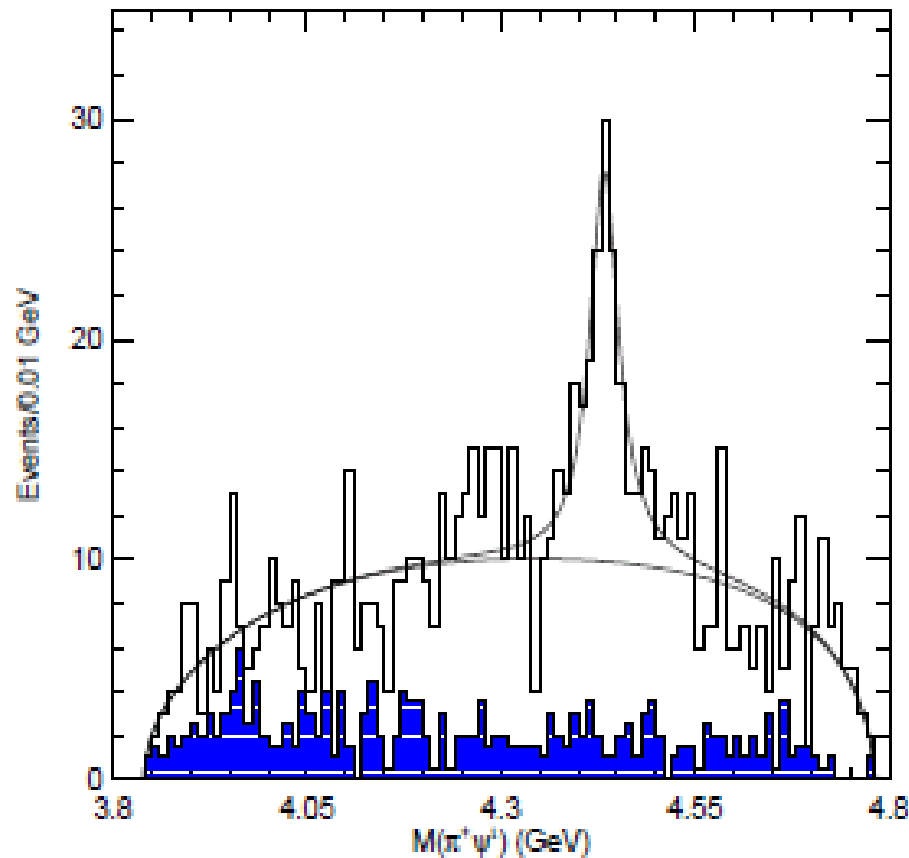
M = D\*D1(4440) - **O(100MeV)**

**4260; 4360 ??**



## Is $Z^+(4430)$ a loosely bound molecular state?

Xiang Liu,<sup>1,\*</sup> Yan-Rui Liu,<sup>2,†</sup> Wei-Zhen Deng,<sup>1,‡</sup> and Shi-Lin Zhu<sup>1,§</sup>



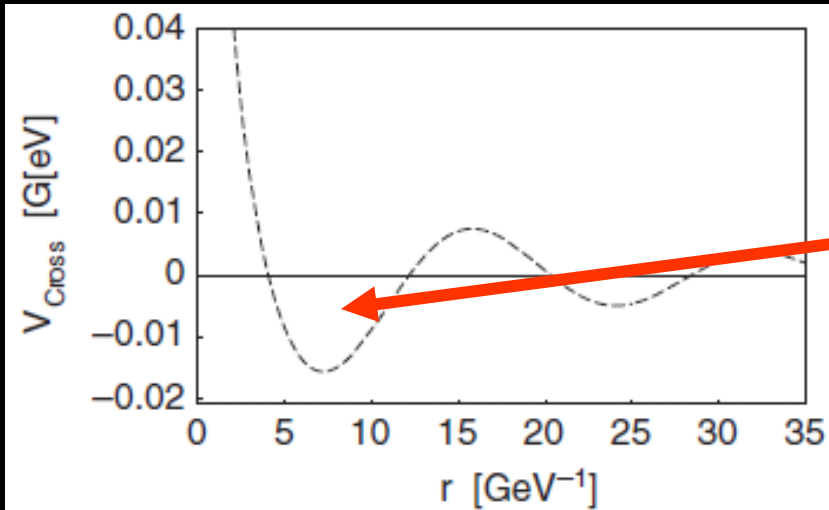
Look at  $I=1$   $D_1 D^* 1^{--}$   
S wave  $\pi$  exchange  
Find it does NOT bind

Is  $Z^+(4430)$  a loosely bound molecular state?

Xiang Liu,<sup>1,\*</sup> Yan-Rui Liu,<sup>2,†</sup> Wei-Zhen Deng,<sup>1,‡</sup> and Shi-Lin Zhu<sup>1,§</sup>

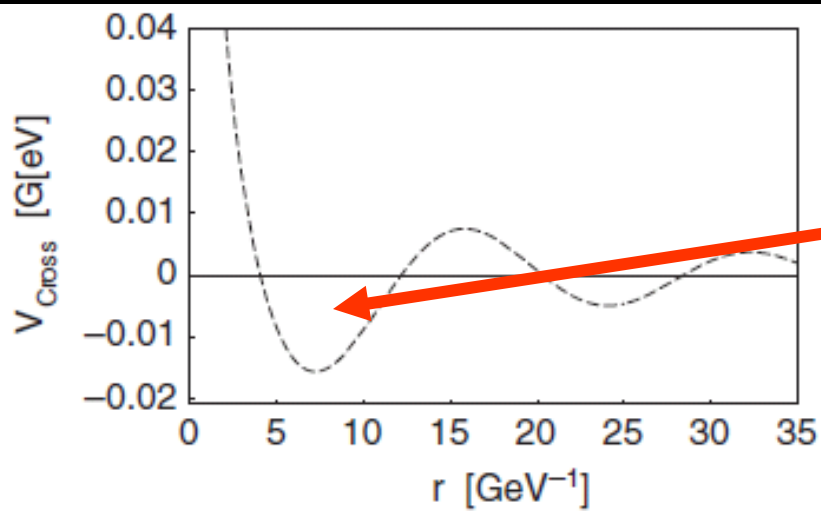
$$V_S(r) = \frac{h^2(m_A - m_B)^2 \cos(\mu r)}{8\pi f_\pi^2 r}$$

$$V_S(\mathbf{q}) = -\frac{h^2}{2f_\pi^2} \frac{(m_A - m_B)^2}{|\mathbf{q}|^2 + \mu^2}$$

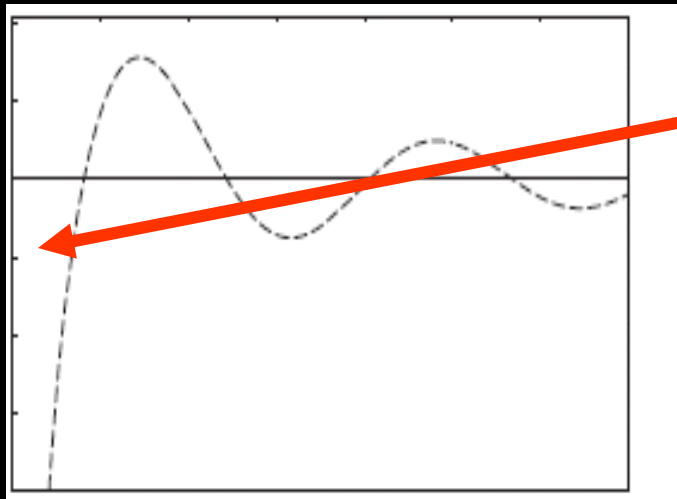


**I=1 feeble binding if any  
Z(4430)**

Liu et al PRD77 034003



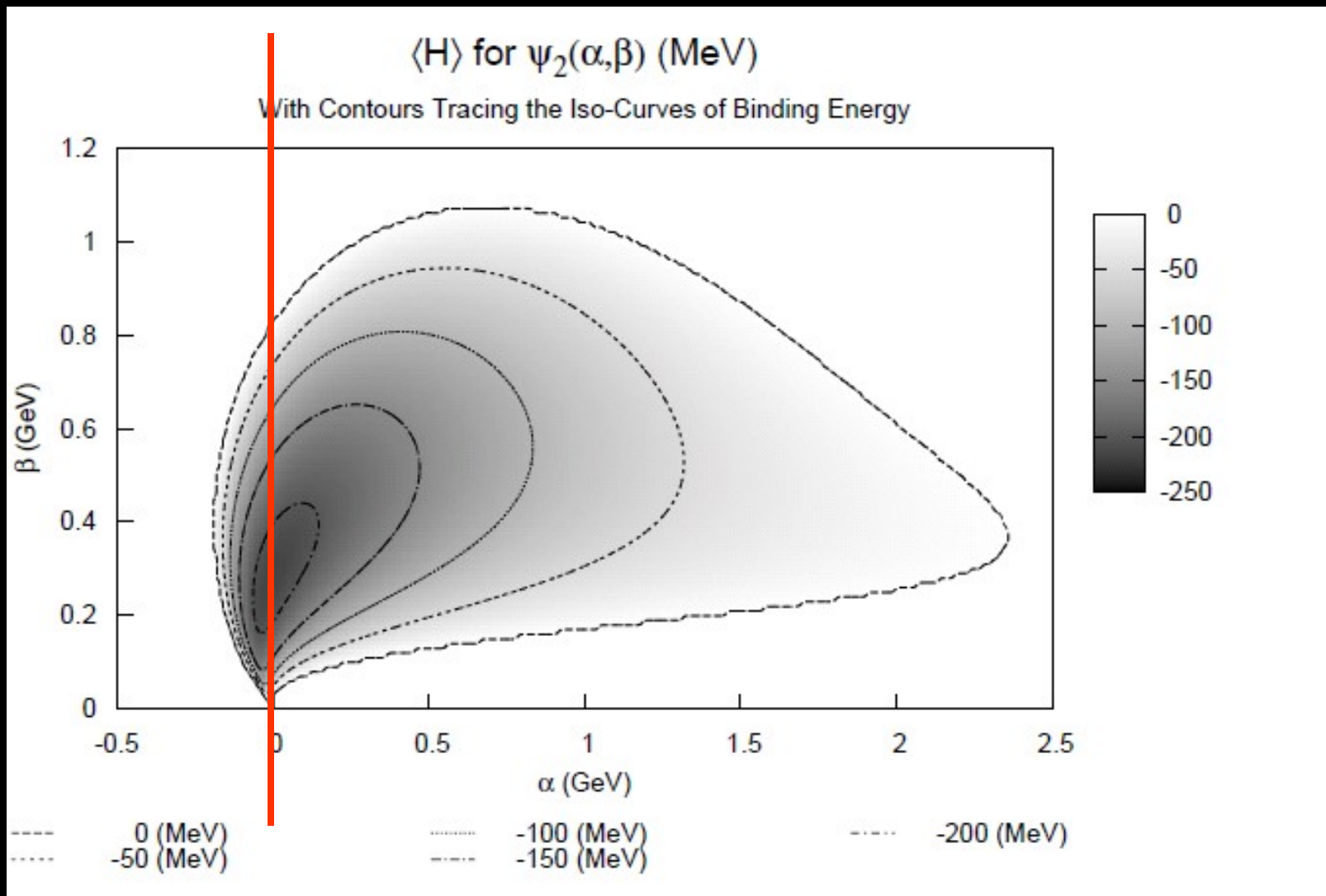
**I=1 feeble binding if any  
Z(4430)  
Liu et al PRD77 034003**



**I=0 strong binding**

# Binding Energy: variational wfns

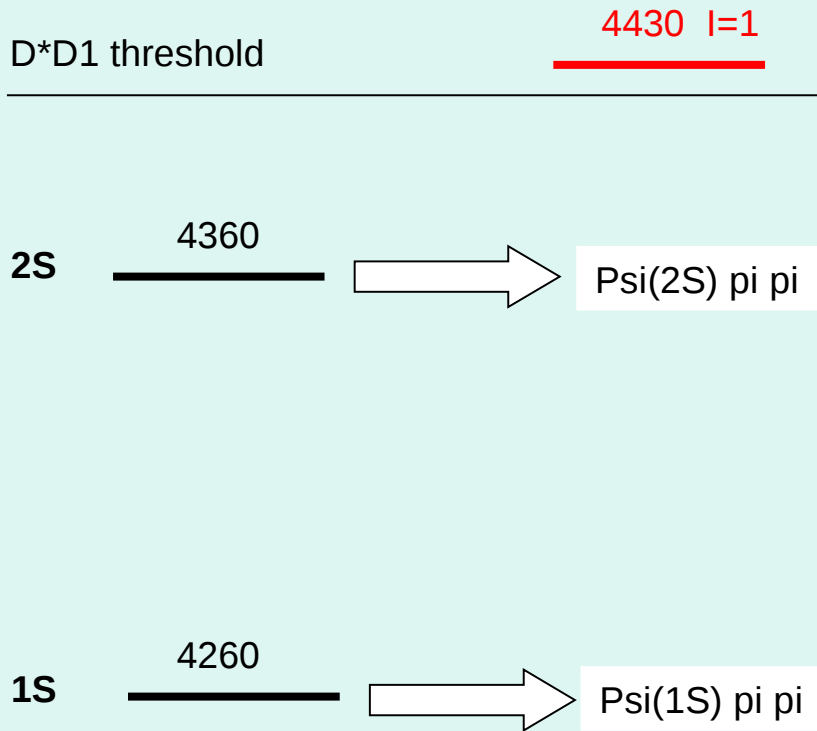
$$\psi(r) = (1 + \alpha r^2)e^{-\beta r^2}$$



Ground state B.E can be 100-200 MeV !!

Radial excitation bound also??

# Vector D\*D1 spectroscopy



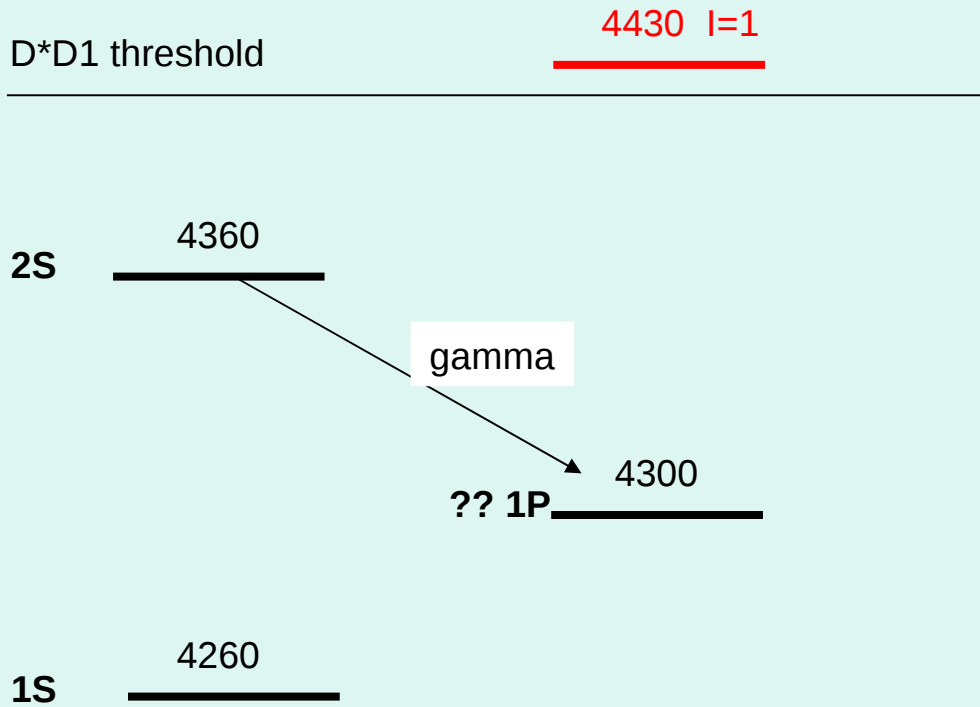
## On the new exotic charmonium states

Frank Close\*  
*Rudolf Peierls Centre for Theoretical Physics,  
University of Oxford,  
1 Keble Road, Oxford, OX1 3NP*

Clark Downum†  
*Clarendon Laboratory, University of Oxford,  
Parks Road, Oxford, OX1 3PU*

Also 0- 1- 2- with C=- or +

# Vector D\*D1 spectroscopy



## On the new exotic charmonium states

Frank Close\*  
*Rudolf Peierls Centre for Theoretical Physics,  
University of Oxford,  
1 Keble Road, Oxford, OX1 3NP*

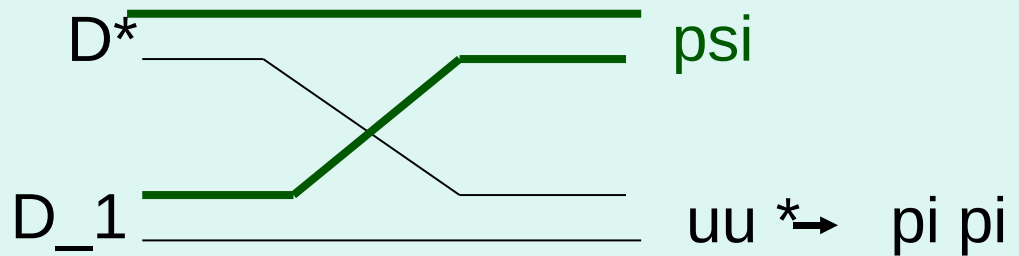
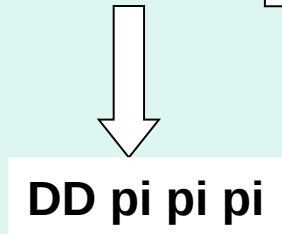
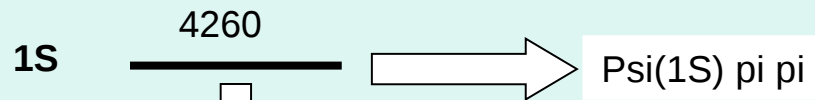
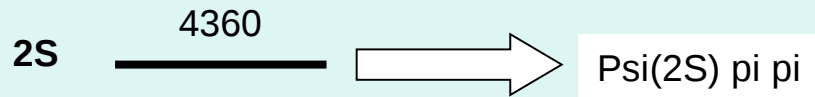
Clark Downum†  
*Clarendon Laboratory, University of Oxford,  
Parks Road, Oxford, OX1 3PU*

And Possible transitions to exotic 1-+

# Vector D\*D1 spectroscopy

4430 I=1

D\*D1 threshold



# On the possibility of Deeply Bound Hadronic Molecules from single Pion Exchange

Frank Close\*

*Rudolf Peierls Centre for Theoretical Physics, University of Oxford,  
1 Keble Road, Oxford, OX1 3NP*

Clark Downum†

*Clarendon Laboratory, University of Oxford,  
Parks Road, Oxford, OX1 3PU*

Phys Rev Letters (in press)

The immediate test is 4260 decay to

$$D\bar{D}3\pi$$

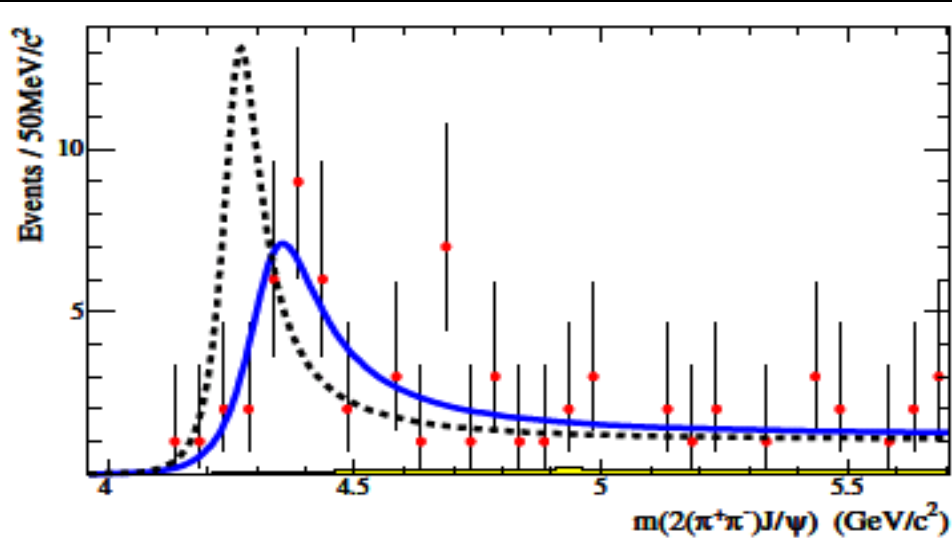
Then look for other exotica. Also in Bottomonium and strangeonium

Compare DD1 selection rules in DD 2pi for conventional or hybrid cc\*





ANTI-MATTER  
FRANK CLOSE



Psiprime pipi (4360)

And (??) (4600)

